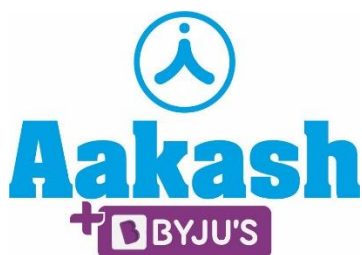


13/04/2023

Evening



Corporate Office : Aakash Tower, 8, Pusa Road, New Delhi-110005 | Ph.: 011-47623456

Answers & Solutions

Time : 3 hrs.

for

M.M. : 300

JEE (Main)-2023 (Online) Phase-2

(Mathematics, Physics and Chemistry)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) The Test Booklet consists of 90 questions. The maximum marks are 300.
- (3) There are **three** parts in the question paper consisting of **Mathematics, Physics** and **Chemistry** having 30 questions in each part of equal weightage. Each part (subject) has two sections.
 - (i) **Section-A:** This section contains 20 multiple choice questions which have only one correct answer. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer.
 - (ii) **Section-B:** This section contains 10 questions. In Section-B, attempt any **five questions out of 10**. The answer to each of the questions is a numerical value. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

Sol. $f_n = \int_0^{\pi/2} \left(\sum_{k=1}^n \sin^{k-1} x \right) \left(\sum_{k=1}^n (2k-1) \sin^{k-1} x \right) \cos x \, dx$

put $\sin x = t$
 $\cos x \, dx = dt$

$$f_n = \int_0^1 \left(\sum_{k=1}^n (t)^{k-1} \right) \left(\sum_{k=1}^n (2k-1) (t)^{k-1} \right) dt$$

$$f_{21} - f_{20} = \int_0^1 \left(\sum_{k=1}^{21} (t)^{k-1} \right) \left(\sum_{k=1}^{21} (2k-1) (t)^{k-1} \right) - \left(\sum_{k=1}^{20} (t)^{k-1} \right) \left(\sum_{k=1}^{20} (2k-1) (t)^{k-1} \right) dt$$

$$= \int_0^1 (1+t+t^2+\dots+t^{19}) (41) t^{20} + (1+3t+5t^2+\dots+41t^{20}) t^{20} dt$$

$$= \left(\frac{1}{21} + \frac{1}{22} + \dots + \frac{1}{40} \right) 41 + \left(\frac{1}{21} + \frac{3}{22} + \dots + \frac{39}{40} + \frac{41}{41} \right)$$

$$= \left[\frac{42}{21} + \frac{44}{22} + \frac{46}{23} + \dots + \frac{80}{40} + \frac{41}{41} \right]$$

$$= 40 + 1 = 41$$

22. Let $A = \{-4, -3, -2, 0, 1, 3, 4\}$ and $R = \{(a, b) \in A \times A : b = |a| \text{ or } b^2 = a + 1\}$ be a relation on A . Then the minimum number of elements, that must be added to the relation R so that it becomes reflexive and symmetric, is _____.

Answer (7)

Sol. $A = \{-4, -3, -2, 0, 1, 3, 4\}$

$$R = \{(-4, 4), (-3, 3), (0, 0), (1, 1), (3, 3), (4, 4), (0, 1), (3, -2)\}$$

Relation to be reflexive $(a, a) \in R \forall a \in A$

$\Rightarrow (-4, -4), (-3, -3), (-2, -2)$ also should be added in R .

Relation to be symmetric if $(a, b) \in R$, then $(b, a) \in R \forall a, b \in A$

$\Rightarrow (4, -4), (3, -3), (1, 0), (-2, 3)$ also should be added in R

\Rightarrow Minimum number of elements to be added to $R = 3 + 4 = 7$

23. The foci of a hyperbola are $(\pm 2, 0)$ and its eccentricity is $\frac{3}{2}$. A tangent, perpendicular to the line $2x + 3y = 6$, is drawn at a point in the first quadrant on the hyperbola. If the intercepts made by the tangent on the x - and y -axes are a and b respectively, then $|6a| + |5b|$ is equal to _____

Answer (12)

Sol. $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1, ae = 2, e = \frac{3}{2} \Rightarrow a = \frac{4}{3}$

$$b^2 = a^2 e^2 - a^2 = 4 - \frac{16}{9} = \frac{20}{9}$$

Equation of tangent, $m = \frac{3}{2}$

$$y = \frac{3}{2}x - \sqrt{\frac{16}{9} \times \frac{9}{4} - \frac{20}{9}}$$

(\because Tangent is in 1st quadrant $\Rightarrow C < 0$)

$$\Rightarrow a = \frac{8}{9}, b = -\frac{4}{3} \Rightarrow |6a| + |5b| = 12$$

24. If $y = y(x)$ is the solution of the differential equation

$$\frac{dy}{dx} + \frac{4x}{(x^2-1)} y = \frac{x+2}{(x^2-1)^{\frac{5}{2}}}, x > 1 \quad \text{such that}$$

$$y(2) = \frac{2}{9} \log_e(2 + \sqrt{3}) \text{ and}$$

$$y(\sqrt{2}) = \alpha \log_e(\sqrt{\alpha} + \beta) + \beta - \sqrt{\gamma}, \alpha, \beta, \gamma \in \mathbb{N}, \text{ then}$$

$\alpha\beta\gamma$ is equal to _____.

Answer (6)

Sol. IF $= e^{\int \frac{4x}{x^2-1} dx} = (x^2-1)^2$

$$y \cdot (x^2-1)^2 = \int \frac{x+2}{(x^2-1)^{1/2}} dx$$

$$y \cdot (x^2-1)^2 = \ln(|\sqrt{x^2-1} + x|) + \sqrt{x^2-1} + C$$

at $x = 2$,

$$9 \cdot \frac{2}{9} \ln(2 + \sqrt{3}) = 2 \ln(2 + \sqrt{3}) + \sqrt{3} + C$$

$$C = -\sqrt{3}$$

at $x = \sqrt{2}$

$$y(1) = 2 \ln(1 + \sqrt{2}) + 1 - \sqrt{3}$$

$$\beta = 1, \alpha = 2, \gamma = 3$$

25. Total numbers of 3-digit numbers that are divisible by 6 and can be formed by using the digits 1, 2, 3, 4, 5 with repetition, is _____

Answer (16)

Sol. $a \leq b \leq 2$

$a + b$ can be 4, 7, 10

if $a + b = 4$ then (a, b) can be (1, 3) OR (3, 1) OR (2, 2)

if $a + b = 7$ then (a, b) can be (2, 5), (5, 2), (3, 4), (4, 3)

if $a + b = 10$ then (a, b) can be (5, 5)

8 such cases when 2 is at unit's place similarly there exist 8 such cases when 4 is at unit's place.

