

EX NAVODAYAN FOUNDATION

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01/02/2023 Evening

Answers & Solutions

for

Time : 3 hrs.

M.M.: 300

JEE (Main)-2023 (Online) Phase-1

(Physics, Chemistry and Mathematics)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) The Test Booklet consists of 90 questions. The maximum marks are 300.
- (3) There are three parts in the question paper consisting of Physics, Chemistry and Mathematics having 30 questions in each part of equal weightage. Each part (subject) has two sections.
 - (i) **Section-A:** This section contains 20 multiple choice questions which have only one correct answer. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer.
 - Section-B: This section contains 10 questions. In Section-B, attempt any five questions out of 10. The answer to each of the questions is a numerical value. Each question carries 4 marks for correct answer and -1 mark for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

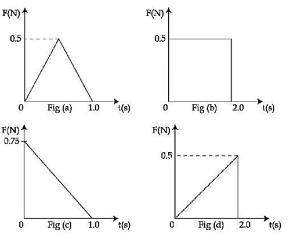
PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. Figures (a), (b), (c) and (d) show variation of force with time.



The impulse is highest in

- (1) Fig. (d) (2) Fig. (c)
- (3) Fig. (b) (4) Fig. (a)

Answer (3)

Sol. Impulse ∞ area under (*F*-*t*) graph.

Impulse for graph (b) is maximum.

 Given below are two statements: One is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : Two metallic spheres are charged to the same potential. One of them is hollow and another is solid, and both have the same radii. Solid sphere will have lower charge than the hollow one.

Reason R: Capacitance of metallic spheres depend on the radii of spheres.

In the light of the above statements, choose the correct answer from the options given below:

- (1) Both **A** and **R** are true but **R** is **not** the correct explanation of **A**
- (2) A is false but R is true
- (3) Both **A** and **R** are true but **R** is the correct explanation of **A**
- (4) **A** is true but **R** is false

Answer (2)

Sol. Assertion (A) is incorrect

Both spheres will have same charge.

Reason (R) is correct.

- A coil is placed in magnetic field such that plane of coil is perpendicular to the direction of magnetic field. The magnetic flux through a coil can be changed:
 - A. By changing the magnitude of the magnetic field within the coil.
 - B. By changing the area of coil within the magnetic field.
 - C. By changing the angle between the direction of magnetic field and the plane of the coil.
 - D. By reversing the magnetic field direction abruptly without changing its magnitude.

Choose the most appropriate answer from the options given below:

(1) A and B only	(2) A, B and D only
(3) A and C only	(4) A, B and C only

Answer (4)

- **Sol.** Flux can be changed by changing magnetic field, area of coil, change the angle between *B* and *A*.
- An electron of a hydrogen like atom, having Z = 4, jumps from 4th energy state to 2nd energy state. The energy released in this process, will be:

(Given Rch = 13.6 eV)

Where R = Rydberg constant, c = Speed of light in vacuum, h = Planck's constant)

(1) 3.4 eV	(2) 10.5 eV
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(3) 40.8 eV (4)) 13.6 eV
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Answer (3)

Sol.
$$E = 13.6Z^2 \left\lfloor \frac{1}{2^2} - \frac{1}{4^2} \right\rfloor^2$$

= 13.6 × 16 × $\left\lfloor \frac{1}{4} - \frac{1}{16} \right\rfloor^2$
= 40.8 eV

 Given below are two statements: One is labelled as Assertion A and the other is labelled as Reason R.

Assertion A: For measuring the potential difference across a resistance of 600 Ω , the voltmeter with resistance 1000 Ω will be preferred over voltmeter with resistance 4000 Ω .

Reason R: Voltmeter with higher resistance will draw smaller current than voltmeter with lower resistance.

In the light of the above statements, choose the **most appropriate** answer from the options given below:

- (1) Both **A** and **R** are correct but **R** is **not** the correct explanation of **A**
- (2) Both **A** and **R** are correct but **R** is the correct explanation of **A**
- (3) A is not correct but R is correct
- (4) A is correct but R is not correct

Answer (3)

Sol. (A) is not correct because we need higher voltmeter resistance.

(R) is correct based on reason given above.

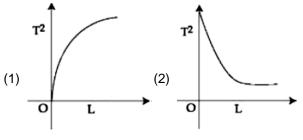
- 6. Choose the correct statement about Zener diode
 - (1) It works as a voltage regulator only in forward bias
 - (2) It works as a voltage regulator in forward bias and behaves like simple pn junction diode in reverse bias.
 - (3) It works as a voltage regulator in both forward and reverse bias.
 - (4) It works as a voltage regulator in reverse bias and behaves like simple pn junction diode in forward bias.

