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## 11/04/2023

## Evening

## Answers \& Solutions

Time : 3 hrs.
M.M. : 300

# JEE (Main)-2023 (Online) Phase-2 <br> (Mathematics, Physics and Chemistry) 

## IMPORTANT INSTRUCTIONS:

(1) The test is of $\mathbf{3}$ hours duration.
(2) The Test Booklet consists of 90 questions. The maximum marks are 300 .
(3) There are three parts in the question paper consisting of Mathematics, Physics and Chemistry having 30 questions in each part of equal weightage. Each part (subject) has two sections.
(i) Section-A: This section contains 20 multiple choice questions which have only one correct
answer. Each question carries $\mathbf{4}$ marks for correct answer and -1 mark for wrong answer.
(ii) Section-B: This section contains 10 questions. In Section-B, attempt any five questions out
of 10. The answer to each of the questions is a numerical value. Each question carries 4 marks
for correct answer and $\mathbf{- 1}$ mark for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

## MATHEMATICS

## SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

## Choose the correct answer:

1. The domain of the function $f(x)=\frac{1}{\sqrt{[x]^{2}-3[x]-10}}$ is (where $[x]$ denotes the greatest integer less than or equal to $x$ )
(1) $(-\infty,-3] \cup(5, \infty)$
(2) $(-\infty,-2) \cup[6, \infty)$
(3) $(-\infty,-2) \cup(5, \infty)$
(4) $(-\infty,-3] \cup[6, \infty)$

## Answer (2)

Sol. $f(x)=\frac{1}{\sqrt{[x]^{2}-3[x]-10}}$
For Domain $[x]^{2}-3[x]-10>0$
$\Rightarrow \quad([x]-5)([x]+2)>0$
$\Rightarrow[x] \in(-\infty,-2) \cup(5, \infty)$
$\therefore \quad x \in(-\infty,-2) \cup[6, \infty)$
2. If the system of linear equations
$7 x+11 y+\alpha z=13$
$5 x+4 y+7 z=\beta$
$175 x+194 y+57 z=361$
has infinitely many solutions, then $\alpha+\beta+2$ is equal to
(1) 4
(2) 3
(3) 5
(4) 6

Answer (1)
Sol. $7 x+11 y+\alpha z=13$
$5 x+4 y+7 z=\beta$
$175 x+194 y+57 z=361$
For infinite solution, $\left|\begin{array}{ccc}7 & 11 & \alpha \\ 5 & 4 & 7 \\ 175 & 194 & 57\end{array}\right|=0$
$\Rightarrow\left|\begin{array}{ccc}7 & 11 & \alpha \\ 5 & 4 & 7 \\ 0 & -81 & 57-25 \alpha\end{array}\right|=0$
$\Rightarrow 81(49-5 \alpha)+(57-25 \alpha)(-27)=0$
$\Rightarrow 270 \alpha=-2430 \Rightarrow \alpha=-9$
and $\Delta_{1}=0$
$\left|\begin{array}{ccc}13 & 11 & -9 \\ \beta & 4 & 7 \\ 361 & 194 & 57\end{array}\right|=0$
$\Rightarrow \beta=11$
$\therefore \alpha+\beta+2=4$
3. Let $A=\{1,3,4,6,9\}$ and $B=\{2,4,5,8,10\}$. Let $R$ be a relation defined on $A \times B$ such that $R=\left\{\left(\left(a_{1}\right.\right.\right.$, $\left.\left.b_{1}\right),\left(a_{2}, b_{2}\right)\right): a_{1} \leq b_{2}$ and $\left.b_{1} \leq a_{2}\right\}$. Then the number of elements in the set $R$ is
(1) 160
(2) 52
(3) 26
(4) 180

Answer (1)
Sol. $A=\{1,3,4,6,9\} B=\{2,4,5,8,10\}$
$R=\left\{\left(\left(a_{1}, b_{1}\right),\left(a_{2}, b_{2}\right)\right): a_{1} \leq b_{2}\right.$ and $\left.b_{1} \leq a_{2}\right\}$
For
Similarly for $\left(b_{1}, a_{2}\right)$ we will have
$a_{1}=1 \quad b_{2} \rightarrow 5 \quad b_{1} \rightarrow 2 \quad a_{2}=4$
$a_{1}=3 \quad b_{2} \rightarrow 4 \quad b_{1} \rightarrow 4 \quad a_{2}=3$
$a_{1}=4 \quad b_{2} \rightarrow 4 \quad b_{1} \rightarrow 5 \quad a_{2}=2$
$a_{1}=6 \quad b_{2} \rightarrow 2 \quad b_{1} \rightarrow 8 \quad a_{2}=1$

$a_{1}=9 \quad \begin{aligned} & \frac{b_{2} \rightarrow 1}{16 \text { cases }}\end{aligned} \quad$| $b_{1} \rightarrow 10$ |
| :--- |

$\therefore$ Total elements in relation $=16 \times 10=160$
4. Let the mean of 6 observations $1,2,4,5, x$ and $y$ be 5 and their variance be 10 . Then their mean deviation about the mean is equal to
(1) $\frac{7}{3}$
(2) 3
(3) $\frac{8}{3}$
(4) $\frac{10}{3}$

Answer (3)

Sol. $12+x+y=30$
$\Rightarrow x+y=18$
and $\frac{x^{2}+y^{2}+46}{6}-25=10$
$\therefore \quad x=10, y=8$
Now, mean deviation about mean
$=\frac{4+3+1+0+5+3}{6}=\frac{8}{3}$
5. If four distinct points with position vectors
$\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are coplanar, then $[\vec{a} \vec{b} \vec{c}]$ is equal to
(1) $[\vec{d} \vec{b} \vec{a}]+[\vec{a} \vec{c} \vec{d}]+[\vec{d} \vec{b} \vec{c}]$
(2) $[\vec{a} \vec{d} \vec{b}]+\left[\begin{array}{lll}\vec{d} & \vec{c} & \vec{a}\end{array}\right]+\left[\begin{array}{lll}\vec{d} & \vec{b} & \vec{c}\end{array}\right]$
(3) $[\vec{d} \vec{c} \vec{a}]+\left[\begin{array}{lll}\vec{b} & \vec{d} & \vec{a}\end{array}\right]+\left[\begin{array}{lll}\vec{c} & \vec{d} & \vec{b}\end{array}\right]$
(4) $[\vec{b} \vec{c} \vec{d}]+[\vec{d} \vec{a} \vec{c}]+[\vec{d} \vec{b} \vec{a}]$

## Answer (3)

Sol. $[\vec{b}-\vec{a} \vec{c}-\vec{a} \vec{d}-\vec{a}]=0$

$$
\begin{aligned}
& (\vec{b}-\vec{a}) \cdot[(\vec{c}-\vec{a}) \times(\vec{d}-\vec{a})]=0 \\
& (\vec{b}-\vec{a}) \cdot(\vec{c} \times \vec{d}-\vec{c} \times \vec{a}-\vec{a} \times \vec{d})=0 \\
& {\left[\begin{array}{l}
\vec{b} \\
\vec{c} \\
\vec{d}]
\end{array}\right]-[\vec{b} \vec{c} \vec{a}]-[\vec{b} \vec{a} \vec{d}]-[\vec{a} \vec{c} \vec{d}]=0} \\
& \therefore \quad[\vec{a} \vec{b} \vec{c}]=[\vec{b} \vec{c} \vec{d}]+[\vec{a} \vec{b} \vec{d}]+[\vec{a} \vec{d} \vec{c}] \\
& \quad=[\vec{d} \vec{c} \vec{a}]+[\vec{b} \vec{d} \vec{a}]+[\vec{c} \vec{d} \vec{b}]
\end{aligned}
$$

6. Let $y=y(x)$ be the solution of the differential equation
$\frac{d y}{d x}+\frac{5}{x\left(x^{5}+1\right)} y=\frac{\left(x^{5}+1\right)^{2}}{x^{7}}, x>0$. If $y(1)=2$, then $y(2)$ is equal to
(1) $\frac{637}{128}$
(2) $\frac{679}{128}$
(3) $\frac{693}{128}$
(4) $\frac{697}{128}$

Answer (3)

Sol. I.F. $=e^{\int \frac{5}{x\left(1+x^{5}\right)} d x}$
$=e^{\int \frac{5}{x^{6}\left(\frac{1}{x^{5}}+1\right)} d x}$
Put $\frac{1}{x^{5}}+1=t$
$\frac{-5}{x^{6}} d x=d t$
$e^{\int-\frac{d t}{t}}=e^{-\ln t}=\frac{1}{t}=\frac{x^{5}}{1+x^{5}}$
$y\left(\frac{x^{5}}{1+x^{5}}\right)=\int \frac{x^{5}}{1+x^{5}} \frac{\left(1+x^{5}\right)^{2}}{x^{7}} d x+c$
$y\left(\frac{x^{5}}{1+x^{5}}\right)=\frac{-1}{x}+\frac{x^{4}}{4}+c$
Now $y(1)=2$, then $c=\frac{7}{4}$
$\therefore y(2)=\frac{693}{128}$
7. Let $P$ be the plane passing through the points (5, 3, $0)$, ( $13,3,-2$ ) and ( $1,6,2$ ). For $\alpha \in \mathbb{N}$, if the distances of the points $A(3,4, \alpha)$ and $B(2, \alpha, a)$ from the plane $P$ are 2 and 3 respectively, then the positive value of $a$ is
(1) 6
(2) 3
(3) 5
(4) 4

Answer (4)

Sol.