Total = 16

26. For $x \in (-1, 1]$, the number of solutions of the equation $\sin^{-1} x = 2 \tan^{-1} x$ is equal to _____.

Answer (2)

Sol. $\sin(\sin^{-1} x) = \sin(2 \tan^{-1} x)$

$$x = \frac{2x}{1+x^2}$$

$$x = 0, \pm 1$$

$\Rightarrow x = 0$ and 1 are possible.

27. The mean and standard deviation of the marks of 10 students were found to be 50 and 12 respectively. Later, it was observed that two marks 20 and 25 were wrongly read as 45 and 50 respectively. Then the correct variance is _____.

Answer (269)

Sol. $\sum x_i \text{ (wrong)} = 500$

$$144 = \frac{\sum x_i^2 \text{ (wrong)}}{10} - (50)^2$$

$$26440 = \sum x_i^2 \text{ (wrong)}$$

$$\sum x_i \text{ (correct)} = 450$$

$$\Rightarrow \bar{x}_i \text{ (correct)} = 45$$

$$\sum x_i^2 \text{ (correct)} = 26440 - 3500 = 22940$$

$$\text{Variance} = \frac{22940}{10} - (45)^2$$

$$= 2294 - 2025$$

$$= 269$$

28. The remainder, when 7^{103} is divided by 17, is _____.

Answer (12)

Sol. 7^{103} divided by 17

$$7 \equiv 7 \pmod{17}$$

$$7^2 \equiv -2 \pmod{17}$$

$$7^6 \equiv -8 \pmod{17}$$

$$7^8 \equiv -1 \pmod{17}$$

$$7^{16} \equiv 1 \pmod{17}$$

$$7^{103} \equiv 12 \pmod{17}$$

\therefore Remainder = 12

29. Let $[\alpha]$ denote the greatest integer $\leq \alpha$. Then $[\sqrt{1}] + [\sqrt{2}] + [\sqrt{3}] + \dots + [\sqrt{120}]$ is equal to _____.

Answer (825)

Sol. $[\sqrt{1}] + [\sqrt{2}] + [\sqrt{3}] + \dots + [120]$

$$E = 1 + 1 + 1 + 2 + 2 + 2 + 2 + 2 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 4 + 4 + \dots$$

$$E = 3 \times 1 + 5 \times 2 + 7 \times 3 + \dots + 19 \times 9 + 10 \times 21$$

$$= \sum_{r=1}^{10} (2r+1)r = 2 \left[\frac{10 \times 11 \times 21}{6} \right] + \frac{10 \times 11}{2}$$

$$= 770 + 55$$

$$= 825$$

30. Let $f(x) = \sum_{k=1}^{10} k x^k, x \in \mathbb{R}$.

If $2f(2) + f'(2) = 119(2)^n + 1$ then n is equal to _____.

Answer (10)

Sol. $f(x) = \sum_{k=1}^{10} k x^k$

$$S = x + 2x^2 + 3x^3 + \dots + 10x^{10}$$

$$S_x = \frac{x^2 + 2x^3 + \dots + 9x^{10} + 10x^{11}}{1-x}$$

$$S(1-x) = x + x^2 + x^3 + \dots + x^{10} - 10x^{11}$$

$$S(1-x) = \frac{x(1-x^{10})}{1-x} - 10x^{11}$$

$$S = \frac{x(1-x^{10})}{(1-x)^2} - \frac{10x^{11}}{(1-x)} = f(x)$$

$$f(2) = 2(1-2^{10}) + 10 \cdot 2^{11}$$

$$= 2 + 18 \cdot 2^{10}$$

$$f' = \frac{-10x^{11}}{(1-x)^2} - \frac{110x^{10}}{1-x} - \frac{10x^{10}}{(1-x)^2} + \frac{2x(1-x^{10})}{(1-x)^3} +$$

$$\frac{1-x^{10}}{(1-x)}$$

$$2f(2) + f'(2) = 119(2)^{10} + 1$$

$\therefore n = 10$

PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

31. Given below are two statements:

Statement I : Out of microwaves, infrared rays and ultraviolet rays, ultraviolet rays are the most effective for the emission of electrons from a metallic surface.

Statement II : Above the threshold frequency, the maximum kinetic energy of photoelectrons is inversely proportional to the frequency of the incident light.

In the light of above statements, choose the **correct** answer from the options given below

- (1) Statement I is false but Statement II is true
- (2) Statement I is true but Statement II is false
- (3) Both Statement I and Statement II are true
- (4) Both Statement I and Statement II are false

Answer (2)

Sol. Since UV would be having highest frequency,

⇒ Most effective for electron emission.

Also, $K_{\max} = hf - \phi$

⇒ Statement II is wrong

32. The distance travelled by an object in time t is given by $s = (2.5)t^2$. The instantaneous speed of the object at $t = 5$ s will be :

- (1) 25 ms^{-1} (2) 5 ms^{-1}
- (3) 62.5 ms^{-1} (4) 12.5 ms^{-1}

Answer (1)

Sol. $s = 2.5t^2$

⇒ Speed = $5t$

⇒ At $t = 5$ s, speed = 25 m/s

33. In a Young's double slit experiment, the ratio of amplitude of light coming from slits is 2 : 1. The ratio of the maximum to minimum intensity in the interference pattern is

- (1) 9 : 4 (2) 25 : 9
- (3) 2 : 1 (4) 9 : 1

Answer (4)

Sol.
$$\frac{I_{\max}}{I_{\min}} = \frac{(\sqrt{I_1} + \sqrt{I_2})^2}{(\sqrt{I_1} - \sqrt{I_2})^2}$$

$$= \left(\frac{A_1 + A_2}{A_1 - A_2} \right)^2 = \left(\frac{2+1}{2-1} \right)^2 = 9$$

34. A $10 \mu\text{C}$ charge is divided into two parts and placed at 1 cm distance so that the repulsive force between them is maximum. The charges of the two parts are:

- (1) $7 \mu\text{C}, 3 \mu\text{C}$ (2) $8 \mu\text{C}, 2 \mu\text{C}$
- (3) $5 \mu\text{C}, 5 \mu\text{C}$ (4) $9 \mu\text{C}, 1 \mu\text{C}$

Answer (3)

Sol. We know that for $\frac{Q}{2}, \frac{Q}{2}$ force would be maximum.