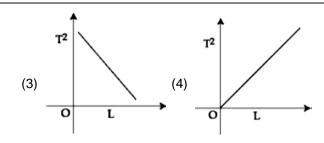
Answer (4)

Sol. Theoretical.

 \because Zener diode is a voltage regulator in reverse bias and behaves as simple pn junction diode in forward bias.

 Choose the correct length (L) versus square of time period (T²) graph for a simple pendulum executing simple harmonic motion.





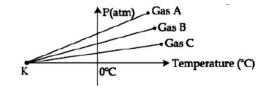
Answer (4)

Sol.
$$T^2 = \frac{(2\pi)^2 L}{g}$$

 $y = \frac{(2\pi)^2 x}{g}$ (y axis has T^2 & x axis has L)

: Straight line

8. For three low density gases A, B, C pressure versus temperature graphs are plotted while keeping them at constant volume, as shown in the figure.



The temperature corresponding to the point 'K' is

(1) –373°C	(2) –273°C
(3) –40°C	(4) –100°C

Answer (2)

Sol. *PV* = *nRT*

At constant volume

 $P \propto T \Rightarrow$ straight line and absolute zero is the common intercept, $T = -273^{\circ}$ C

9. A Carnot engine operating between two reservoirs has efficiency $\frac{1}{3}$. When the temperature of cold

reservoir raised by x, its efficiency decreases to $\frac{1}{6}$.

The value of x, if the temperature of hot reservoir is 99°C, will be

(1) 66 K	(2) 33 K
(3) 62 K	(4) 16.5 K

Answer (3)

Sol.
$$\eta = 1 - \frac{I_C}{T_H}$$

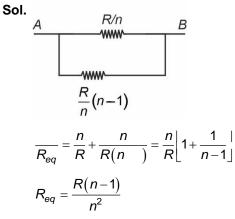
Initially $\frac{T_C}{T_H} = \frac{2}{3}$ (1)
Finally $\frac{T_{C+x}}{T_H} = \frac{5}{6}$ (2)
 $T_H = 99^{\circ}C = 372 \text{ K}$
 $\therefore x = 62 \text{ K}$

10. Equivalent resistance between the adjacent corners of a regular n-sided polygon of uniform wire of resistance R would be

(1)
$$\frac{(n-1)R}{(2n-1)}$$
 (2) $\frac{(n-1)R}{n^2}$
(3) $\frac{(n-1)R}{n}$ (4) $\frac{n^2R}{n-1}$

Answer (2)



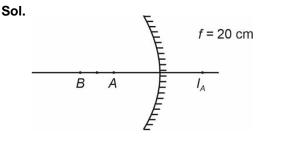


11. Two objects *A* and *B* are placed at 15 cm and 25 cm from the pole in front of a concave mirror having radius of curvature 40 cm. The distance between images formed by the mirror is

(1)	100 cm	(2)	40 cm

(3)	160 cm	(4)	60 cm
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Answer (3)



$$I_A \Rightarrow \frac{1}{v} - \frac{1}{15} = -\frac{1}{20}$$

$$v = 60 \text{ (+ ve, virtual)}$$

$$I_B \Rightarrow \frac{1}{v} - \frac{1}{25} = -\frac{1}{20}$$

v = -100 (- ve, real)

distance b/w images $I_A - I_B = 60 - (-100)$

= 160 cm

- 12. For a body projected at an angle with the horizontal from the ground, choose the correct statement.
 - The horizontal component of velocity is zero at the highest point.
 - (2) The vertical component of momentum is maximum at the highest point.
 - (3) Gravitational potential energy is maximum at the highest point
 - (4) The Kinetic Energy (K.E.) is zero at the highest point of projectile motion.

Answer (3)



At highest point $KE = \frac{1}{2}mv^2\cos^2\theta \neq 0$

horizontal momentum = $mv \cos\theta \neq 0$

vertical momentum = 0

PE = mgh (Max at maximum height)

13. The threshold frequency of a metal is f_0 . When the light of frequency $2f_0$ is incident on the metal plate, the maximum velocity of photoelectrons is v_1 . When the frequency of incident radiation is increases to $5f_0$, the maximum velocity of photoelectrons emitted is v_2 . The ratio of v_1 to v_2 is:

(1)
$$\frac{v_1}{v_2} = \frac{1}{2}$$
 (2) $\frac{v_1}{v_2} = \frac{1}{4}$

$$\frac{v_1}{v_2} = \frac{1}{8}$$
 (4) $\frac{v_1}{v_2} = \frac{1}{16}$

Answer (1)