$\overrightarrow{A B}=8 \hat{i}-2 \hat{k}$
$\overrightarrow{A C}=-4 \hat{i}+3 \hat{j}+2 \hat{k}$
$\overrightarrow{A B} \times \overrightarrow{A C}=\left|\begin{array}{ccc}\hat{i} & \hat{j} & \hat{k} \\ 8 & 0 & -2 \\ -4 & 3 & 2\end{array}\right|$
$=6 \hat{i}-8 \hat{j}+24 \hat{k}$

Equation of plane : $6 x-8 y+24 z=d$ passes through $(5,3,0)$
$6 \times 5-8 \times 3+24 \times 0=d$
$d=6$
$6 x-8 y+24 z=6 \Rightarrow 3 x-4 y+12 z=3$
Distance of point ( $3,4, \alpha$ )
$\frac{9-16+12 \alpha-3}{\sqrt{9+16+144}}=2 \Rightarrow \alpha=3$
Distance of point (2, $\alpha, a)$
$\frac{3 \times 2-4 \times 3+12 \times a-3}{13}=3$
$12 a-9=39$
$12 a=48$
$a=4$
8. The converse of $((\sim p) \wedge q) \Rightarrow r$ is
(1) $((\sim p) \vee q) \Rightarrow r$
(2) $(\sim r) \Rightarrow p \wedge q$
(3) $\quad(\sim r) \Rightarrow((\sim p) \wedge q)$
(4) $(p \vee(\sim q)) \Rightarrow(\sim r)$

## Answer (4)

Sol. Converse of $(\sim p \wedge q) \Rightarrow r$ is

$$
\begin{aligned}
& r \Rightarrow(\sim p \wedge q) \\
& (p \vee(\sim q)) \Rightarrow(\sim r)
\end{aligned}
$$

9. Let the function $f:[0,2] \rightarrow \mathbb{R}$ be defined as

$$
f(x)= \begin{cases}e^{\min \left\{x^{2}, x-[x]\right\}}, & x \in[0,1) \\ e^{\left[x-\log _{e} x\right],} & x \in[1,2]\end{cases}
$$

where $[t]$ denotes the greatest integer less than or equal to $t$. Then the value of the integral $\int_{0}^{2} x f(x) d x$ is
(1) $1+\frac{3 e}{2}$
(2) $(e-1)\left(e^{2}+\frac{1}{2}\right)$
(3) $2 e-1$
(4) $2 e-\frac{1}{2}$

## Answer (4)

Sol. $f(x)=\left\{\begin{array}{cc}e^{\min \left\{x^{2}, x\right\}} & x \in[0,1) \\ e & x \in[1,2]\end{array}\right.$
$=\left\{\begin{array}{cc}e^{x^{2}} & x \in[0,1) \\ e & x \in[1,2]\end{array}\right.$
$\because \quad x-\ln x \in[1,2)$ for $x \in[1,2]$
$\therefore \quad[x-\ln x]=1$
$\int_{0}^{2} x f(x)=\int_{0}^{1} x \cdot e^{x^{2}} d x+\int_{1}^{2} x \cdot e d x$
$x^{2}=t \Rightarrow 2 x d x=d t$
$=\frac{1}{2} \int_{0}^{1} e^{t} d t+\left.e \frac{x^{2}}{2}\right|_{1} ^{2}$
$\Rightarrow\left(\frac{e-1}{2}\right)+\frac{3 e}{2} \Rightarrow 2 e-\frac{1}{2}$
Option (4) is correct.
10. If $f: \mathbb{R} \rightarrow \mathbb{R}$ be a continuous function satisfying $\int_{0}^{\frac{\pi}{2}} f(\sin 2 x) \sin x d x+\alpha \int_{0}^{\frac{\pi}{4}} f(\cos 2 x) \cos x d x=0$, then the value of $\alpha$ is
(1) $\sqrt{2}$
(2) $-\sqrt{3}$
(3) $\sqrt{3}$
(4) $-\sqrt{2}$

## Answer (4)

Sol. $\int_{0}^{\frac{\pi}{2}} f(\sin 2 x) \sin x d x+\alpha \int_{0}^{\frac{\pi}{4}} f(\cos 2 x) \cdot \cos x d x=0$
Let $I=\int_{0}^{\frac{\pi}{2}} f(\sin 2 x) \cdot \sin x d x$
$=\int_{0}^{\frac{\pi}{4}} f(\sin 2 x) \sin x d x+\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} f(\sin 2 x) \cdot \sin x d x$

$$
=\int_{0}^{\frac{\pi}{4}} f(\cos 2 x) \sin \left(\frac{\pi}{4}-x\right) d x
$$

$$
+\int_{0}^{\frac{\pi}{4}} f\left(\sin 2\left(\frac{\pi}{4}+x\right)\right) \sin \left(\frac{\pi}{4}+x\right) d x
$$

$$
=\int_{0}^{\frac{\pi}{4}} f(\cos 2 x)\left(\frac{1}{\sqrt{2}} \cos x-\frac{1}{\sqrt{2}} \sin x\right) d x
$$

$$
+\int_{0}^{\frac{\pi}{4}} f(\cos 2 x)\left(\frac{1}{\sqrt{2}} \cos x+\frac{1}{\sqrt{2}} \sin x\right) d x
$$

$$
\begin{aligned}
& =\int_{0}^{\frac{\pi}{4}} f(\cos 2 x)(\sqrt{2} \cos x) d x \\
& \therefore \alpha=-\sqrt{2}
\end{aligned}
$$

Option (4) is correct.
11. If the radius of the largest circle with centre $(2,0)$ inscribed in the ellipse $x^{2}+4 y^{2}=36$ is $r$, then $12 r^{2}$ is equal to
(1) 115
(2) 92
(3) 69
(4) 72

Answer (2)
Sol. Equation of normal at $P(6 \cos \theta, 3 \sin \theta)$ is
$6 \sec \theta x-3 \operatorname{cosec} \theta y=27$
If passes through ( 2,0 )
$\therefore \quad 12 \sec \theta=27$
$\therefore \quad \cos \theta=\frac{4}{9}, \sin \theta=\frac{\sqrt{65}}{9}$

$$
P\left(\frac{8}{3}, \frac{\sqrt{65}}{3}\right)
$$

$$
\begin{aligned}
r & =O P \quad(O=(2,0)) \\
& =\sqrt{\left(\frac{8}{3}-2\right)^{2}+\left(\frac{\sqrt{65}}{3}\right)^{2}} \\
& =\frac{\sqrt{69}}{3}
\end{aligned}
$$

$\therefore \quad 12 r^{2}=12 \times \frac{69}{9}=92$
$\therefore$ Option (2) is correct.
12. Let the line passing through the points $P(2,-1,2)$ and $Q(5,3,4)$ meet the plane $x-y+z=4$ at the point $R$. Then the distance of the point $R$ from the plane $x+2 y+3 z+2=0$ measured parallel to the line $\frac{x-7}{2}=\frac{y+3}{2}=\frac{z-2}{1}$ is
(1) $\sqrt{61}$
(2) $\sqrt{189}$
(3) $\sqrt{31}$
(4) 3

## Answer (4)

Sol. Equation of line $P Q$.
$\frac{x-2}{3}=\frac{y+1}{4}=\frac{z-2}{2}=\lambda$
Let $R$ be $(3 \lambda+2,4 \lambda-1,2 \lambda+2)$
$R$ lies on plane $x-y+z=4$
$\therefore \quad 3 \lambda+2-4 \lambda+1+2 \lambda+2=4$
$\Rightarrow \lambda=-1$
$\therefore \quad R(-1,-5,0)$
Let $S R$ be : $\frac{x+1}{2}=\frac{y+5}{2}=\frac{z}{1}=k$

$S:(2 k-1,2 k-5, k)$
Slies on plane : $x+2 y+3 z+2=0$
$\Rightarrow(2 k-1)+(4 k-10)+3 k+2=0$
$\Rightarrow 9 k-9=0 \Rightarrow k=1$

$$
S(1,-3,1) \quad \therefore S R=\sqrt{4+4+1}=3
$$

$\therefore$ Option (4) is correct.
13. If $\left|\begin{array}{ccc}x+1 & x & x \\ x & x+\lambda & x \\ x & x & x+\lambda^{2}\end{array}\right|=\frac{9}{8}(103 x+81)$, then $\lambda, \frac{\lambda}{3}$ are the roots of the equation
(1) $4 x^{2}+24 x-27=0$
(2) $4 x^{2}-24 x-27=0$
(3) $4 x^{2}+24 x+27=0$
(4) $4 x^{2}-24 x+27=0$

Answer (4)
Sol. $\left|\begin{array}{ccc}x+1 & x & x \\ x & x+\lambda & x \\ x & x & x+\lambda^{2}\end{array}\right|=\frac{9}{8}(103 x+81)$
Put $x=0$
$\left|\begin{array}{ccc}1 & 0 & 0 \\ 0 & \lambda & 0 \\ 0 & 0 & \lambda^{2}\end{array}\right|=\frac{9}{8} \times 81$
$\lambda^{3}=\frac{3^{6}}{2^{3}}$
$\lambda=\frac{9}{2}$
$\frac{\lambda}{3}=\frac{3}{2}$
Equation : $x^{2}-\left(\frac{9}{2}+\frac{3}{2}\right) x+\frac{9}{2} \times \frac{3}{2}=0$
$4 x^{2}-24 x+27=0$
14. If the letters of the word MATHS are permuted and all possible words so formed are arranged as in a dictionary with serial numbers, then the serial number of the word THAMS is
(1) 103
(2) 102
(3) 101
(4) 104

## Answer (1)

Sol. $\begin{array}{llllll}5 & 2 & 1 & 3 & 4 \\ 7 & H & A & M & S \\ 4 & 1 & 0 & 0 & 0\end{array}$
$\begin{array}{ccccc}4 & 1 & 0 & 0 & 0 \\ 4! & 3! & 2! & 1! & 0!\end{array}$
Rank $=4 \times 4!+1 \times 3!+1$

$$
\begin{aligned}
& =96+6+1 \\
& =103
\end{aligned}
$$

15. Let $f$ and $g$ be two functions defined by
$f(x)=\left\{\begin{array}{cc}x+1, & x<0 \\ |x-1|, & x \geq 0\end{array}\right.$ and $g(x)=\left\{\begin{array}{cc}x+1, & x<0 \\ 1, & x \geq 0\end{array}\right.$
Then $(g \circ f)(x)$ is
(1) Continuous everywhere but not differentiable exactly at one point
(2) Continuous everywhere but not differentiable at $x=1$
(3) Differentiable everywhere
(4) Not continuous at $x=-1$