35. A passenger sitting in a train A moving at 90 km/h observes another train B moving in the opposite direction for 8 s. If the velocity of the train B is 54 km/h, then length of train B is:

- (1) 120 m (2) 320 m
- (3) 80 m (4) 200 m

Answer (2)

Sol. Relative velocity = 144 km/h
= 40 m/s

⇒ Length = $40 \text{ m/s} \times 8 \text{ s}$
= 320 m

36. The initial pressure and volume of an ideal gas are P_0 and V_0 . The final pressure of the gas when the gas is suddenly compressed to volume $\frac{V_0}{4}$ will be:

(Given γ = ratio of specific heats at constant pressure and at constant volume)

- (1) $P_0(4)^\gamma$ (2) $4P_0$
- (3) P_0 (4) $P_0(4)^{\frac{1}{\gamma}}$

Answer (1)

Sol. $PV^\gamma = \text{constant}$

$$P_0 V_0^\gamma = P \cdot \left(\frac{V_0}{4} \right)^\gamma$$

⇒ $P = 4^\gamma \cdot P_0$

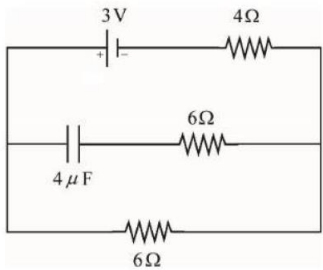
37. A vehicle of mass 200 kg is moving along a levelled curved road of radius 70 m with angular velocity of 0.2 rad/s. The centripetal force acting on the vehicle is:

- (1) 560 N (2) 2800 N
 (3) 2240 N (4) 14 N

Answer (1)

Sol. $F = MR\omega^2$
 $= 200 \times 70 \times 0.2^2 \text{ N}$
 $= 560 \text{ N}$

38. In the network shown below, the charge accumulated in the capacitor in steady state will be:



- (1) 10.3 μC (2) 4.8 μC
 (3) 12 μC (4) 7.2 μC

Answer (4)

Sol. In steady state, capacitor behaves as open circuit.

$\Rightarrow \Delta V_C = i \times 6 \Omega$
 $= \frac{3}{10} \times 6 \text{ V}$
 $= 1.8 \text{ V}$

$\Rightarrow Q = CV = 7.2 \mu\text{C}$

39. Given below are two statements:

Statement I : An AC circuit undergoes electrical resonance if it contains either a capacitor or an inductor.

Statement II: An AC circuit containing a pure capacitor or a pure inductor consumes high power due to its non-zero power factor.

In the light of above statements, choose the **correct** answer from the options given below:

- (1) Statement I is false but statement II is true
 (2) Statement I is true but statement II is false
 (3) Both Statement I and Statement II are false
 (4) Both Statement I and Statement II are true

Answer (3)

Sol. For resonance, $X_L = X_C$

\Rightarrow Both inductor and capacitor would be required.

Also, for pure capacitor or pure inductor power factor = 0

\Rightarrow Both statements are incorrect

40. A particle executes SHM of amplitude A. The distance from the mean position when its kinetic energy becomes equal to its potential energy is:

- (1) $\frac{1}{\sqrt{2}} A$ (2) 2A
 (3) $\sqrt{2} A$ (4) $\frac{1}{2} A$

Answer (1)

Sol. $\frac{1}{2} m\omega^2 (A^2 - x^2) = \frac{1}{2} m\omega^2 x^2$

$\Rightarrow x = \frac{A}{\sqrt{2}}$

41. In the equation $\left[X + \frac{a}{Y^2} \right] [Y - b] = RT$, X is pressure, Y is volume, R is universal gas constant T is temperature. The physical quantity equivalent to the ratio $\frac{a}{b}$ is:

- (1) Pressure gradient
 (2) Energy
 (3) Impulse
 (4) Coefficient of viscosity

Answer (2)

Sol. $a \equiv PV^2$

$b \equiv V$

$\Rightarrow \frac{a}{b} \equiv PV \equiv \text{Energy}$

42. To radiate EM signal of wavelength λ with high efficiency, The antennas should have a minimum size equal to:

- (1) 2λ (2) $\frac{\lambda}{2}$
 (3) $\frac{\lambda}{4}$ (4) λ

Answer (3)

Sol. Length of antenna = $\frac{\lambda}{4}$

43. Given below are two statements: one is labelled as **Assertion A** and the other is labelled as **Reason R**

Assertion A : A spherical body of radius (5 ± 0.1) mm having a particular density is falling through a liquid of constant density. The percentage error in the calculation of its terminal velocity is 4%.

Reason R : The terminal velocity of the spherical body falling through the liquid is inversely proportional to its radius.

In the light of the above statements, choose the **correct** answer from the options given below

- (1) Both **A** and **R** are true and **R** is the correct explanation of **A**
- (2) Both **A** and **R** are true but **R** is **NOT** the correct explanation of **A**
- (3) **A** is true but **R** is false
- (4) **A** is false but **R** is true

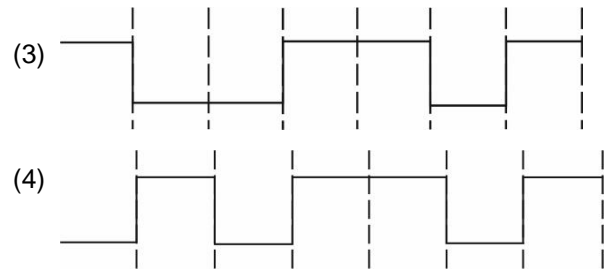
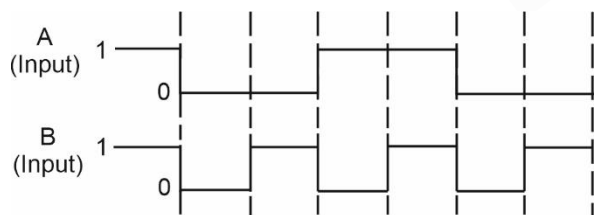
Answer (3)

Sol. $V_T = \frac{2}{9} r^2 g \frac{(\rho - \rho')}{\eta} \propto r^2$

$$\Rightarrow \frac{dV_T}{V_T} = 2 \frac{dr}{r} = 2 \times \frac{0.1}{5}$$

$$\equiv 4\%$$

44. The output from a NAND gate having inputs A and B given below will be,



Answer (2)

Sol. $Y = (AB)'$

$\Rightarrow Y$ would be zero only when both A and B are 1.

\Rightarrow option 2.