(3)

Sol.
$$\frac{1}{2}mv^2 = hf - hf_0$$

 $\Rightarrow \frac{1}{2}mv_1^2 = 2hf_0 - hf_0 = hf_0$...(1)
also, $\frac{1}{2}mv_2^2 = 5hf_0 - hf_0 = 4hf_0$...(2)

taking ratio,

- $\frac{v_1^2}{v_2^2} = \frac{1}{4} \Longrightarrow \frac{v_1}{v_2} = \frac{1}{2}$
- 14. The escape velocities of two planets *A* and *B* are in the ratio 1 : 2. If the ratio of their radii respectively is 1 : 3, then the ratio of acceleration due to gravity of planet *A* to the acceleration of gravity of planet *B* will be:

(1)	2 3	(2)	$\frac{4}{3}$
(3)	$\frac{3}{2}$	(4)	$\frac{3}{4}$

Answer (4)

Sol. $V_e = \sqrt{2gR}$ $\frac{(V_e)_A}{(V_e)_B} = \sqrt{\frac{g_A R_A}{g_B R_B}}$ $\Rightarrow - = \left(\frac{g_A}{g_B}\right) \times \frac{1}{3}$ $\frac{g_A}{g_B} = \left(\frac{3}{4}\right)$

15. The ratio of average electric energy density and total average energy density of electromagnetic wave is

(1) 3 (2) 2

(3) 1 (4) $\frac{1}{2}$

Answer (4)

Sol. Average electric energy density = $\frac{1}{4}\varepsilon_0 E_0^2$

Average energy density = $\frac{1}{2}\varepsilon_0 E_0^2$

Ratio of electric average energy density to the average energy density = $\left(\frac{1}{2}\right)$.

16. In an amplitude modulation, a modulating signal having amplitude of X V is superimposed with a carrier signal of amplitude Y V in first case. Then, in second case, the same modulating signal is superimposed with different carrier signal of amplitude 2Y V. The ratio of modulation index in the two cases respectively will be:

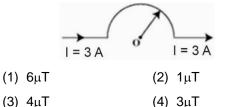
Answer (1)

Sol. μ = modulation index

$$\mu_{1} = \frac{A_{m}}{A_{c_{1}}} = \left(\frac{X}{Y}\right)$$
$$\mu_{2} = \frac{A_{m}}{A_{c_{2}}} = \left(\frac{X}{2Y}\right)$$
$$\Rightarrow \frac{\mu_{1}}{\mu_{2}} = \frac{\left(\frac{X}{Y}\right)}{\left(\frac{X}{2Y}\right)} = 2:1$$

17. As shown in the figure, a long straight conductor with semicircular arc of radius $\frac{\pi}{10}$ m is carrying current I = 3 A. The magnitude of the magnetic field at the center O of the arc is:

(The permeability of the vacuum = $4\pi \times 10^{-7} \text{ NA}^{-2}$)



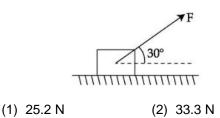
Answer (4)

Sol.

Magnetic field at *B* will be only due to the semicircular arc.

So,
$$B = \left(\frac{\mu_0 i}{4r}\right) = \frac{\left(4\pi \times 10^{-7}\right) \times 3}{4 \times \left(\frac{\pi}{10}\right)}$$
$$= 3 \times 10^{-6} \text{ T}$$
$$= 3 \,\mu\text{T}$$

18. As shown in the figure a block of mass 10 kg lying on a horizontal surface is pulled by a force F acting at an angle 30°, with horizontal. For $\mu_s = 0.25$, the block will just start to move for the value of $F : [Given g = 10 ms^{-2}]$



(4) 35.7 N

F

...(i)

(3) 20 N

Answer (1)

Sol.

$$\mu_{s} = 0.25$$

$$F \cos 30^{\circ} = \mu N$$

$$N = (1 \ g - F \sin 30^\circ) = (100 - \frac{F}{2})$$
 ...(ii)

On solving (i) and (ii)

$$\Rightarrow \frac{\sqrt{3}}{2} F = 0.25 \left(100 - \frac{F}{2} \right)$$
$$\Rightarrow \left(\frac{\sqrt{3}}{2} + \frac{1}{8} \right) F = 25$$
$$F = \frac{25 \times 8}{\left(1 + 4\sqrt{3} \right)} = \frac{200}{\left(4\sqrt{3} + 1 \right)} N$$
$$= 25.22 N$$