Answer (1)
Sol. $f x=\left\{\begin{array}{cc}x+1 & x<0 \\ 1-x & 0 \leq x<1 \\ x-1 & x>1\end{array} \quad g \quad x=\left\{\begin{array}{cc}1+x & x<0 \\ 1 & x \geq 0\end{array}\right.\right.$
For $\operatorname{gof}(x)$

$$
\text { gof } x=\left\{\begin{array}{cl}
x+2 & x<-1 \\
1 & x \geq-1
\end{array}\right.
$$


$\therefore \quad$ Continuous but not differentiable at $x=-1$
16. Let $a, b, c$ and $d$ be positive real numbers such that $a+b+c+d=11$. If the maximum value of $a^{5} b^{3} c^{2} d$ is $3750 \beta$, then the value of $\beta$ is
(1) 90
(2) 110
(3) 55
(4) 108

Answer (1)
Sol. $a+b+c+d=11$
$\left.a^{5} b^{3} c^{2} d\right|_{\min }=3750 \beta$
Assume numbers be $\frac{a}{5}, \frac{a}{5}, \frac{a}{5}, \frac{a}{5}, \frac{a}{5}, \frac{b}{3}, \frac{b}{3}, \frac{b}{3}, \frac{c}{2}, \frac{c}{2}, a$
Apply $\mathrm{AM} \geq \mathrm{GM}$
$\frac{\frac{a}{5}+\frac{a}{5}+\frac{a}{5}+\frac{a}{5}+\frac{a}{5}+\frac{b}{3}+\frac{b}{3}+\frac{b}{3}+\frac{c}{2}+\frac{c}{2}+d}{11}$

$$
\geq\left(\frac{\left(a^{5} b^{3} c^{2} d\right)}{5^{5} 3^{3} 2^{2} 1}\right)^{\frac{1}{11}}
$$

$\therefore a^{5} b^{3} c^{2} d \leq 90 \times 3750$
$\therefore \beta=90$
17. For $a \in \mathbb{C}$, let $A=\{z \in \mathbb{C}: \operatorname{Re}(a+\bar{z})>\operatorname{Im}(\bar{a}+z)\}$ and $B=\{z \in \mathbb{C}: \operatorname{Re}(a+\bar{z})<\operatorname{Im}(\bar{a}+z)\}$. Then among the two statements:
(S1): If $\operatorname{Re}(a), \operatorname{Im}(a)>0$, then the set $A$ contains all the real numbers
(S2) : If $\operatorname{Re}(a), \operatorname{Im}(a)<0$, then the set $B$ contains all the real numbers,
(1) Only (S2) is true
(2) Only (S1) is true
(3) Both are true
(4) Both are false

## Answer (4)

Sol. Let $a=x_{1}+i y_{1}, \quad \bar{a}=x_{1}-i y_{1}$

$$
\begin{aligned}
& \quad z=x_{2}+i y_{2}, \quad \bar{z}=x_{2}-i y_{2} \\
& A= \\
& \left.A z: x_{1}+x_{2}>y_{2}-y_{1}\right\}=\left\{z: x_{1}+y_{1}+x_{2}>y_{2}\right\} \\
& B= \\
& \text { If } \left.y_{2}=0 \text { and } x_{1}, y_{1}+x_{2}>y_{2}-y_{1}\right\}=\left\{z: x_{1}+y_{1}+x_{2}<y_{2}\right\}
\end{aligned}
$$

$$
A=\left\{z: x_{2}>-\left(x_{1}+y_{1}\right)\right\}
$$

$A$ covers a part of negative real axis and therefore, does not contain whole real axis
Similarly if $y_{2}=0$, and $x_{1}, y_{1}<0$, then
$B=\left\{z: x_{2}<-\left(x_{1}+y_{1}\right)\right\}$
$\therefore B$ covers part of positive real axis and therefore does not cover whole real axis.
18. If the $1011^{\text {th }}$ term from the end in the binomial expansion of $\left(\frac{4 x}{5}-\frac{5}{2 x}\right)^{2022}$ is 1024 times $1011^{\text {th }}$ term from the beginning, then $|x|$ is equal to
(1) 15
(2) 10
(3) 12
(4) 8

Answer (*)
Sol. $1011^{\text {th }}$ term from end $=a_{1013}=1013^{\text {th }}$ term from beginning
$\frac{a_{1013}}{a_{1011}}=1024$
$\frac{{ }^{2022} C_{1012}\left(\frac{4 x}{5}\right)^{1010} \cdot\left(\frac{-5}{2 x}\right)^{1012}}{{ }^{2022} C_{1010}\left(\frac{4 x}{5}\right)^{1012}\left(\frac{-5}{2 x}\right)^{1010}}=1024$
$\frac{\left(\frac{-5}{2 x}\right)^{2}}{\left(\frac{4 x}{5}\right)^{2}}=1024$
$\frac{5^{4}}{2^{6} x^{4}}=2^{10}$
$\left(\frac{5}{x}\right)^{4}=2^{16}$
$|x|=\frac{5}{16}$
Note : If the binomial expansion of $(x+a)^{n}$ is written in increasing power of $x$ (and decreasing power of a), then answer matches to one of the option.
19. The sum of the coefficients of three consecutive terms in the binomial expansion of $(1+x)^{n+2}$, which are in the ratio $1: 3: 5$, is equal to
(1) 92
(2) 63
(3) 41
(4) 25

Answer (2)

Sol. Let the three terms be $T_{r}, T_{r+1}, T_{r+2}$
$\frac{T_{r+1}}{T_{r}}=\frac{{ }^{n+2} C_{r}}{{ }^{n+2} C_{r-1}}=\frac{n+2-r+1}{r}=\frac{n+3-r}{r}=3$
$n-4 r+3=0$
$\frac{T_{r+2}}{T_{r+1}}=\frac{{ }^{n+2} C_{r+1}}{{ }^{n+2} C_{r}}=\frac{(n+2)-(r+1)+1}{r+1}=\frac{n-r+2}{r+1}=\frac{5}{3}$
$3 n-8 r+1=0$
(1) and (2) $\Rightarrow n=5, r=2$

$$
\begin{aligned}
T_{r}+T_{r+1}+T_{r+2} & ={ }^{7} C_{1}+{ }^{7} C_{2}+{ }^{7} C_{3} \\
& =7+21+35=63
\end{aligned}
$$

20. The angle of elevation of the top $P$ of a tower from the feet of one person standing due south of the tower is $45^{\circ}$ and from the feet of another person standing due west of the tower is $30^{\circ}$. If the height of the tower is 5 meters, then the distance (in meters) between the two persons is equal to
(1) $\frac{5}{2} \sqrt{5}$
(2) 10
(3) 5
(4) $5 \sqrt{5}$

Answer (2)
Sol.

$\tan 45^{\circ}=\frac{5}{x_{1}}, \tan 30^{\circ}=\frac{5}{x_{2}}$
$x_{1}=5, x_{2}=5 \sqrt{3}, A B=10$

## SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10 . The answer to each question is a NUMERICAL VALUE. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, $-00.33,-00.30,30.27,-27.30$ ) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
21. The number of points, where the curve $f(x)=e^{8 x}-e^{6 x}-3 e^{4 x}-e^{2 x}+1, x \in \mathbb{R}$ cuts $\quad x$ axis, is equal to $\qquad$

## Answer (2)

Sol. $f(x)=e^{8 x}-e^{6 x}-3 e^{4 x}-e^{2 x}+1, x \in \mathbb{R}$

$$
\lim _{x \rightarrow-\infty} f(x)=1, \quad f(0)=-3, \quad \lim _{x \rightarrow \infty} f(x) \rightarrow \infty
$$

One root of $f(x)=0$ is negative and other root of
$f(x)=0$ is positive
Curve $y=f(x)$ cuts $x$-axis at two points
22. Let $S=\left\{z \in \mathbb{C}-\{i, 2 i\}: \frac{z^{2}+8 i z-15}{z^{2}-3 i z-2} \in \mathbb{R}\right\}$. If $\alpha-\frac{13}{11} i \in S, \alpha \in \mathbb{R}-\{0\}$, then $242 \alpha^{2}$ is equal to

## Answer (1680)

Sol. Put $z=x+i y$

$$
\begin{aligned}
& \quad \operatorname{lm}\left(\frac{z^{2}+8 i z-15}{z^{2}-3 i z-2}\right)=0 \\
& \quad \Rightarrow-\left(x^{2}-y^{2}-8 y-15\right)(2 x y-3 x)+(2 x y+8 x)\left(x^{2}-\right. \\
& \left.y^{2}+3 y-2\right)=0 \\
& \quad \Rightarrow\left(x^{2}-y^{2}\right)(2 x y+8 x-2 x y+3 x)+(8 y+15)(2 x y- \\
& 3 x)+(2 x y+8 x)(3 y-2)=0 \\
& \quad \Rightarrow 11 x^{3}-11 x y^{2}+16 x y^{2}-24 x y+30 x y-45 x+6 x y^{2} \\
& -4 x y+24 x y-16 x=0 \\
& \quad \Rightarrow 11 x^{3}+11 x y^{2}+26 x y-61 x=0 \\
& \quad \Rightarrow\left(11 x^{2}+11 y^{2}+26 y-61=0\right. \\
& \quad \because \alpha \neq 0, \Rightarrow x=0 \text { (neglected) }
\end{aligned}
$$

Put $y=-\frac{13}{11}, \quad x=\alpha$
$11 \alpha^{2}+11 \cdot \frac{13^{2}}{11^{2}}-26 \cdot \frac{13}{11}-61=0$
$\Rightarrow 121 \alpha^{2}=840$
$\Rightarrow 242 \alpha^{2}=1680$
23. Let the probability of getting head for a biased coin be $\frac{1}{4}$. It is tossed repeatedly until a head appears. Let $N$ be the number of tosses required. If the probability that the equation $64 x^{2}+5 N x+1=0$ has no real root is $\frac{p}{q}$, where $p$ and $q$ are co-prime, then $q-p$ is equal to $\qquad$ .