45. The mean free path of molecules of a certain gas at STP is $1500d$, where d is the diameter of the gas molecules. While maintaining the standard pressure, the mean free path of the molecules at 373 K is approximately:

- (1) $750d$
- (2) $1098d$
- (3) $2049d$
- (4) $1500d$

Answer (3)

Sol. Mean free path $= \frac{1}{\sqrt{2}\pi n d^2}$

$$\Rightarrow \frac{1500d}{\lambda'} = \frac{273}{373}$$

$$\Rightarrow \lambda' = 2049.45d$$

46. Two planets A and B of radii R and $1.5R$ have densities ρ and $\rho/2$ respectively. The ratio of acceleration due to gravity at the surface of B to A is:

- (1) 2 : 3
- (2) 2 : 1
- (3) 3 : 4
- (4) 4 : 3

Answer (3)

Sol. $g = \frac{GM}{R^2} \propto \rho \cdot R$

$$\Rightarrow \frac{g_B}{g_A} = \frac{1}{2} \times 1.5 = 0.75$$

47. In an electromagnetic wave, at an instant and at a particular position, the electric field is along the negative z-axis and magnetic field is along the positive x-axis. Then the direction of propagation of electromagnetic wave is:

- (1) positive z-axis
- (2) positive y-axis
- (3) at 45° angle from positive y-axis
- (4) negative y-axis

Answer (4)

Sol. $\hat{C} = \hat{E} \times \hat{B}$

$\Rightarrow \hat{C}$ is along $-y$ axis

48. An electron is moving along the positive x-axis. If uniform magnetic field is applied parallel to the negative z-axis, then

- A. The electron will experience magnetic force along positive y-axis
- B. The electron will experience magnetic force along negative y-axis
- C. The electron will not experience any force in magnetic field
- D. The electron will continue to move along the positive x-axis
- E. The electron will move along circular path in magnetic field

Choose the correct answer from the option given below:

- | | |
|------------------|------------------|
| (1) A and E only | (2) C and D only |
| (3) B and E only | (4) B and D only |

Answer (3)

Sol. $\vec{F} = q\vec{v} \times \vec{B}$

$= -e\vec{v} \times \vec{B}$

$\Rightarrow \vec{F}$ along $-y$ axis

Also, motion would be circular.

49. Given below are two statements: one is labelled as **Assertion A** and the other is labelled as **Reason R**

Assertion A : The binding energy per nucleon is practically independent of the atomic number for nuclei of mass number in the range 30 to 170.

Reason R : Nuclear force is short ranged.

In the light of the above statements, choose the **correct** answer from the options given below

- (1) **A** is false but **R** is true
- (2) Both **A** and **R** are true and **R** is the correct explanation of **A**
- (3) Both **A** and **R** are true but **R** is **NOT** the correct explanation of **A**
- (4) **A** is true but **R** is false

Answer (2)

Sol. Binding energy per nucleon is almost constant in the mass number range 30 – 170. This is because nuclear force is a short-range force.

50. Given below are two statements:

Statement I : For a planet, if the ratio of mass of the planet to its radius increase, the escape velocity from the planet also increase.

Statement II : Escape velocity is independent of the radius of the planet.

In the light of above statements, choose the **most appropriate** answer from the options given below

- (1) Statement I is incorrect but Statement II is correct
- (2) Statement I is correct but statement II is incorrect
- (3) Both Statement I and Statement II are incorrect
- (4) Both Statement I and Statement II are correct

Answer (2)

Sol. $v_{\text{esc}} = \sqrt{\frac{2GM}{R}}$

\Rightarrow Statement I is correct while statement II is wrong.

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

51. Two plates A and B have thermal conductivities $84 \text{ Wm}^{-1}\text{K}^{-1}$ and $126 \text{ Wm}^{-1}\text{K}^{-1}$ respectively. They have same surface area and same thickness. They are placed in contact along their surfaces. If the temperatures of the outer surfaces of A and B are kept at 100°C and 0°C respectively, then the temperature of the surface of contact in steady state is _____ $^\circ\text{C}$.

Answer (40)

Sol.
$$\frac{84 \cdot A \cdot (100 - T)}{L} = \frac{126 \cdot A \cdot (T - 0)}{L}$$

$$\Rightarrow 200 - 2T = 3T$$

$$\Rightarrow T = 40^\circ\text{C}$$

52. An atom absorbs a photon of wavelength 500 nm and emits another photon of wavelength 600 nm . The net energy absorbed by the atom in this process is $n \times 10^{-4} \text{ eV}$. The value of n is _____. [Assume the atom to be stationary during the absorption and emission process] (Take $h = 6.6 \times 10^{-34} \text{ Js}$ and $c = 3 \times 10^8 \text{ m/s}$).

Answer (4125)

Sol.
$$\Delta E = \frac{hc}{\lambda_1} - \frac{hc}{\lambda_2}$$

$$= \frac{6.6 \times 10^{-34} \times 3 \times 10^8 \times 100}{500 \times 600 \times 10^{-9}}$$

$$= \frac{6.6 \times 3}{30} \times 10^{-19} \text{ J}$$

$$= \frac{6.6 \times 3}{30 \times 1.6} \text{ eV}$$

$$= \frac{6.6 \times 3 \times 10^4}{30 \times 1.6} \times 10^{-4} \text{ eV}$$

$$= 4125 \times 10^{-4} \text{ eV}$$

53. A bi convex lens of focal length 10 cm is cut in two identical parts along a plane perpendicular to the principal axis. The power of each lens after cut is _____ D .

Answer (5)

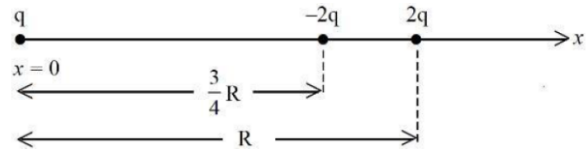
Sol.
$$\frac{1}{f} = (\mu - 1) \left(\frac{2}{R} \right)$$

$$\frac{1}{f'} = (\mu - 1) \left(\frac{1}{R} \right)$$

$$\Rightarrow \frac{P'}{P} = \frac{1}{2}$$

$$\Rightarrow P' = \frac{P}{2} = 5 \text{ D}$$

54. Three point charges q , $-2q$ and $2q$ are placed on x -axis at a distance $x = 0$, $x = \frac{3}{4}R$ and $x = R$ respectively from origin as shown. If $q = 2 \times 10^{-6} \text{ C}$ and $R = 2 \text{ cm}$, the magnitude of net force experienced by the charge $-2q$ is _____ N .