19. The Young's modulus of a steel wire of length 6 m and cross-sectional area 3 mm², is 2×10^{11} N/m². The wire is suspended from its support on a given planet. A block of mass 4 kg is attached to the free end of the wire. The acceleration due to gravity on the planet is $\frac{1}{4}$ of its value on the earth. The elongation of wire is (Take g on the earth = 10 m/s^2):

(1) 0.1 cm	(2) 0.1 mm
(3) 1 mm	(4) 1 cm

Sol.
$$\Delta I = \frac{FL}{AY} = \frac{\frac{Mg}{4} \times L}{AY}$$
$$= \frac{\frac{4 \times 10}{4} \times 6}{3 \times 10^{-6} \times 2 \times 10^{11}}$$
$$= \frac{60}{6 \times 10^5} = 10^{-4} \text{ m} = 0.1 \text{ mm}$$

20. If the velocity of light c, universal gravitational constant G and Planck's constant h are chosen as fundamental quantities. The dimensions of mass in the new system is:

(1)
$$\left[h^{\frac{1}{2}}c^{\frac{1}{2}}G^{-\frac{1}{2}}\right]$$
 (2) $\left[h^{\frac{1}{2}}c^{-\frac{1}{2}}G^{1}\right]$
(3) $\left[h^{-\frac{1}{2}}c^{\frac{1}{2}}G^{\frac{1}{2}}\right]$ (4) $\left[h^{1}c^{1}G^{-1}\right]$

Answer (1)

Sol.
$$c = LT^{-1}$$

 $G = M^{-1}L^{3}T^{-2}$
 $h = ML^{2}T^{-1}$
Let $M = c^{x} G^{y} h^{z}$
 $\Rightarrow M^{1}L^{0}T^{0} = M^{z-y} L^{x+3y+2z} T^{-x-2y-z}$
 $\Rightarrow x + 2y + z = 0$...(i)
 $x + 3y + 2z = 0$...(ii)
 $z - y = 1$...(iii)
 $\Rightarrow x = \frac{1}{2}, y = \frac{-1}{2}, z = \frac{1}{2}$
 $\Rightarrow M = c^{1/2} G^{-1/2} h^{1/2}$

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a NUMERICAL VALUE. For each question, enter the numerical value decimal correct (in notation. truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. A force $F = (5 + 3y^2)$ acts on a particle in the ydirection, where F is in newton and y is in meter. The work done by the force during a displacement from y = 2m to y = 5m is _____ J.

Answer (132)

Sol.
$$W = \int F \, dy = \int_{2}^{5} (5+3y^2) \, dy$$

= $(5y+y^3)\Big|_{2}^{5}$
= $(15+125-8) \, J$
= $132 \, J$

22. A block is fastened to a horizontal spring. The block is pulled to a distance x = 10 cm from its equilibrium position (at x = 0) on a frictionless surface from rest. The energy of the block at x = 5 cm is 0.25 J. The spring constant of the spring is _____ Nm⁻¹.

Answer (50)

Sol.
$$\frac{1}{2}kx^2 = 0.25 \text{ J}$$

 $\Rightarrow k = \frac{0.25 \times 2}{(0.01)} = (50 \text{ N/m})$

23. A square shaped coil of area 70 cm² having 600 turns rotates in magnetic field of 0.4 Wbm⁻², about an axis which is parallel to one of the side of the coil and perpendicular to the direction of field. If the coil completes 500 revolution in a minute, the instantaneous emf when the plane of the coil is inclined at 60° with the field, will be ______V.

(Take
$$\pi = \frac{22}{7}$$
)

Answer (44)

Sol. $\phi = BA \cos \omega t$

$$\varepsilon = -\frac{d\phi}{dt} = +BA\omega \sin \omega t$$
$$= 0.4 \times 600 \times \frac{70}{10^4} \times \frac{500 \times 2}{60} \sin 30^\circ$$
$$= \frac{0.4 \times 6 \times 7}{600} \times 500 \times \frac{44}{7} \times \frac{1}{2} = 44 \text{ volts}$$

24. For a train engine moving with speed of 20 ms⁻¹, the driver must apply brakes at a distance of 500 m before the station for the train to come to rest at the station. If the brakes were applied at half of this distance, the train engine would cross the station with speed \sqrt{x} ms⁻¹. The value of x is

(Assuming same retardation is produced by brakes)

Answer (200)

Sol. Distance up to the station = 250 m
Also
$$0^2 - 20^2 = 2(a) (500)$$

 $\Rightarrow a = \frac{-}{1000} = -0.4 \text{ m/s}^2$
 $\Rightarrow v^2 - 20^2 = 2(-0.4) (250)$
 $\Rightarrow v^2 - 400 - 200$
 $\Rightarrow v = \sqrt{200} \text{ m/s}$
 $\Rightarrow x = 200$

25. Nucleus A having Z = 17 and equal number of protons and neutrons has 1.2 MeV binding energy per nucleon.

Another nucleus B of Z = 12 has total 26 nucleons and 1.8 MeV binding energy per nucleons.