## Answer (27)

Sol. $64 x^{2}+5 N x+1=0$ has no real root
$\Rightarrow 25 N^{2}-4 \times 64<0$
$\Rightarrow \quad N<\frac{16}{5} \Rightarrow N=1,2,3$
$\Rightarrow \quad \frac{1}{4}+\frac{3}{4} \times \frac{1}{4}+\frac{3}{4} \cdot \frac{3}{4} \cdot \frac{1}{4}=\frac{p}{q}$
$\Rightarrow \frac{p}{q}=\frac{37}{64} \Rightarrow q-p=64-37=27$
24. If $A$ is the area in the first quadrant enclosed by the curve $C: 2 x^{2}-y+1=0$, the tangent to $C$ at the point $(1,3)$ and the line $x+y=1$, then the value of $60 A$ is $\qquad$ _.

## Answer (16.00)

Sol. $y=2 x^{2}+1$
Tangent : $y-3=4(x-1)$
$y=4 x-1$


Required area
$=\frac{1}{2} \times \frac{1}{2} \times \frac{2}{5}+\int_{1}^{3}\left(\frac{y+1}{4}-\left(\frac{y-1}{2}\right)^{\frac{1}{2}}\right) d y$
$=\frac{4}{15}$
$60 A=16$
25. Let the tangent to the parabola $y^{2}=12 x$ at the point
$(3, \alpha)$ be perpendicular to the line $2 x+2 y=3$. Then the square of distance of the point $(6,-4)$ from the normal to the hyperbola $\alpha^{2} x^{2}-9 y^{2}=9 \alpha^{2}$ at its point $(\alpha-1, \alpha+2)$ is equal to $\qquad$ .

## Answer (116.00)

Sol. Slope of tangent $=1=\frac{6}{\alpha} \Rightarrow \alpha=6$
$36 x^{2}-9 y^{2}=324$
$\frac{x^{2}}{9}-\frac{y^{2}}{36}=1$
Tangent at $(5,8)$
$\frac{5 x}{9}-\frac{8 y}{36}=1$
$5 x-2 y=9$
Slope of normal $=\frac{-2}{5}$
Equation of normal
$y-8=\frac{-2}{5}(x-5)$
$5 y-40=-2 x+10$
$5 y+2 x=50$
Distance from (6, -4)
$=\left|\frac{12-20-50}{\sqrt{29}}\right|=\frac{58}{\sqrt{29}}$
$=2 \sqrt{29}$
26. Let $\vec{a}=\hat{i}+2 \hat{j}+3 \hat{k}$ and $\vec{b}=\hat{i}+\hat{j}-\hat{k}$. If $\vec{c}$ is a vector such that $\vec{a} \cdot \vec{c}=11, \vec{b} \cdot(\vec{a} \times \vec{c})=27$ and $\vec{b} \cdot \vec{c}=$ $-\sqrt{3}|\vec{b}|$, then $|\vec{a} \times \vec{c}|^{2}$ is equal to $\qquad$ .

## Answer (285)

Sol. $\vec{a}=\hat{i}+2 \hat{j}+3 \hat{k}$
$\vec{b}=\hat{i}+\hat{j}-\hat{k}$
$\vec{a} \cdot \vec{c}=11$
$\vec{b} \cdot(\vec{a} \times \vec{c})=27$
$\vec{b} \cdot \vec{c}=-\sqrt{3}|\vec{b}|$
$(\vec{b} \times \vec{a}) \cdot \vec{c}=27$

Let $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$
$c_{1}+2 c_{2}+3 c_{3}=11$
$c_{1}+c_{2}-c_{3}=-\sqrt{3} \sqrt{3}$
$c_{1}+c_{2}-c_{3}=-3$
$5 c_{1}-4 c_{2}+c_{3}=27$
From (i), (ii) \& (iii)
$\vec{c}=3 \hat{i}-2 \hat{j}+4 \hat{k}$
$|\vec{a} \times \vec{c}|^{2}=\left|\begin{array}{ccc}\hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ 3 & -2 & +4\end{array}\right|^{2}$
$=|14 \hat{i}+5 \hat{j}-8 \hat{k}|^{2}$
$=14^{2}+5^{2}+8^{2}=285$
27. Let $A=\{1,2,3,4,5\}$ and $B=\{1,2,3,4,5,6\}$. Then the number of functions $f: A \rightarrow B$ satisfying $f(1)+$ $f(2)=f(4)-1$ is equal to

## Answer (360.00)

Sol. $f(1)+f(2)+1=f(4)$
$\Rightarrow f(1)+f(2) \leq 5$
Let $f(4)=6$, then $f(1)+f(2)=5$
So ( $f_{1}, f_{2}$ ) may be ( 1,4 ), (4, 1), (2, 3), (3, 2)
Total ways $=4 \cdot 1 \cdot 6 \cdot 6=144$
Let $f(4)=5, \quad f(1)+f(2)=4$
so ( $f_{1}, f_{2}$ ) may be $(1,3),(3,1),(2,2)$
Total ways $=3 \cdot 1 \cdot 6 \cdot 6=108$
Let $f(4)=4, \quad f(1)+f(2)=3$
so $\left(f_{1}, f_{2}\right)$ may be $(1,2),(2,1)$
Total ways $=2 \cdot 1 \cdot 6 \cdot 6=72$
Let $f(4)=3, \quad f(1)+f(2)=2$
Only way $(1,1)$
Total ways $=1 \cdot 1 \cdot 36=36$
28. For $k \in \mathbb{N}$, if the sum of the series $1+\frac{4}{k}+\frac{8}{k^{2}}+\frac{13}{k^{3}}+\frac{19}{k^{4}}+\ldots$ is 10 , then the value of $k$ is
$\qquad$ .

## Answer (2)

Sol. $S=1+\frac{4}{k}+\frac{8}{k^{2}}+\frac{13}{k^{3}}+\frac{19}{k^{4}}+\ldots \ldots$.
$\frac{1}{k} S=\frac{1}{k}+\frac{4}{k^{2}}+\frac{8}{k^{3}}+\ldots$.
(i) - (ii) $\Rightarrow\left(1-\frac{1}{k}\right) S=1+\frac{3}{k}+\frac{4}{k^{2}}+\frac{5}{k^{3}}+$

Let $S^{\prime}=\frac{3}{k}+\frac{4}{k^{2}}+\frac{5}{k^{3}}+\ldots . . \infty$

$$
\frac{S^{\prime}}{k}=\frac{3}{k^{2}}+\frac{4}{k^{3}}+\ldots \ldots \infty
$$

(iv) $-(v) \Rightarrow\left(1-\frac{1}{k}\right) S^{\prime}=\frac{3}{k}+\frac{1}{k^{2}}+\frac{1}{k^{3}}+\frac{1}{k^{4}}+\ldots . \infty$

$$
\begin{equation*}
=\frac{3}{k}+\frac{\frac{1}{k^{2}}}{1-\frac{1}{k}} \tag{vi}
\end{equation*}
$$

$\Rightarrow S^{\prime}=\frac{3}{k-1}+\frac{1}{(k-1)^{2}}$
From (iii) and (vi)
$\frac{k-1}{k} S=1+\frac{3}{k-1}+\frac{1}{(k-1)^{2}}$
$S=10 \Rightarrow 9 k^{3}-31 k^{2}+31 k-10=0$
$\Rightarrow k=2$
29. Let the line $1: x=\frac{1-y}{-2}=\frac{z-3}{\lambda}, \lambda \in \mathbb{R}$ meet the plane $P: x+2 y+3 z=4$ at the point $(\alpha, \beta, \gamma)$. If the angle between the line $I$ and the plane $P$ is $\cos ^{-1}\left(\sqrt{\frac{5}{14}}\right)$, then $\alpha+2 \beta+6 \gamma$ is equal to $\qquad$

## Answer (11)

Sol. $L: \frac{x-0}{1}=\frac{y-1}{2}=\frac{z-3}{\lambda} \& P: x+2 y+3 z=4$
Vector parallel to line : <1, 2, $\lambda>=\bar{b}$
Normal vector to plane $P:<1,2,3>=\bar{n}$

Angle between plane \& line is $\theta$
Then, $\sin \theta=\frac{\langle 1,2, \lambda\rangle \cdot\langle 1,2,3\rangle}{\sqrt{1^{2}+2^{2}+\lambda^{2}} \cdot \sqrt{1^{2}+2^{2}+3^{2}}}$
$\Rightarrow \frac{3}{\sqrt{14}}=\frac{1+4+3 \lambda}{\sqrt{\lambda^{2}+5} \sqrt{14}} \Rightarrow \lambda=\frac{2}{3}$
$L_{1} \equiv \frac{x-0}{3}=\frac{y-1}{6}=\frac{z-3}{2}=\mu$
Any point on line : $(3 \mu, 6 \mu+1,2 \mu+3)$
It lies on $P \Rightarrow 3 \mu+12 \mu+2+6 \mu+9=4$

$$
\Rightarrow \quad \mu=\frac{-1}{3}
$$

Hence, $\alpha=3 \mu=-1, \beta=6 \mu+1=-1, \gamma=2 \mu+3=\frac{7}{3}$
Now, $\alpha+2 \beta+6 \gamma=11$
30. If the line $l_{1}: 3 y-2 x=3$ is the angular bisector of the lines $I_{2}: x-y+1=0$ and $I_{3}: \alpha x+\beta y+17=0$, then $\alpha^{2}+\beta^{2}-\alpha-\beta$ is equal to $\qquad$ .