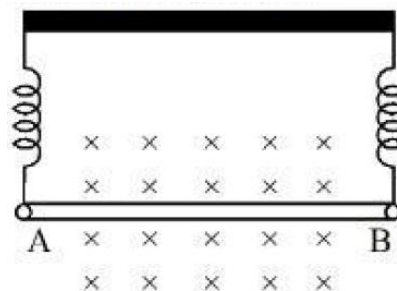
Answer (5440)

Sol.
$$\frac{1}{4\pi\epsilon_0} \frac{4q^2}{\left(\frac{R}{4}\right)^2} - \frac{1}{4\pi\epsilon_0} \frac{2q^2}{\left(\frac{3R}{4}\right)^2}$$

$$= 9 \times 10^9 \times \frac{16q^2}{R^2} \left[4 - \frac{2}{9} \right]$$

$$= \frac{9 \times 10^9 \times 16 \times 4 \times 10^{-12}}{4} \times \frac{34}{9} \text{ N} = 5440 \text{ N}$$

55. A straight wire AB of mass 40 g and length 50 cm is suspended by a pair of flexible leads in uniform magnetic field of magnitude 0.40 T as shown in the figure. The magnitude of the current required in the wire to remove the tension in the supporting leads is _____ A . (Take $g = 10 \text{ ms}^{-2}$).



Answer (2)

Sol. On current carrying wires

$$ILB = Mg$$

$$\Rightarrow I = \frac{\frac{40}{1000} \times 10}{0.5 \times 0.4} = 2 \text{ A}$$

56. In an experiment with sonometer when a mass of 180 g is attached to the string, it vibrates with fundamental frequency of 30 Hz. When a mass m is attached, the string vibrates with fundamental frequency of 50 Hz. The value of m is _____ g.

Answer (500)

Sol. $f = \frac{v}{2L} = \frac{1}{2L} \sqrt{\frac{T}{\mu}}$

$$\Rightarrow \frac{30}{50} = \sqrt{\frac{180}{m}}$$

$$\Rightarrow m = 180 \times \frac{25}{9} = 500 \text{ grams}$$

57. A light rope is wound around a hollow cylinder of mass 5 kg and radius 70 cm. The rope is pulled with a force of 52.5 N. The angular acceleration of the cylinder will be _____ rad s^{-2} .

Answer (15)

Sol. $\tau = I\alpha$

$$\Rightarrow \alpha = \frac{52.5 \times \frac{70}{100}}{5 \times \left(\frac{70}{100}\right)^2} = 10.5 \times \frac{10}{7}$$

$$= 15 \text{ rad/s}^2$$

58. A car accelerates from rest of u m/s. The energy spent in this process is E J. The energy required to accelerate the car from u m/s to $2u$ m/s is nE J. The value of n is _____.

Answer (3)

Sol. $E = \frac{1}{2}mv^2$... (1)

$$nE = \frac{1}{2}m\{(2v)^2 - v^2\}$$
 ... (2)

$$\Rightarrow n = 3$$

59. An insulated copper wire of 100 turns is wrapped around a wooden cylindrical core of the cross-sectional area 24 cm^2 . The two ends of the wire are connected to a resistor. The total resistance in the circuit is 12Ω . If an externally applied uniform magnetic field in the core along its axis changes from 1.5 T in one direction to 1.5 T in the opposite direction, the charge flowing through a point in the circuit during the change of magnetic field will be _____ mC.

Answer (60)

Sol. $\varepsilon = \frac{-d\theta}{dt} = iR$

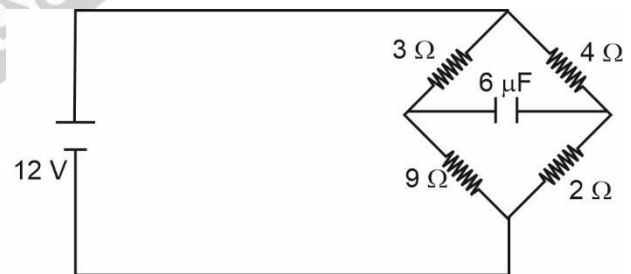
$$\Rightarrow \int idt = \frac{-\Delta\phi}{R}$$

$$\Rightarrow -\frac{1}{R} [2 \times 1.5 \times 24 \times 10^{-4}] \times 100 \text{ C}$$

$$\Rightarrow \text{Charge} = \frac{0.72}{12} \text{ C}$$

$$= 60 \text{ mC}$$

60. In the circuit shown, the energy stored in the capacitor is $n \mu\text{J}$. The value of n is _____.



Answer (75)

Sol. Capacitor would behave as open circuit.

$$\Delta V_C = \left(\frac{4}{6} \times 12 - \frac{3}{12} \times 12 \right) \text{ volts}$$

$$= (8 - 3) \text{ V} = 5 \text{ V}$$

$$\Rightarrow U = \frac{1}{2}C(5)^2$$

$$= 75 \mu\text{J}$$

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

61. Match List-I with List-II.

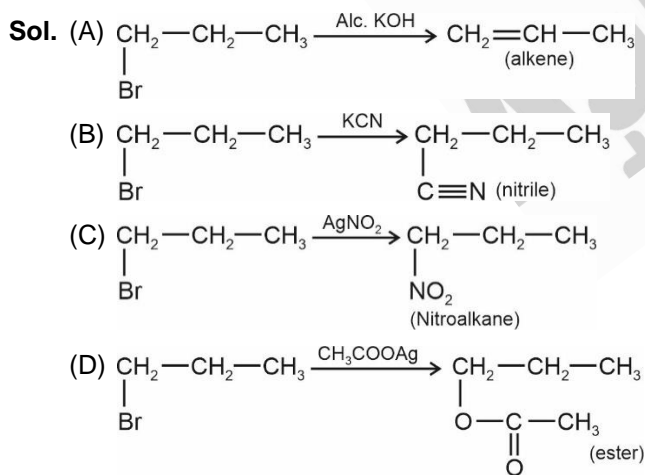
1-Bromopropane is reacted with reagents in List-I to give product in List-II

	List-I Reagent		List-II Product
A.	KOH (alc)	I.	Nitrile
B.	KCN (alc)	II.	Ester
C.	AgNO ₂	III.	Alkene
D.	H ₃ CCOOAg	IV.	Nitroalkane

Choose the correct answer from the options given below

- (1) A-III, B-I, C-IV, D-II (2) A-I, B-II, C-III, D-IV
(3) A-I, B-III, C-IV, D-II (4) A-IV, B-III, C-II, D-I

Answer (1)



62. In the wet tests for detection of various cations by precipitation, Ba²⁺ cations are detected by obtaining precipitate of

- (1) Ba(ox) : Barium oxalate
(2) BaCO₃
(3) Ba(OAc)₂
(4) BaSO₄

Answer (2)

Sol. Ba²⁺ belongs to Vth Group and hence they are precipitated with CO₃²⁻ to give ppt of BaCO₃.