The difference of binding energy of B and A will be _____ MeV.

Answer (6)

Sol.
$$BE_A = (17 + 17)1.2 \text{ MeV} = 40.8 \text{ MeV}$$

 $BE_B = 26 \times 1.8 \text{ MeV} = 46.8 \text{ MeV}$

 $BE_B - BE_A = 6 \text{ MeV}$

26. A cubical volume is bounded by the surfaces x = 0, x = 0, x = a, y = 0, y = a, z = 0, z = a. The electric field in the region is given by $\vec{E} = E_0 x \hat{i}$. Where $E_0 =$ $4 \times 10^4 \text{ NC}^{-1}\text{m}^{-1}$. If a = 2 cm, the charge contained in the cubical volume is $Q \times 10^{-14}$ C. The value of Q is _____. (Take $\epsilon_0 = 9 \times 10^{-12} \text{ C}^2/\text{Nm}^2$)

Answer (288)

Sol. $\phi_{\text{net}} = E_0 a a^3 - E_0(0) (a^2)$

$$\frac{q_{encl.}}{\varepsilon_0} = E_0 a^3$$

$$q_{encl.} = 4 \times 10^4 \times 8 \times 10^{-6} \times 9 \times 10^{-12}$$

$$= 288 \times 10^{-14}$$
∴ Q = 288

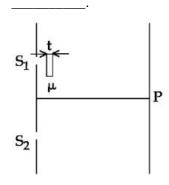
27. The surface of water in a water tank of crosssection area 750 cm² on the top of a house is *h* m above the tap level. The speed of water coming out through the tap of cross-section area 500 mm² is 30 cm/s. At that instant, $\frac{dh}{dt}$ is $x \times 10^{-3}$ m/s. The value of *x* will be _____.

Answer (02)

Sol. AV= av

$$750 \times 10^{-4} \times \left(\frac{dh}{dt}\right) = (500 \times 10^{-6})(30 \times 10^{-2})$$
$$\frac{dh}{dt} = \frac{15 \times 10^{-5}}{75 \times 10^{-3}}$$
$$= \frac{1}{5} \times 10^{-2}$$
$$= 2 \times 10^{-3} \text{ m/s}$$
$$x = 2$$

28. As shown in the figure, in Young's double slit experiment, a thin plate of thickness t = 10 μ m and refractive index μ = 1.2 is inserted infront of slit S₁. The experiment is conducted in air (μ = 1) and uses a monochromatic light of wavelength λ = 500 nm. Due to the insertion of the plate, central maxima is shifted by a distance of $x\beta_0$. β_0 is the fringe-width before the insertion of the plate. The value of *x* is



Answer (04)

Sol. shift due to slab $= \frac{(\mu - 1) tD}{d}$

$$\frac{(\mu - 1) tD}{d} = x \left(\frac{\lambda D}{d}\right)$$
$$x = \frac{(\mu - 1)t}{\lambda}$$
$$= \frac{(1.2 - 1) \times 10 \times 10^{-6}}{500 \times 10^{-9}}$$
$$= \frac{0.2}{5} \times \frac{10^{-5}}{10^{-7}}$$
$$= \frac{1}{25} \times 100$$
$$= 4$$

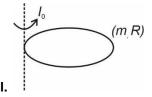
29. Moment of inertia of a disc of mass M and radius

'R' about any of its diameter is $\frac{MR^2}{4}$. The moment

of inertia of this disc about an axis normal to the disc and passing through a point on its edge will be,

$$\frac{x}{2}$$
 MR². The value of x is _

Answer (03)

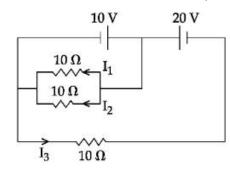


Sol.

$$\therefore I_D = \frac{mR^2}{4}$$
$$I_0 = \frac{3}{2}mR^2$$
$$\therefore x = 3$$

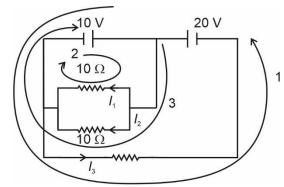
30. In the given circuit, the value of

 $\frac{|l_1 + l_3|}{l_1}$ is _____.



Answer (02)

Sol.