## Answer (348)

Sol. $L_{1}: 3 y-2 x=3$
$L_{2}: x-y+1=0$
$L_{3}: \alpha x+\beta y+17=0$
Point of intersection of $L_{1} \& L_{2}$ is $(0,1)$, should lie on $L_{3} \Rightarrow \beta=-17$

Any point, say $\left(\frac{-3}{2}, 0\right)$ on $L_{1}$ should be equidistant from the lines $L_{2} \& L_{3}$

$$
\begin{aligned}
& \Rightarrow\left|\frac{\frac{-3}{2}-0+1}{\sqrt{1^{2}+1^{2}}}\right|=\left|\frac{\frac{-3 \alpha}{2}+0+17}{\sqrt{\alpha^{2}+(-17)^{2}}}\right| \\
& \Rightarrow \quad(\alpha-7)(\alpha-17)=0
\end{aligned}
$$

For $\alpha=17, L_{2} \& L_{3}$ coincides $\Rightarrow \alpha=7$
$\alpha^{2}+\beta^{2}-\alpha-\beta=(-17)^{2}+7^{2}-7+17$
$=348$

## PHYSICS

## SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

## Choose the correct answer:

31. A car $P$ travelling at $20 \mathrm{~ms}^{-1}$ sounds its horn at a frequency of 400 Hz . Another car Q is travelling behind the first car in the same direction with a velocity $40 \mathrm{~ms}^{-1}$. The frequency heard by the passenger of the car $Q$ is approximately [Take, velocity of sound $=360 \mathrm{~ms}^{-1}$ ]
(1) 421 Hz
(2) 471 Hz
(3) 485 Hz
(4) 514 Hz

Answer (2)
Sol.


$$
\begin{aligned}
f & =f_{0}\left(\frac{C+40}{C-20}\right) \\
& =400\left(\frac{360+40}{340}\right) \\
& \approx 471 \mathrm{~Hz}
\end{aligned}
$$

32. A capacitor of capacitance $C$ is charged to a potential V. The flux of the electric field through a closed surface enclosing the positive plate of the capacitor is:
(1) $\frac{C V}{\varepsilon_{0}}$
(2) Zero
(3) $\frac{2 \mathrm{CV}}{\varepsilon_{0}}$
(4) $\frac{\mathrm{CV}}{2 \varepsilon_{0}}$

Answer (1)

Sol.


$$
\phi=\frac{q_{\text {inc }}}{\varepsilon_{0}}=\left(\frac{C V}{\varepsilon_{0}}\right)
$$

33. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason $\mathbf{R}$
Assertion A: A bar magnet dropped through a metallic cylindrical pipe takes more time to come down compared to a non-magnetic bar with same geometry and mass.
Reason R: For the magnetic bar, Eddy currents are produced in the metallic pipe which oppose the motion of the magnetic bar.
In the light of the above statements, choose the correct answer from the options given below
(1) $\mathbf{A}$ is false but $\mathbf{R}$ is true
(2) Both $\mathbf{A}$ and $\mathbf{R}$ are true and $\mathbf{R}$ is the correct explanation of $\mathbf{A}$
(3) $\mathbf{A}$ is true but $\mathbf{R}$ is false
(4) Both $\mathbf{A}$ and $\mathbf{R}$ are true but $\mathbf{R}$ is NOT the correct explanation of $\mathbf{A}$
Answer (2)
Sol. Due to change in flux, eddy current is produced which opposes the motion.
34. When one light ray is reflected from a plane mirror with $30^{\circ}$ angle of reflection, the angle of deviation of the ray after reflection is:
(1) $120^{\circ}$
(2) $110^{\circ}$
(3) $140^{\circ}$
(4) $130^{\circ}$

Answer (1)
Sol. As $i=30^{\circ}$

$$
\begin{aligned}
\delta & =180^{\circ}-2 i \\
& =180^{\circ}-60^{\circ} \\
& =120^{\circ}
\end{aligned}
$$

35. The logic operations performed by the given digital circuit is equivalent to:

(1) NOR
(2) AND
(3) OR
(4) NAND

Answer (2)
Sol. $(A+B) \cdot(A \cdot B)=A \cdot(A B)+B \cdot(A B)$

$$
\begin{aligned}
& =A B+A B \\
& =(A B)
\end{aligned}
$$

36. If V is the gravitational potential due to sphere of uniform density on it's surface, then it's value at the centre of sphere will be:
(1) $\frac{4}{3} \mathrm{~V}$
(2) $\frac{V}{2}$
(3) V
(4) $\frac{3 V}{2}$

## Answer (4)

Sol. $V=\frac{G M}{R}$

$$
V_{\text {centre }}=-\frac{3}{2}\left(\frac{G M}{R}\right)=\left(\frac{3}{2} V\right)
$$

37. In satellite communication, the uplink frequency band used is:
(1) $420-890 \mathrm{MHz}$
(2) $5.925-6.425 \mathrm{GHz}$
(3) $76-88 \mathrm{MHz}$
(4) $3.7-4.2 \mathrm{GHz}$

Answer (2)
Sol. Uplink frequency band for satellite communication is $5.925-6.425 \mathrm{GHz}$.
38. When vector $\vec{A}=2 \hat{i}+3 \hat{j}+2 \hat{k}$ is subtracted from vector $\vec{B}$, it gives a vector equal to $2 \hat{j}$. Then the magnitude of vector $\vec{B}$ will be:
(1) $\sqrt{5}$
(2) 3
(3) $\sqrt{6}$
(4) $\sqrt{13}$

## Answer (*)

Sol. $\vec{B}-(2 \hat{i}+3 \hat{j}+2 \hat{k})=2 \hat{j}$
$\vec{B}=2 \hat{i}+5 \hat{j}+2 \hat{k}$
$|\vec{B}|=\sqrt{4+25+4}=\sqrt{33}$
39. A projectile is projected at $30^{\circ}$ from horizontal with initial velocity $40 \mathrm{~ms}^{-1}$. The velocity of the projectile at $t=2 \mathrm{~s}$ from the start will be:
(Given $g=10 \mathrm{~m} / \mathrm{s}^{2}$ )
(1) $40 \sqrt{3} \mathrm{~ms}^{-1}$
(2) Zero
(3) $20 \mathrm{~ms}^{-1}$
(4) $20 \sqrt{3} \mathrm{~ms}^{-1}$

Answer (4)
Sol. $V_{H}=40 \cos 30^{\circ}=20 \sqrt{3}$
$V_{v}=20-10 \times 2=0 \mathrm{~m} / \mathrm{s}$
$V=V_{H}=20 \sqrt{3} \mathrm{~m} / \mathrm{s}$
40. A body of mass 500 g moves along x -axis such that it's velocity varies with displacement $x$ according to the relation $v=10 \sqrt{x} \mathrm{~m} / \mathrm{s}$ the force acting on the body is:
(1) 125 N
(2) 25 N
(3) 166 N
(4) 5 N

Answer (2)
Sol. $v=10 \sqrt{x}$
$\frac{d v}{d x}=\frac{10}{2 \sqrt{x}}=\frac{5}{\sqrt{x}}$
$v \frac{d v}{d x}=a=10 \sqrt{x} \times \frac{5}{\sqrt{x}}=50 \mathrm{~m} / \mathrm{s}^{2}$
$F=\frac{1}{2} \times 50=25 \mathrm{~N}$
41. A plane electromagnetic wave of frequency 20 MHz propagates in free space along x-direction. At a particular space and time $\vec{E}=6.6 \hat{j} \mathrm{v} / \mathrm{m}$. What is $\vec{B}$ at this point?
(1) $2.2 \times 10^{-8} \hat{k} T$
(2) $-2.2 \times 10^{-8} \hat{i} T$
(3) $-2.2 \times 10^{-8} \hat{k} T$
(4) $2.2 \times 10^{-8} \hat{i} T$

Answer (1)
Sol. $\vec{E}=6.6 \hat{j}(\mathrm{~V} / \mathrm{m})$
$\vec{E} \times \vec{B}=\vec{C}$

$\vec{B}=B_{0}(\hat{k})$
$C B_{0}=E$
$B_{0}=\left(\frac{E}{C}\right)=\frac{6.6}{3 \times 10^{8}}=2.2 \times 10^{-8} \mathrm{~T}$
42. The root mean square speed of molecules of nitrogen gas at $27^{\circ} \mathrm{C}$ is approximately: (Given mass of a nitrogen molecule $=4.6 \times 10^{-26} \mathrm{~kg}$ and take Boltzmann constant $\mathrm{k}_{\mathrm{B}}=1.4 \times 10^{-23} \mathrm{JK}^{-1}$ )
(1) $27.4 \mathrm{~m} / \mathrm{s}$
(2) $91 \mathrm{~m} / \mathrm{s}$
(3) $1260 \mathrm{~m} / \mathrm{s}$
(4) $523 \mathrm{~m} / \mathrm{s}$

## Answer (4)

Sol. $V_{\mathrm{rms}}=\sqrt{\frac{3 R T}{M}}=\sqrt{\frac{3 K T}{m}}=\sqrt{\frac{3 \times 1.4 \times 10^{-23} \times 300}{4.6 \times 10^{-26}}}$
$\approx 523 \mathrm{~m} / \mathrm{s}$
43. Eight equal drops of water are falling through air with a steady speed of $10 \mathrm{~cm} / \mathrm{s}$. If the drops coalesce, the new velocity is:-
(1) $16 \mathrm{~cm} / \mathrm{s}$
(2) $40 \mathrm{~cm} / \mathrm{s}$
(3) $5 \mathrm{~cm} / \mathrm{s}$
(4) $10 \mathrm{~cm} / \mathrm{s}$

Answer (2)
Sol. $V_{T} \propto r^{2}$
as, $8 r_{1}^{3}=r_{2}^{3}$
$\frac{\left(V_{T}\right)_{1}}{\left(V_{T}\right)_{2}}=\left(\frac{r_{1}}{r_{2}}\right)^{2}$
$\Rightarrow \frac{r_{1}}{r_{2}}=\left(\frac{1}{2}\right)$
$\frac{10}{V_{T}}=\frac{1}{4}$
$\Rightarrow \quad V_{T}=40 \mathrm{~cm} / \mathrm{s}$
44. An electron is allowed to move with constant velocity along the axis of current carrying straight solenoid.
(A) The electron will experience magnetic force along the axis of the solenoid.
(B) The electron will not experience magnetic force.
(C) The electron will continue to move along the axis of the solenoid.
(D) The electron will be accelerated along the axis of the solenoid.
(E) The electron will follow parabolic path-inside the solenoid.

Choose the correct answer from the option given below:
(1) B, C and D only
(2) A and D only
(3) B and C only
(4) B and E only

Answer (3)
Sol.