63. Match Lis-I with List-II.

	List-I		List-II
A.	Weak intermolecular forces of attraction	I.	Hexamethylenediamine + adipic acid
B.	Hydrogen bonding	II.	AlEt ₃ + TiCl ₄
C.	Heavily branched polymer	III.	2-chloro-1, 3-butadiene
D.	High density polymer	IV.	Phenol + formaldehyde

Choose the correct answer from the options given below

- (1) A-IV, B-II, C-III, D-I (2) A-IV, B-I, C-III, D-II
(3) A-II, B-IV, C-I, D-III (4) A-III, B-I, C-IV, D-II

Answer (4)

Sol. (A) Weak Intermolecular Forces are present in polymer of 2-chloro, 1, 3-butadiene
(B) Hydrogen Bonding is present in NYLON-66 which is a polymer of Hexamethylenediamine and adipic acid
(C) Heavily branched polymer is Bakelite which is polymer of phenol and formaldehyde
(D) High density polymer preparation requires AL(Et)₃ and TiCl₄ as a catalyst (Ziegler Natta Catalyst)

64. The covalency and oxidation state respectively of boron in [BF₄]⁻, are

- (1) 3 and 5 (2) 3 and 4
(3) 4 and 4 (4) 4 and 3

Answer (4)

Sol. $[\text{BF}_4]^-$

Covalency = No. of Bonds = 4

Oxidation state = +3 for Boron

65. Identify the correct order of standard enthalpy of formation of sodium halides.

(1) $\text{NaI} < \text{NaBr} < \text{NaF} < \text{NaCl}$

(2) $\text{NaI} < \text{NaBr} < \text{NaCl} < \text{NaF}$

(3) $\text{NaF} < \text{NaCl} < \text{NaBr} < \text{NaI}$

(4) $\text{NaCl} < \text{NaF} < \text{NaBr} < \text{NaI}$

Answer (2)

Sol. Lattice energy $\propto \frac{1}{(r_+ + r_-)}$

Size \uparrow Enthalpy of formation \downarrow

Order :

$\text{NaF} > \text{NaCl} > \text{NaBr} > \text{NaI}$

66. What happens when methane undergoes combustion in systems A and B respectively?

Adiabatic system

Diathermic container

System A

System B

	System A	System B
(1)	Temperature rises	Temperature remains same
(2)	Temperature remains same	Temperature rises
(3)	Temperature falls	Temperature remains same
(4)	Temperature falls	Temperature rises

Answer (1)

Sol. For adiabatic system, heat will not escape and temperature of system will rise.

For diathermic container, heat will escape the container and hence temperature of container will remain same.

67. Which of the following complexes will exhibit maximum attraction to an applied magnetic field?

(1) $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$

(2) $[\text{Co}(\text{en})_3]^{3+}$

(3) $[\text{Zn}(\text{H}_2\text{O})_6]^{2+}$

(4) $[\text{Co}(\text{H}_2\text{O})_6]^{2+}$

Answer (4)

Sol. Complex having maximum number of unpaired electrons will exhibit maximum attraction to applied magnetic field.

$[\text{Ni}(\text{H}_2\text{O})_6]^{2+} = 2$ unpaired electrons

$[\text{Co}(\text{en})_3]^{3+} = 0$ unpaired electrons

$[\text{Zn}(\text{H}_2\text{O})_6]^{2+} = 0$ unpaired electrons

$[\text{Co}(\text{H}_2\text{O})_6]^{2+} = 3$ unpaired electrons

68. Given below are two statements, one is labelled as **Assertion A** and the other is labelled as **Reason R**.

Assertion A : The diameter of colloidal particles in solution should not be much smaller than wavelength of light to show Tyndall effect.

Reason R : The light scatters in all directions when the size of particles is large enough.

In the light of the above statements, choose the correct answer from the options given below :

(1) Both A and R are correct but R is NOT the correct explanation of A

(2) A is true but R is false

(3) A is false but R is true

(4) Both A and R are correct and R is the correct explanation of A

Answer (4)

Sol. Conditions for Tyndall effect:

(i) Diameter of colloidal particles in solution is not much smaller than wavelength of the light used.

(ii) The refractive indices of the dispersed phase and dispersion medium differ greatly in magnitude.

If size of particles is large enough than light scatters in all directions.

69. Given below are two statements, one is labelled as **Assertion A** and the other is labelled as **Reason R**.

Assertion A : Isotopes of hydrogen have almost same chemical properties, but difference in their rates of reactions.

Reason R: Isotopes of hydrogen have different enthalpy of bond dissociation.

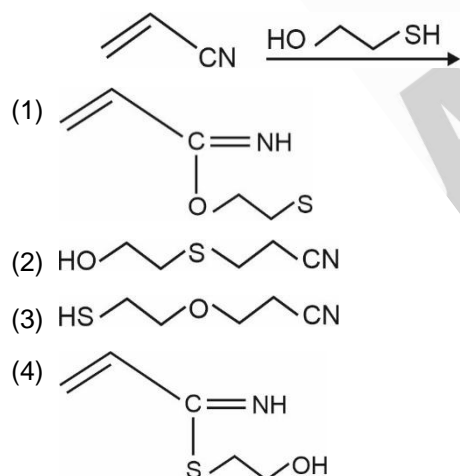
In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Both A and R are correct but R is NOT the correct explanation of A
- (2) Both A and R are correct and R is the correct explanation of A
- (3) A is not correct but R is correct
- (4) A is correct but R is not correct

Answer (2)

Sol. Isotopes of hydrogen have almost same chemical properties, but rate will be different due to difference in bond dissociation enthalpy.

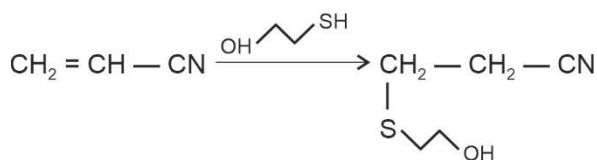
70. The major product for the following reaction is :



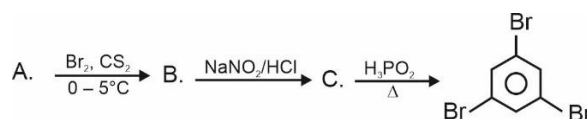
Answer (2)

Sol. Nucleophilicity: SH > OH

Stable carbocation will be that which is away from CN group.