Using Kirchhoff's law in the indicated loop we get $l_1 = l_2 = l_3 = 1$ A

So
$$\frac{I_1 + I_3}{I_2} = 2$$

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer :

Given below are two statements : one is labelled as Assertion (A) and the other is labelled as Reason (R).

Assertion (A): Cu²⁺ in water is more stable than Cu⁺.

Reason (R): Enthalpy of hydration for Cu²⁺ is much less than that of Cu⁺.

In the light of the above statements, choose the **correct** answer from the options given below:

- (1) Both (A) and (R) are correct and (R) is the correct explanation of (A)
- (2) (A) is not correct but (R) is correct
- (3) (A) is correct but (R) is not correct
- (4) Both (A) and (R) are correct but (R) is not the correct explanation of (A)

Answer (3)

- Sol. Cu²⁺ in water is more stable than Cu⁺ due to much higher hydration enthalpy of Cu²⁺ ion.
 Hence correct answer is option (3)
- 32. Given below are two statements : one is labelled as Assertion (A) and the other is labelled as Reason (R).

Assertion (A): α -halocarboxylic acid on reaction with dil NH₃ gives good yield of α -amino carboxylic acid whereas the yield of amines is very low when prepared from alkyl halides.

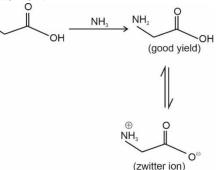
Reason (R): Amino acids exist in zwitter ion form in aqueous medium.

In the light of the above statements, choose the **correct** answer from the options given below:

- (1) (A) is not correct but (R) is correct
- (2) (A) is correct but (R) is not correct
- (3) Both (A) and (R) are correct and (R) is the correct explanation of (A)
- (4) Both (A) and (R) are correct but (R) is not the correct explanation of (A)





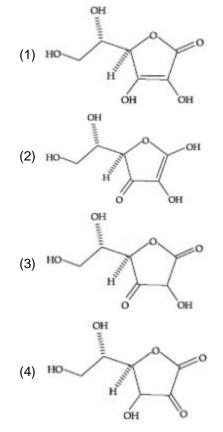


Statement-II : Reason is a correct statement as amino do exist as a zwitter ion. Reason is also a correct explanation.

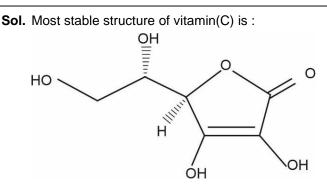
- 33. Which element is not present in Nessler's reagent?
 - (1) Potassium (2) Oxygen
 - (3) Mercury (4) Iodine

Answer (2)

- Sol. Nessler's reagent is K₂[HgI₄]
- 34. All structures given below are of vitamin C. Most stable of them is:







35. Which one of the following sets of ions represents a collection of isoelectronic species?

(Given : Atomic Number : F : 9, CI : 17, Na = 11, Mg

- = 12, AI = 13, K = 19, Ca = 20, Sc = 21)
- (1) Ba²⁺, Sr²⁺, K⁺, Ca²⁺
- (2) N³⁻, O²⁻, F⁻, S²⁻
- (3) K⁺, Cl⁻, Ca²⁺, Sc³⁺
- (4) Li+, Na+, Mg2+, Ca2+

Answer (3)

Sol. Isoelectronic species have same number of electrons.

k⁺, Cl⁻, Ca²⁺ and Sc³⁺ all have 18 electrons, hence these are isoelectronic.

- 36. The correct order of bond enthalpy (kJ mol-1) is
 - (1) C C > Si Si > Sn Sn > Ge Ge
 - (2) Si Si > C C > Sn Sn > Ge Ge
 - (3) C C > Si Si > Ge Ge > Sn Sn
 - (4) Si Si > C C > Ge Ge > Sn Sn

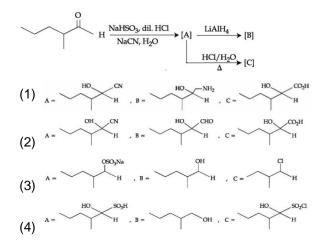
Answer (3)

Sol.	Bond	Bond energy
		(kJ mol ⁻¹)
	C–C	348
	Si–Si	297
	Ge–Ge	260
	Sn–Sn	240
	Correct answer will be (3)

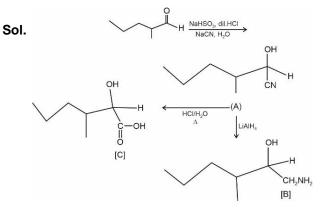
- 37. The industrial activity held least responsible for global warming is
 - (1) industrial production of urea
 - (2) manufacturing of cement
 - (3) steel manufacturing
 - (4) Electricity generation in thermal power plants

Answer (1)

- **Sol.** Industrial production of urea is least responsible for global warming.
- 38. The structures of major products A, B and C in the following reaction are sequence.