$\vec{F}=0$
45. A space ship of mass $2 \times 10^{4} \mathrm{~kg}$ is launched into a circular orbit close to the earth surface. The additional velocity to be imparted to the space ship in the orbit to overcome the gravitational pull will be (if $g=10 \mathrm{~m} / \mathrm{s}^{2}$ and radius of earth $=6400 \mathrm{~km}$ ):
(1) $11.2(\sqrt{2}-1) \mathrm{km} / \mathrm{s}$
(2) $8(\sqrt{2}-1) \mathrm{km} / \mathrm{s}$
(3) $7.9(\sqrt{2}-1) \mathrm{km} / \mathrm{s}$
(4) $7.4(\sqrt{2}-1) \mathrm{km} / \mathrm{s}$

Answer (2)
Sol. $\Delta V=\sqrt{\frac{2 G M}{R}}-\sqrt{\frac{G M}{R}}=(\sqrt{2}-1) \sqrt{\frac{G M}{R}}$

$$
\begin{aligned}
& =(\sqrt{2}-1) \sqrt{g R} \\
& =(\sqrt{2}-1) \sqrt{10 \times 6400 \times 10^{3}} \\
& =8(\sqrt{2}-1) \mathrm{km} / \mathrm{s}
\end{aligned}
$$

46. The ratio of the de-Broglie wavelengths of proton and electron having same kinetic energy:
(Assume $m_{p}=m_{e} \times 1849$ )
(1) $1: 43$
(2) $1: 30$
(3) $1: 62$
(4) $2: 43$

Answer (1)
Sol. $(K)_{e}=(K)_{p}$

$$
\begin{aligned}
& \lambda=\frac{h}{\sqrt{2 k m}} \\
& \frac{\lambda_{p}}{\lambda_{e}}=\frac{\sqrt{2 k_{e} m_{e}}}{\sqrt{2 k_{e} m_{p}}}=\sqrt{\frac{m_{e}}{m_{p}}}=\sqrt{\frac{1}{1849}}=\frac{1}{43}
\end{aligned}
$$

47. 



The current flowing through $\mathrm{R}_{2}$ is :
(1) $\frac{2}{3} \mathrm{~A}$
(2) $\frac{1}{2} \mathrm{~A}$
(3) $\frac{1}{3} \mathrm{~A}$
(4) $\frac{1}{4} \mathrm{~A}$

Answer (3)

Sol. I through battery $\frac{8}{2}=4 \mathrm{~A}$
$I$ through $C D=\frac{3}{9} \times 2=\frac{2}{3} \mathrm{~A}$
$/$ through $R_{2}=\frac{1}{2}\left(\frac{2}{3}\right)=\frac{1}{3} \mathrm{~A}$
48. The thermodynamic process, in which internal energy of the system remains constant is
(1) Isochoric
(2) Adiabatic
(3) Isothermal
(4) Isobaric

## Answer (3)

Sol. $\Delta T=0, \Delta U=0$
49. If force ( F ), velocity $(\mathrm{V})$ and time $(\mathrm{T})$ are considered as fundamental physical quantity, then dimensional formula of density will be :
(1) $\mathrm{FV}^{4} \mathrm{~T}^{-6}$
(2) $\mathrm{FV}^{-4} \mathrm{~T}^{-2}$
(3) $\mathrm{F}^{2} \mathrm{~V}^{-2 T^{6}}$
(4) $\mathrm{FV}^{-2} \mathrm{~T}^{2}$

## Answer (2)

Sol. Density $=\frac{M}{L^{3}}=M L^{-3}=\left[M L T^{-2}\right]^{x}\left[L T^{-1}\right]^{y}[T]^{z}$
$M L^{-3}=M^{x} L^{(x+y)} T^{-2 x-y+z}$
$x=1, \quad x+y=-3, \quad-2 x-y+z=0$
$y=-4 \quad-2+4+z=0$
$z=-2$
density $=F V^{-4} T^{-2}$
50. The energy of $\mathrm{He}^{+}$ion in its first state is, (The ground state energy for the Hydrogen atom -13.6 eV ):
(1) -27.2 eV
(2) -3.4 eV
(3) -13.6 eV
(4) -54.4 eV

## Answer (3)

Sol. $E=-\frac{13.6 \times 2^{2}}{2^{2}}=-13.6 \mathrm{eV}$

## SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10 . The answer to each question is a NUMERICAL VALUE. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, $-00.33,-00.30,30.27,-27.30$ ) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
51. A nucleus disintegrates into two nuclear parts, in such a way that ratio of their nuclear sizes is $1: 2^{1 / 3}$. Their respective speed have a ratio of $n: 1$. The value of $n$ is $\qquad$

## Answer (2)

Sol. Momentum conservation

$$
\begin{aligned}
& m_{1} v_{1}=m_{2} v_{2} \\
& \Rightarrow\left(\frac{m_{1}}{m_{2}}\right)=\left(\frac{v_{2}}{v_{1}}\right) \\
& \Rightarrow\left(\frac{r_{1}}{r_{2}}\right)^{3}=\left(\frac{v_{2}}{v_{1}}\right) \Rightarrow\left(\frac{1}{2}\right)=\left(\frac{v_{2}}{v_{1}}\right) \\
& \frac{v_{1}}{v_{2}}
\end{aligned}=\frac{2}{1}-1 .
$$

52. A metallic cube of side 15 cm moving along $y$-axis at a uniform velocity of $2 \mathrm{~ms}^{-1}$. In a region of uniform magnetic field of magnitude 0.5 T directed along $z$ axis. In equilibrium the potential difference between the faces of higher and lower potential developed because of the motion through the field will be
$\qquad$ mV .


Answer (150)

Sol. $q E=e V B \quad \Rightarrow \quad \Delta V=(E . d)$

$$
\begin{aligned}
E=V B \quad & =(V B) \times 0.15 \\
& =2 \times \frac{1}{2} \times 0.15 \mathrm{~V} \\
& =0.15 \mathrm{~V}=150 \mathrm{mV}
\end{aligned}
$$

53. A wire of density $8 \times 10^{3} \mathrm{~kg} / \mathrm{m}^{3}$ is stretched between two clamps 0.5 m apart. The extension developed in the wire is $3.2 \times 10^{-4} \mathrm{~m}$. If $Y=8 \times 10^{10} \mathrm{~N} / \mathrm{m}^{2}$, the fundamental frequency of vibration in the wire will be $\qquad$ Hz .

## Answer (80)

Sol. $\frac{T}{A}=Y\left(\frac{\Delta L}{L}\right) \quad \mu=\left(\frac{m}{L}\right)$
$T=\left(\frac{Y \Delta L}{L} \times A\right)$
$\frac{T}{\mu}=\frac{Y \Delta L A}{L\left(\frac{m}{L}\right)}=\frac{Y(\Delta L) \times L A}{L(m)}=\left(\frac{Y \Delta L}{L}\right) \times\left(\frac{1}{\rho}\right)$
$\frac{T}{\mu}=\frac{8 \times 10^{10} \times 3.2 \times 10^{-4}}{0.5} \times\left(\frac{1}{8 \times 10^{3}}\right)=6.4 \times 10^{3}$
$\frac{T}{\mu}=64 \times 10^{2}$
$\sqrt{\frac{T}{\mu}}=8 \times 10=80 \mathrm{~m} / \mathrm{s}$
$f=\left(\frac{V}{2 L}\right)=\left(\frac{80}{1}\right)=80 \mathrm{~Hz}$
54. A coil has an inductance of 2 H and resistance of $4 \Omega$. A 10 V is applied across the coil. The energy stored in the magnetic field after the current has built up to its equilibrium value will be $\qquad$ $\times 10^{-2} \mathrm{~J}$.

## Answer (625)

Sol. $I=\frac{10}{4}=\frac{5}{2} \mathrm{~A}$

$$
E=\frac{1}{2} L i^{2}=\frac{1}{2} \times 2 \times\left(\frac{25}{4}\right)=625 \times 10^{-2} \mathrm{~J}
$$

55. A circular plate is rotating in horizontal plane, about an axis passing through its centre and perpendicular to the plate, with an angular velocity $\omega$. A person sits at the centre having two dumbbells in his hands. When he stretched out his hands, the moment of inertia of the system becomes triple. If $E$ be the initial Kinetic energy of the system, then final Kinetic energy will be $\frac{E}{x}$. The value of $x$ is

## Answer (3)

Sol. $E=\frac{1}{2} l \omega^{2}=\left(\frac{L^{2}}{2 l}\right)$
as $I^{\prime}=3 I$

$$
E_{f}=\frac{L^{2}}{6 l} \Rightarrow E_{f}=\left(\frac{E}{3}\right)
$$

56. As shown in the figure, a plane mirror is fixed at a height of 50 cm from the bottom of tank containing water $\left(\mu=\frac{4}{3}\right)$. The height of water in the tank is 8 cm . A small bulb is placed at the bottom of the water tank. The distance of image of the bulb formed by mirror from the bottom of the tank is
$\qquad$ cm .



Answer (98)
Sol. $h^{\prime}=\frac{8}{\frac{4}{3}}=6 \mathrm{~cm}$
Distance of object from mirror $=42+6=48 \mathrm{~m}$
Distance of image from bottom of tank $=48+50$

$$
=98 \mathrm{~m}
$$

57. Two identical cells each of emf 1.5 V are connected in series across a $10 \Omega$ resistance. An ideal voltmeter connected across $10 \Omega$ resistance reads 1.5 V. The internal resistance of each cell is
$\qquad$ $\Omega$.

Answer (5)

$i=\left(\frac{3}{10+2 r}\right)$
$10 \times \frac{3}{10+2 r}=1.5$
$20=10+2 r$
$\Rightarrow 2 r=10$
$r=5 \Omega$
58. In the given circuit.
$\mathrm{C}_{1}=2 \mu \mathrm{~F}, \mathrm{C}_{2}=0.2 \mu \mathrm{~F}, \mathrm{C}_{3}=2 \mu \mathrm{~F}, \mathrm{C}_{4}=4 \mu \mathrm{~F}, \mathrm{C}_{5}=$ $2 \mu \mathrm{~F}, \mathrm{C}_{6}=2 \mu \mathrm{~F}$. The charge stored on capacitor $\mathrm{C}_{4}$
$\qquad$ $\mu \mathrm{C}$.