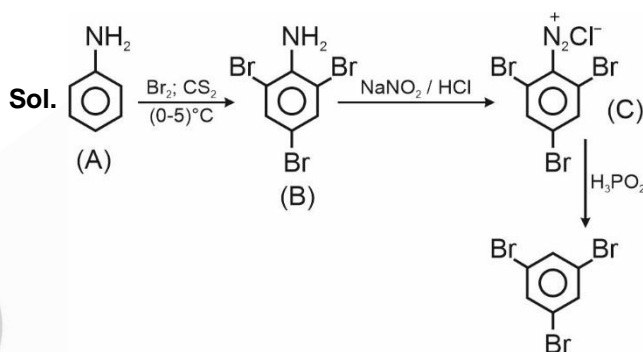


71. Compound A from the following reaction sequence is :



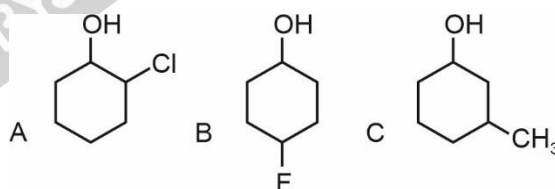
- (1) Benzoic Acid
- (2) Aniline
- (3) Salicylic Acid
- (4) Phenol

Answer (2)



72. Given below are two statements, one is labelled as **Assertion A** and the other is labelled as **Reason R**.

Assertion A : Order of acidic nature of the following compounds is A > B > C.



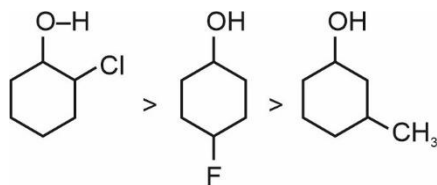
Reason R: Fluoro is a stronger electron withdrawing group than Chloro group.

In the light of the above statements, choose the correct answer from the options given below :

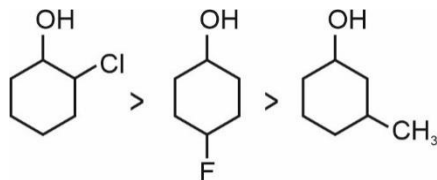
- (1) A is false but R is true
- (2) Both A and R are correct and R is the correct explanation of A
- (3) A is true but R is false
- (4) Both A and R are correct but R is NOT the correct explanation of A

Answer (4)

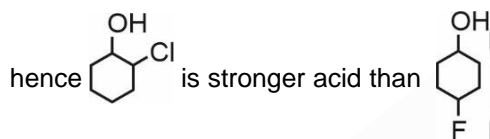
Sol. The F & Cl are electron withdrawing while CH₃ is electron loosing hence acidic strength will be



On further differentiation the – I effect depends most importantly over distance hence.



The F has higher –I effect as compared to Cl hence reason is correct statement but the –I effect depends more on distance as compared to power



73. The correct group of halide ions which can be oxidised by oxygen in acidic medium is

- (1) Br[–] and I[–] only
- (2) Br[–] only
- (3) I[–] only
- (4) Cl[–], Br[–] and I[–] only

Answer (3)

Sol. Fluorine oxidises water to oxygen whereas chlorine & bromine react with water to form corresponding HX & HOX acids. The reaction of I₂ with water is nonspontaneous. In fact I[–] can be oxidised by oxygen in acidic medium.

It is why the I[–] in nature is not present in that much amount as other halides are present in nature.

74. Given below are two statements :

Statement I : SO₂ and H₂O both possess V-shaped structure.

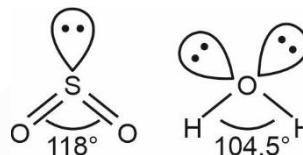
Statement II : The bond angle of SO₂ is less than that of H₂O.

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Both Statement I and Statement II are incorrect
- (2) Both Statement I and Statement II are correct
- (3) Statement I is incorrect but Statement II is correct
- (4) Statement I is correct but Statement II is incorrect

Answer (4)

Sol.



SO₂ and H₂O both have V-Shape

Bond angle: SO₂ > H₂O

75. Better method for preparation of BeF₂, among the following is

- (1) BeO + C + F₂ $\xrightarrow{\Delta}$ BeF₂
- (2) (NH₄)₂BeF₄ $\xrightarrow{\Delta}$ BeF₂
- (3) Be + F₂ $\xrightarrow{\Delta}$ BeF₂
- (4) BeH₂ + F₂ $\xrightarrow{\Delta}$ BeF₂

Answer (2)

Sol. (NH₄)₂BeF₄ \longrightarrow 2NH₄F + BeF₂

76. Given below are two statements :

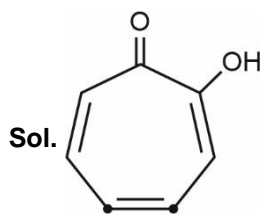
Statement I : Tropolone is an aromatic compound and has 8 π electrons.

Statement II : π electrons of >C = O group in tropolone is involved in aromaticity.

In the light of the above statements choose the correct answer from the options given below:

- (1) Statement I is true but Statement II is false
- (2) Statement I is false but Statement II is true
- (3) Both Statement I and Statement II are false
- (4) Both Statement I and Statement II are true

Answer (1)



Tropolone has 8π electrons

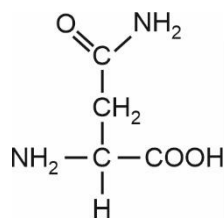
π -electrons of group does not get involved in aromaticity.

77. The naturally occurring amino acid that contains only one basic functional group in its chemical structure is
- (1) asparagine (2) histidine
 (3) arginine (4) lysine

Answer (1)

Sol. Asparagine have only one Basic Functional Group

Structure of Asparagine:



78. Given below are two statements related to Ellingham diagram :

Statement I : Ellingham diagrams can be constructed for formation of oxides, sulfides and halides of metals.

Statement II : It consists of plots of $\Delta_f H^\circ$ vs T for formation of oxides of elements.

In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) Both Statement I and Statement II are correct
 (2) Both Statement I and Statement II are incorrect
 (3) Statement I is correct but Statement II is incorrect
 (4) Statement I is incorrect but Statement II is correct

Answer (3)

Sol. Ellingham diagram have plot of ΔG_f° vs. temperature

79. Which of the following are the Green house gases?
- A. Water vapour
 B. Ozone
 C. I_2
 D. Molecular hydrogen

Choose the most appropriate answer from the options given below :

- (1) A and D only (2) B and C only
 (3) A and B only (4) C and D only

Answer (3)

Sol. I_2 and H_2 are not green house gases.

80. The total number of stereoisomers for the complex $[Cr(ox)_2ClBr]^{3-}$ (where ox = oxalate) is

- (1) 3 (2) 2
 (3) 4 (4) 1

Answer (1)

Sol. $\frac{\text{Cis}-2}{\text{trans}-1}$

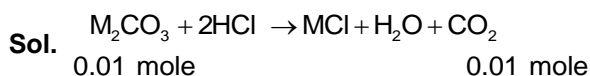
Total 3 stereoisomers.