Answer (1)



 The starting material for convenient preparation of deuterated hydrogen peroxide (D₂O₂) in laboratory is

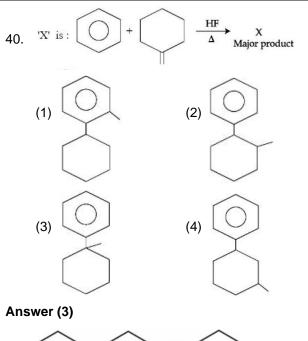
(1) 2-ethylanthraquinol (2) BaO

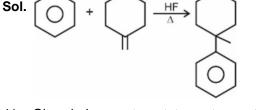
(3) BaO_2 (4) $K_2S_2O_8$

Answer (4)

Sol. $K_2S_2O_8$ is used in the laboratory preparation of D_2O_2

 $K_2S_2O_8(s) + 2D_2O(l) \rightarrow 2KDSO_4(aq) + D_2O_2(l)$





41. Given below are two statements: one is labelled asAssertion (A) and the other is labelled as Reason (R).

Assertion (A) : An aqueous solution of KOH when used for volumetric analysis, its concentration should be checked before the use.

Reason (R) : On aging, KOH solution absorbs atmospheric CO₂.

In the light of the above statements, choose the **correct** answer from the options given below :

- Both (A) and (R) are correct but (R) is not the correct explanation of (A)
- (2) Both (A) and (R) are correct and (R) is the correct explanation of (A)
- (3) (A) is correct but (R) is not correct
- (4) (A) is not correct but (R) is correct

Answer (2)

Sol. KOH absorbs CO₂ get converted to K₂CO₃

$$KOH + CO_2 \longrightarrow K_2CO_3 + H_2O$$

- 42. Given below are two statements :
 - Statement I : Sulphanilic acid gives esterification test for carboxyl group.
 - Statement II : Sulphanilic acid gives red colour in Lassigne's test for extra element detection.

In the light of the above statements, choose the **most appropriate** answer from the options given below :

- (1) Statement I is incorrect but Statement II is correct
- (2) Both **Statement I** and **Statement II** are incorrect
- (3) Statement I is correct but Statement II is incorrect

(4) Both Statement I and Statement II are correct Answer (1)

Sol. Sulphanilic acid is p-amino benzene sulphonic acid

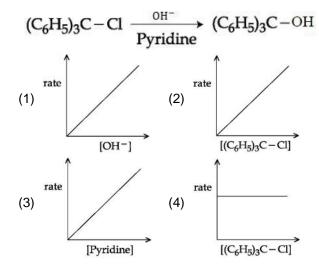


Since it contain both N and S so it give red colour in Lassaigne's test.

- 43. The complex cation which has two isomers is:
 - (1) $[Co(NH_3)_5CI]^+$ (2) $[Co(H_2O)_6]^{3+}$
 - (3) [Co(NH₃)₅NO₂]²⁺ (4) [Co(NH₃)₅Cl]²⁺

Answer (3)

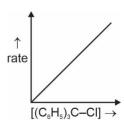
- **Sol.** Complex [Co(NH₃)₅NO₂]²⁺ will have two isomer one linked through N (Nitro) and one through O (Nitrite).
- 44. The graph which represents the following reaction is :



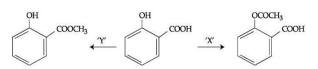


Sol. Rate = $K[(C_6H_5)_3C - CI]$

The correct mechanism is S_N1.



45. In a reaction,

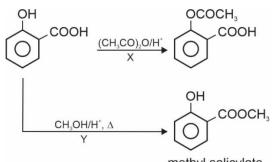


reagents 'X' and 'Y' respectively are :

- (1) $(CH_3CO)_2O/H^+$ and $(CH_3CO)_2O/H^+$
- (2) CH₃OH/H⁺, Δ and CH₃OH/H⁺, Δ
- (3) (CH_3CO)_2O/H+ and CH_3OH/H+, Δ
- (4) CH₃OH/H⁺, Δ and (CH₃CO)₂O/H⁺

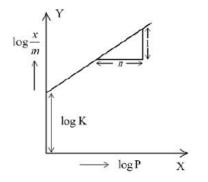
Answer (3)





methyl salicylate

46. In figure, a straight line is given for Freundrich Adsorption (y = 3x + 2.505). The value of $\frac{1}{n}$ and log K are respectively.