Answer (4)
Sol. $q$ through battery $=10 \times \frac{1}{2}=5 \mu \mathrm{C}$

$$
\frac{q}{0.8 C}=\frac{5-q}{0.2}
$$

$\Rightarrow \quad q=20-4 q$
$5 q=20$

$$
q=4 \mu \mathrm{C}
$$

59. A block of mass 5 kg starting from rest pulled up on a smooth incline plane making an angle of $30^{\circ}$ with horizontal with an affective acceleration of $1 \mathrm{~ms}^{-2}$. The power delivered by the puling force at $t=10 \mathrm{~s}$ from the start is $\qquad$ W
[Use $\mathrm{g}=10 \mathrm{~ms}^{-2}$ ]
(Calculate the nearest integer value)

## Answer (300)

Sol.

$F-50 \sin 30=5 \times 1$
$F=5+25=30 \mathrm{~N}$
$v$ at $t=10 \mathrm{sec}=0+1 \times 10=10 \mathrm{~m} / \mathrm{s}$

Power $=30 \times 10=300$ watt
60. The surface tension of soap solution is $3.5 \times 10^{-2}$ $\mathrm{Nm}^{-1}$. The amount of work done required to increase the radius of soap bubble from 10 cm to 20 cm is $\qquad$ $\times 10^{-4} \mathrm{~J}$. (take $\pi=22 / 7$ )

Answer (264)

Sol. $\Delta U=\Delta w=(T \times \Delta A) \times 2$

$$
\begin{aligned}
& =3.5 \times 10^{-2} \times 4 \pi\left[(0.2)^{2}-(0.1)^{2}\right] \times 2 \\
& =3.5 \times 10^{-2} \times 4 \times \frac{22}{7} \times 0.03 \times 2 \\
& =2 \times 1.32 \times 10^{-2} \\
& =2 \times 132 \times 10^{-4} \mathrm{~J} \\
& =264 \times 10^{-4} \mathrm{~J}
\end{aligned}
$$

## CHEMISTRY

## SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

## Choose the correct answer:

61. For a chemical reaction $\mathrm{A}+\mathrm{B} \rightarrow$ Product, the order is 1 with respect to $A$ and $B$.

| Rate <br> $\mathrm{mol} \mathrm{L}^{-1} \mathrm{~S}^{-1}$ | $[\mathbf{A}]$ <br> $\mathrm{mol} \mathrm{L}^{-1}$ | $[\mathbf{B}]$ <br> $\mathrm{mol} \mathrm{L}^{-1}$ |
| :---: | :---: | :---: |
| 0.10 | 20 | 0.5 |
| 0.40 | x | 0.5 |
| 0.80 | 40 | y |

What is the value of $x$ and $y$ ?
(1) 160 and 4
(2) 80 and 4
(3) 80 and 2
(4) 40 and 4

## Answer (3)

Sol. Rate of Reaction $\alpha$ (A) (B)
From experiment II $\quad x=80$
from experiment III $\quad y=2$
62. Which of the following compounds is an example of Freon?
(1) $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{~F}_{2}$
(2) $\mathrm{C}_{2} \mathrm{~F}_{4}$
(3) $\mathrm{C}_{2} \mathrm{HF}_{3}$
(4) $\mathrm{C}_{2} \mathrm{Cl}_{2} \mathrm{~F}_{2}$

## Answer (4)

Sol. From is chlorofluoro carbons. Hence the correct answer is (4).
63. Alkali metal from the following with least melting point is
(1) Cs
(2) Rb
(3) Na
(4) K

## Answer (1)

Sol. Element
Na
K
Rb
Cl
M.P. (k)

371
336
Rb
312
302
64. Compound from the following that will not produce precipitate on reaction with $\mathrm{AgNO}_{3}$ is
(1)

(2)

(3)

(4)


Answer (4)
Sol. Compounds which results in the formation of stable carbocation upon rating with $\mathrm{AgNO}_{3}$ will produce precipitate.
65. Which one of the following pairs is an example of polar molecular solids?
(1) $\mathrm{SO}_{2}(\mathrm{~s}), \mathrm{CO}_{2}(\mathrm{~s})$
(2) $\mathrm{SO}_{2}(\mathrm{~s}), \mathrm{NH}_{3}(\mathrm{~s})$
(3) $\mathrm{MgO}(\mathrm{s}), \mathrm{SO}_{2}(\mathrm{~s})$
(4) $\mathrm{HCl}(\mathrm{s}), \mathrm{AlN}(\mathrm{s})$

Answer (2)
Sol. Solide
$\mathrm{SO}_{2}$ (s)
$\mathrm{CO}_{2}$ (s)
NH3(s)
MgO
HCl
AIN

## type

Polar molecular
Non polar molecular Polar molecular Ionic Solid
Polar molecular solid
Covalent solid
66. Which hydride among the following is less stable?
(1) $\mathrm{BeH}_{2}$
(2) HF
(3) $\mathrm{NH}_{3}$
(4) LiH

Answer (1)
Sol. $\mathrm{BeH}_{2}$ is the least stable among the given hydrides.
67. If $\mathrm{Ni}^{2+}$ is replaced by $\mathrm{Pt}^{2+}$ in the complex $\left[\mathrm{NiCl}_{2} \mathrm{Br}_{2}\right]^{2-}$, which of the following properties are expected to get changed?
A. Geometry
B. Geometrical isomerism
C. Optical isomerism
D. Magnetic properties
(1) A and D
(2) A, B and C
(3) B and C
(4) A, B and D

## Answer (4)

Sol. $\left[P+\mathrm{Cl}_{2} \mathrm{Br}_{2}\right]^{2-}-$ Square planar

$\left[\mathrm{PtCl}_{2} \mathrm{Br}_{2}\right]^{2-}$-Diamagnetic
68. Match List I with List II

| LIST-I <br> Complex |  | LIST II <br> Colour |  |
| :--- | :--- | :--- | :--- |
| A. | $\mathrm{Mg}\left(\mathrm{NH}_{4}\right) \mathrm{PO}_{4}$ | I. | brown |
| B. | $\mathrm{K}_{3}\left[\mathrm{Co}\left(\mathrm{NO}_{2}\right)_{6}\right]$ | II. | white |
| C. | $\mathrm{MnO}(\mathrm{OH})_{2}$ | III. | yellow |
| D. | $\mathrm{Fe} 4\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]_{3}$ | IV. | Blue |

Choose the correct answer from the options given below:
(1) A-III, B-IV, C-II, D-I
(2) A-II, B-III, C-I, D-IV
(3) A-II, B-IV, C-I, D-III
(4) A-II, B-III, C-IV, D-I

## Answer (2)

Sol.

| Complex | Colour |
| :--- | :--- |
| $\mathrm{Mg}\left(\mathrm{NH}_{4}\right) \mathrm{PO}_{4}$ | White |
| $\mathrm{K}_{3}\left[\mathrm{Co}\left(\mathrm{NO}_{2}\right)_{6}\right]$ | Yellow |
| $\mathrm{MnO}(\mathrm{OH})_{2}$ | Brown |
| $\mathrm{Fe}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]_{3}$ | Blue |

69. Given below are two statements :

Statement I: In the metallurgy process, sulphide ore is converted to oxide before reduction.

Statement II : Oxide ores in general are easier to reduce.

In the light of the above statements, choose the most appropriate answer from the options given below :
(1) Statement I is correct but Statement II is incorrect
(2) Both Statement I and Statement II are incorrect
(3) Statement I is incorrect but Statement II is correct
(4) Both Statement I and Statement II are correct

## Answer (4)

Sol. Both Statements (I) and (II) are correct.
70. A solution is prepared by adding 2 g of " $X$ " to 1 mole of water. Mass percent of " $X$ " in the solution is
(1) $5 \%$
(2) $20 \%$
(3) $2 \%$
(4) $10 \%$

Answer (4)
Sol. Mass percent of $X=\frac{2}{2+18} \times 100=10$
71. What weight of glucose must be dissolved in 100 g of water to lower the vapour pressure by 0.20 mm Hg ?
(Assume dilute solution is being formed)
Given : Vapour pressure of pure water is 54.2 mm Hg at room temperature. Molar mass of glucose is $180 \mathrm{~g} \mathrm{~mol}^{-1}$
(1) 3.59 g
(2) 3.69 g
(3) 4.69 g
(4) 2.59 g

Answer (2)

Sol. Using the formula

$$
\frac{P_{0}-P}{P}=\frac{\text { Moles of solute }}{\text { Moles of solvent }}
$$

$$
\frac{54.2-54}{54}=\frac{w / 180}{\frac{100}{18}}
$$

$$
\mathrm{w}=3.69 \mathrm{~g}
$$

72. Given below are two statements :

Statement I : Ethane at 333 to 343 K and 6-7 atm pressure in the presence of $\mathrm{AlEt}_{3}$ and $\mathrm{TiCl}_{4}$ undergoes addition polymerization to give LDP.

Statement II : Caprolactam at $533-543 \mathrm{~K}$ in $\mathrm{H}_{2} \mathrm{O}$ through step growth polymerizes to give Nylon 6.
In the light of the above statements, choose the correct answer from the options given below:
(1) Statement I is false but Statement II is true
(2) Statement I is true but Statement II is false
(3) Both Statement I and Statement II are true
(4) Both Statement I and Statement II are false

## Answer (1)

Sol. Ethene at 333 to 343 K and 6-7 atm pressure in the presence of $\mathrm{AlEt}_{3}$ and $\mathrm{TiCl}_{4}$ undergo addition polymerization to give HDP.
Caprolactam at $533-543 \mathrm{~K}$ in $\mathrm{H}_{2} \mathrm{O}$ through step growth polymerization gives Nylon 6.
73. Compound ' $B$ ' is

(1)

(2)

(3)

(4)


Answer (1)

Sol.

(A)

(B)
74. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R. Assertion A : A solution of the product obtained by heating a mole of glycine with a mole of chlorine in presence of red phosphorous generates chiral carbon atom.

Reason R : A molecule with 2 chiral carbons is always optically active.
In the light of the above statements, choose the correct answer from the options given below :
(1) $A$ is true but $R$ is false
(2) Both $A$ and $R$ are true but $R$ is the correct explanation of $A$
(3) $A$ is false but $R$ is true
(4) Both $A$ and $R$ are true but $R$ is NOT the correct explanation of $A$
Answer (1)


All molecules with 2 chiral carbons are not always optically active.
E.g.