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

81. 1g of a carbonate (M_2CO_3) on treatment with excess HCl produces 0.01 mol of CO_2 . The molar mass of M_2CO_3 is _____ g mol⁻¹. (Nearest integer)

Answer (100)



$$\Rightarrow \frac{1}{MW} = 0.01$$

$$MW = 100 \left(\frac{\text{gm}}{\text{mole}} \right)$$

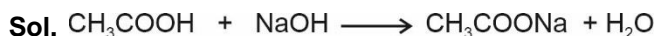
82. 20 mL of 0.1 M NaOH is added to 50 mL of 0.1 M acetic acid solution. The pH of the resulting solution is _____ $\times 10^{-2}$. (Nearest integer)

Given : $pK_a(\text{CH}_3\text{COOH}) = 4.76$

$$\log 2 = 0.30$$

$$\log 3 = 0.48$$

Answer (458)



$$\text{pH} = \text{p}K_a + \log\left(\frac{2}{3}\right)$$

$$\text{pH} = 4.76 + 0.30 - 0.48$$

$$= 4.76 - .18$$

$$= 4.58$$

83. If the formula of Borax is $\text{Na}_2\text{B}_4\text{O}_x(\text{OH})_y \cdot z\text{H}_2\text{O}$, then $x + y + z =$ _____

Answer (17)

Sol. Borax is $\text{Na}_2[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 8\text{H}_2\text{O}$

$$\frac{x}{y} = \frac{5}{4}$$

$$\frac{y}{z} = \frac{4}{8}$$

$$(x + y + z) = 5 + 4 + 8 = 17$$

84. At 298 K, the standard reduction potential for Cu^{2+}/Cu electrode is 0.34 V.

Given : $K_{sp} \text{Cu}(\text{OH})_2 = 1 \times 10^{-20}$

$$\text{Take } \frac{2.303 RT}{F} = 0.059 \text{ V}$$

The reduction potential at $\text{pH} = 14$ for the above couple is $(-x) \times 10^{-2}$ V.

The value of x is

Answer (25)

Sol. $K_{sp} = 10^{-20} = (\text{Cu}^{2+})(1)^2$

$$[\text{Cu}^{2+}] = 10^{-20}$$

$$E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{0.059}{2} \log 10^{20}$$

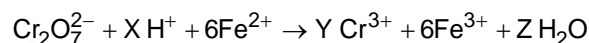
$$E_{\text{cell}} = 0.34 - \frac{0.059}{2} (20)$$

$$= 0.34 - 0.59$$

$$= -0.25$$

$$x = 25$$

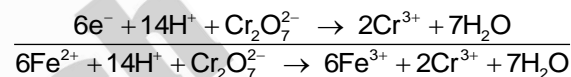
85. See the following chemical reaction:



The sum of X, Y and Z is

Answer (23)

Sol. $(\text{Fe}^{2+} \rightarrow \text{Fe}^{3+} + e^-) \times 6$



$$\underline{X = 14}$$

$$\underline{Y = 2}$$

$$\underline{Z = 7}$$

$$(X + Y + Z) = 14 + 2 + 7$$

$$= 23$$

86. The orbital angular momentum of an electron in 3s

orbital is $\frac{xh}{2\pi}$. The value of x is _____ (nearest

integer)

Answer (0)

Sol. Orbital angular Momentum

$$\sqrt{\ell(\ell+1)} \frac{h}{2\pi}$$

For s-orbital $\ell = 0$

Orbital angular momentum for s-orbital = 0

87. Sodium metal crystallizes in a body centred cubic lattice with unit cell edge length of 4 Å. The radius of sodium atom is _____ $\times 10^{-1}$ Å. (Nearest integer)

Answer (17)

Sol. $a\sqrt{3} = 4r$

$$4 \times \sqrt{3} = 4 \times r$$

$$r = \sqrt{3} \text{ \AA} = 1.73 \text{ \AA}$$

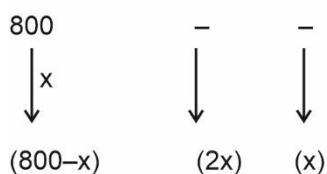
$$1.73 = t \times 10^{-1}$$

$$t = 17.3$$

$$\text{Closest integer} = 17$$

88. $A(g) \rightarrow 2B(g) + C(g)$ is a first order reaction. The initial pressure of the system was found to be 800 mm Hg which increased to 1600 mm Hg after 10 min. The total pressure of the system after 30 min will be _____ mm Hg. (Nearest integer)

Answer (2200)



$$800 + 2x = 1600$$

$$2x = 800$$

$$x = 400$$

$$K = \frac{2.303}{10} \log \frac{800}{400} = \frac{2.303 \times \log 2}{10}$$

For 30 min,

$$K = \frac{2.303}{30} \log \frac{(800)}{(800-y)}$$

$$\frac{2.303 \times \log 2}{10} = \frac{2.303}{30} \log \left(\frac{800}{800-y} \right)$$

$$\Rightarrow \left(\frac{800}{800-y} \right) = 8$$

$$100 = 800 - y$$

$$y = 700$$

Total pressure after 30 min

$$(800 - y) + (2y) + (y)$$

$$= 800 + 2y$$

$$= 800 + 1400$$

$$= 2200 \text{ mm Hg}$$

89. Sea water contains 29.25% NaCl and 19% $MgCl_2$ by weight of solution. The normal boiling point of the sea water is _____ °C (Nearest integer)

Assume 100% ionization for both NaCl and $MgCl_2$

Given: $K_b(H_2O) = 0.52 \text{ K kg mol}^{-1}$

Molar mass of NaCl and $MgCl_2$ is 58.5 and 95 g mol^{-1} respectively.

Answer (116)

Sol. Molality of solutions

$$\text{NaCl} = \frac{0.5}{51.75} \times 1000$$

$$\text{MgCl}_2 = \frac{0.2}{51.75} \times 1000$$

$$(\Delta T_b) = \{(i_1 m_1) + (i_2 m_2)\} k_b$$

$$\left(\frac{2 \times 0.5 \times 1000}{51.75} + \frac{3 \times 0.2 \times 1000}{51.75} \right) \times 0.52$$

$$= 16.077$$

Boiling point of sea water

$$= 116.077^\circ\text{C}$$

$$\approx 116^\circ\text{C} \text{ (Nearest integer)}$$

90. 0.400 g of an organic compound (X) gave 0.376 g of AgBr in Carius method for estimation of bromine.

% of bromine in the compound (X) is _____.

(Given: Molar mass AgBr = 188 g mol^{-1})

Br = 80 g mol^{-1})

Answer (40)

Sol. Moles of AgBr = $\frac{0.376}{188}$

$$\text{Moles of Br} = \frac{0.376}{188}$$

$$\text{Mass of Br} = \frac{0.376}{188} \times 80$$

$$\% \text{ of Br} = \frac{0.376 \times 80}{188 \times (0.400)} \times 100$$

$$= 40\%$$