Optically inactive
75. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.

Assertion
 can be subjected to Wolff-Kishner reduction to give


Reason R : Wolff-Kishner reduction is used to convert


In the light of the above statements, choose the correct answer from the options given below :
(1) $A$ is true but $R$ is false
(2) $A$ is false but $R$ is true
(3) Both $A$ and $R$ are true and $R$ is the correct explanation of A
(4) Both A and R are true but R is NOT the correct explanation of A

## Answer (2)

Sol.


Wolff-Kishner reduction is used to convert into $\widehat{\text {. }}$
76. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : $\left[\mathrm{CoCl}\left(\mathrm{NH}_{3}\right)_{5}\right]^{2+}$ absorbs at lower wavelength of light with respect to $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right) 5\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{3+}$

Reason R : It is because the wavelength of the light absorbed depends on the oxidation state of the metal ion.

In the light of the above statements, choose the correct answer from the options given below :
(1) $A$ is false but $R$ is true
(2) $A$ is true but $R$ is false
(3) Both $A$ and $R$ are true and $R$ is the correct explanation of $A$
(4) Both $A$ and $R$ are true but $R$ is NOT the correct explanation of $A$

## Answer (1)

Sol. $\left[\mathrm{CoCl}\left(\mathrm{NH}_{3}\right)_{5}\right]^{2+}$ absorbs at higher wavelength of light with respect to $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{H}_{2} \mathrm{O}\right]^{3+}$ because $\mathrm{Cl}^{-}$is weaker ligand than $\mathrm{H}_{2} \mathrm{O}$.

Wavelength of light absorbed depends upon the oxidation state of the metal ion.
Hence, $A$ is false but $R$ is true.


Product $[\mathrm{X}]$ formed in the above reaction is :
(1)

(2) $\mathrm{H}_{3} \mathrm{C}-\mathrm{CH}=\mathrm{CH}-\mathrm{CH}_{3}$
(3)

(4) $\mathrm{H}_{2} \mathrm{C}-\mathrm{CH}_{2}-\mathrm{CH}=\mathrm{CH}_{2}$

## Answer (3)

Sol.

78. One mole of $\mathrm{P}_{4}$ reacts with 8 moles of $\mathrm{SOCl}_{2}$ to give 4 moles of $\mathrm{A}, \mathrm{x}$ mole of $\mathrm{SO}_{2}$ and 2 moles of B . A, B and x respectively are
(1) $\mathrm{POCl}_{3}, \mathrm{~S}_{2} \mathrm{Cl}_{2}$ and 2
(2) $\mathrm{PCl}_{3}, \mathrm{~S}_{2} \mathrm{Cl}_{2}$ and 4
(3) $\mathrm{PCl}_{3}, \mathrm{~S}_{2} \mathrm{Cl}_{2}$ and 2
(4) $\mathrm{POCl}_{3}, \mathrm{~S}_{2} \mathrm{Cl}_{2}$ and 4

## Answer (2)

Sol. $\mathrm{P}_{4}+8 \mathrm{SOCl}_{2} \longrightarrow 4 \mathrm{PCl}_{3}+4 \mathrm{SO}_{2}+2 \mathrm{~S}_{2} \mathrm{Cl}_{2}$
Hence, $\mathrm{A}=\mathrm{PCl}_{3}, \mathrm{x}=4, \mathrm{~B}=\mathrm{S}_{2} \mathrm{Cl}_{2}$
79. The magnetic moment is measured in Bohr Magneton (BM).
Spin only magnetic moment of Fe in $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ and $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ complexes respectively is:
(1) 6.92 B.M. in both
(2) 3.87 B.M. and 1.732 B.M.
(3) 5.92 B.M. and 1.732 B.M.
(4) 4.89 B.M. and 6.92 B.M.

## Answer (3)

Sol. $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}=\mathrm{d}^{5}(\mathrm{H} . \mathrm{S})=$.5 unpaired electrons

$$
\begin{aligned}
\mu & =\sqrt{5 \times 7}=\sqrt{35} \\
& =5.92 \mathrm{~B} . \mathrm{M} . \\
{\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-} } & =\mathrm{d}^{5}(\mathrm{~L} . \mathrm{S} .)=1 \text { unpaired electrons } \\
\mu & =\sqrt{1 \times 3}=\sqrt{3} \\
& =1.732 \mathrm{~B} . \mathrm{M} .
\end{aligned}
$$

80. The major product formed in the following reaction is


B. $\mathrm{C}_{6} \mathrm{H}_{5}-\mathrm{CH}=\underset{\mathrm{CH}_{3}}{\mathrm{C}}-\mathrm{C}_{2} \mathrm{H}_{5}$

D.


Choose the correct answer from the options given below:
(1) B only
(2) A only
(3) C only
(4) D only

Answer (B)

Sol.


## SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10 . The answer to each question is a NUMERICAL VALUE. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., $06.25,07.00,-00.33,-00.30,30.27,-27.30$ ) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
81. Number of compounds from the following which will not produce orange red precipitate with Benedict solution is $\qquad$ .
Glucose, maltose, sucrose, ribose, 2-deoxyribose, amylose, lactose

## Answer (2)

Sol. Except sucrose and amylose all other give orange red precipitate with Benedict solution.
Sucrose being non-reducing disaccharide and amylose being polysaccharides do not give positive Benedict's test.
82. The maximum number of lone pairs of electron on the central atom from the following species is $\qquad$ _.
$\mathrm{ClO}_{3}{ }^{-}, \mathrm{XeF}_{4}, \mathrm{SF}_{4}$ and $\mathrm{I}_{3}{ }^{-}$
Answer (3)

Sol.


1 L.P on central atom


1L.P on central
atom

2. L.P. on central atom

3. L.P. on central
atom
83. The number of correct statements from the following is $\qquad$ .
A. For 1 s orbital, the probability density is maximum at the nucleus
B. For $2 s$ orbital, the probability density first increases to maximum and then decreases sharply to zero.
C. Boundary surface diagrams of the orbitals encloses a region of $100 \%$ probability of finding the electron.
D. $p$ and d-orbitals have 1 and 2 angular nodes respectively
E. probability density of p-orbital is zero at the nucleus

## Answer (3)

Sol. Except B and C all statements are correct.
Probability density curves for $1 \mathrm{~s}, 2 \mathrm{~s}$ and 2 p orbitals are given below.

84. The total number of intensive properties from the following is $\qquad$ .
Volume, Molar heat capacity, molarity, $\mathrm{E}^{\ominus}$ cell, Gibbs free energy change, Molar mass, Mole

## Answer (4)

Sol. Molar heat capacity, molarity, $\mathrm{E}_{\text {cell }}^{\circ}$ and molar mass are intensive properties.
85. 4.5 moles each of hydrogen and iodine is heated in a sealed ten litre vessel. At equilibrium, 3 moles of HI were found. The equilibrium constant for $\mathrm{H}_{2}(\mathrm{~g})+$ $\mathrm{I}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{HI}(\mathrm{g})$ is $\qquad$ .

## Answer (1)

Sol. $\quad \mathrm{H}_{2}+\mathrm{I}_{2} \rightleftharpoons 2 \mathrm{HI}$
$\begin{array}{llll}\text { at initial } & 4.5 & 4.5 & 0\end{array}$
at equilibrium 3 3 3
$\mathrm{k}_{\mathrm{eq}}=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(3)^{2}}{3 \times 3}=1$
86. The volume of hydrogen liberated at STP by treating 2.4 g of magnesium with excess of hydrochloric acid is $\qquad$ $\times 10^{-2} \mathrm{~L}$

Given: Molar volume of gas is 22.4 L at STP.
Molar mass of magnesium is $24 \mathrm{~g} \mathrm{~mol}^{-1}$

## Answer (224)

Sol. $\underset{\substack{2.49 \\ \text { 2. } \\=0.1 \text { mole }}}{\mathrm{Mg}}+2 \mathrm{HCl} \longrightarrow \mathrm{MgCl}_{2}+\underset{0.1 \text { mole }}{\mathrm{H}_{2}}$
Volume of 1 mole $\mathrm{H}_{2}$ at STP $=22.4$ Litre
$\therefore 0.1 \mathrm{~mole}_{\mathrm{H}}$ at STP will occupy $=2.24$ Litre
87. The number of correct statements about modern adsorption theory of heterogeneous catalysis from the following is $\qquad$ .
A. The catalyst is diffused over the surface of reactants.
B. Reactants are adsorbed on the surface of the catalyst.
C. Occurrence of chemical reaction on the catalyst's surface through formation of an intermediate.
D. It is a combination of intermediate compound formation theory and the old adsorption theory.
E. It explains the action of the catalyst as well as those of catalytic promoters and poisons.

## Answer (3)

Sol. Except (A) and (E) all statements are correct.
88. The number of possible isomeric products formed when 3-chloro-1-butene reacts with HCl through carbocation formation is $\qquad$ .

## Answer (4)

Sol.

89. $\mathrm{Mg}\left(\mathrm{NO}_{3}\right)_{2} \cdot \mathrm{XH}_{2} \mathrm{O}$ and $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2} \cdot \mathrm{YH}_{2} \mathrm{O}$, represent formula of the crystalline forms of nitrate salts. Sum of $X$ and $Y$ is $\qquad$ _.

## Answer (6)

Sol. Magnesium nitrate crystallises with six molecules of water, whereas barium nitrate crystallises as the anhydrous salt as $\mathrm{Mg}\left(\mathrm{NO}_{3}\right)_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$
$\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$ respectively
$\therefore x=6, y=0$
90. The number of correct statements from the following is $\qquad$ .
A. Ecell is an intensive parameter
B. A negative $\mathrm{E}^{\ominus}$ means that the redox couple is a stronger reducing agent than the $\mathrm{H}^{+} / \mathrm{H}_{2}$ couple.
C. The amount of electricity required for oxidation or reduction depends on the stoichiometry of the electrode reaction.
D. The amount of chemical reaction which occurs at any electrode during electrolysis by a current is proportional to the quantity of electricity passed through the electrolyte.

## Answer (4)

Sol. All statements are correct.