(1) 3 and 2.505 (2) 0.3 and 0.7033

(3) 0.3 and log 2.505 (4) 3 and 0.7033

Answer (1)

Sol. $\log \frac{x}{m} = \log k + \frac{1}{n} \log p$

On comparing, we get

$$\frac{1}{n} = 3 \Rightarrow n = 0.3$$
 and log k = 2.505

47. The effect of addition of helium gas to the following reaction in equilibrium state, is

 $PCI_5(g) \rightleftharpoons PCI_3(g) + CI_2(g)$

- (1) the equilibrium will go backward due to suppression of dissociation of PCI₅
- (2) addition of helium will not affect the equilibrium
- (3) the equilibrium will shift in the forward direction and more of Cl_2 and PCl_3 gases will be produced
- (4) helium will deactivate PCI₅ and reaction will stop

Answer (3)

- **Sol.** If we consider addition of He gas at constant pressure, the reaction will shift in forward direction [As rigid container is not given]
- 48. For electron gain enthalpies of the elements denoted as $\Delta_{eg}H$, the incorrect option is

(1)
$$\Delta_{eg}H(CI) < \Delta_{eg}H(F)$$
 (2) $\Delta_{eg}H(Se) < \Delta_{eg}H(S)$

(3) $\Delta_{eg}H(I) < \Delta_{eg}H(At)$ (4) $\Delta_{eg}H(Te) < \Delta_{eg}H(Po)$

Answer (2)

Sol.
$$\Delta H_{eg}$$
 (Cl) = -349 kJ/mole ΔH_{eg} (F) = -333 kJ/mole

$$\Delta H_{eq}$$
 (I) = -296 kJ/mole

 ΔH_{eq} (Se) = -195 kJ/mole

 $\Delta H_{eq}(S) = -200 \text{ kJ/mole}$

$$\Delta H_{eq}$$
 (Te) = -190 kJ/mole

 ΔH_{eq} (Po) = -174 kJ/mole

Electron gain enthalpy of Se is less negative than that of sulphur.

49. Given below are two statements: one is labelled as Assertion (A) and the other is labelled as Reason (R).

Assertion (A): Gypsum is used for making fireproof wall boards.

Reason (R): Gypsum is unstable at high temperatures.

In the light of the above statements, choose the **correct** answer from the options given below

- (1) Both (A) and (R) are correct and (R) is the correct explanation of (A)
- (2) (A) is correct but (R) is not correct
- (3) Both (A) and (R) are correct but (R) is not the correct explanation of (A)
- (4) (A) is not correct but (R) is correct

Answer (3)

- **Sol.** Both statements are correct. However, IInd statement has no relation with Ist Statement.
- 50. O O bond length in H_2O_2 is \underline{X} than the O O bond length in F_2O_2 . The O H bond length in H_2O_2 is \underline{Y} than that of the O F bond in F_2O_2 .

Choose the correct option for \underline{X} and \underline{Y} from those given below

- (1) X shorter, Y shorter
- (2) X shorter, Y longer
- (3) X longer, Y shorter
- (4) X longer, Y longer

Answer (3)

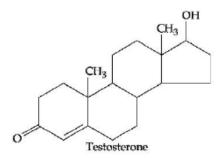
Sol. X – longer [because of more p-character in O – F bond]

Y – shorter [size of H is very small as compared to F]

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse andw the on-screen virtual numeric keypad in the place designated to enter the answer.

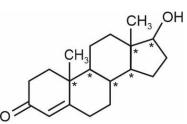
51. Testosterone, which is a steroidal hormone, has the following structure.



The total number of asymmetric carbon atom/s in testosterone is _____.

Answer (6)

Sol.



The total number of asymmetric carbon atoms in testosterone is 6.

52. A metal M crystallizes into two lattices: face centred cubic (fcc) and body centred cubic (bcc) with unit cell edge length of 2.0 and 2.5 Å respectively. The ratio of densities of lattices fcc to bcc for the metal M is _____.

(Nearest integer)

Answer (4)

Sol. d₁, Density of fcc lattice of metal M = $\frac{4 \times M}{N_0 (a_{fcc})^3}$

d₂, Density of bcc lattice of metal M =
$$\frac{2 \times M}{N_0 (a_{bcc})^3}$$

$$\frac{d_1}{d_2} = \frac{4}{2} \left(\frac{a_{bcc}}{a_{fcc}} \right)^3 = 2 \left(\frac{2.5}{2} \right)^3 = 3.90 \simeq 4$$

53. $A \rightarrow B$

The above reaction is of zero order. Half life of this reaction is 50 min. The time taken for the concentration of A to reduce to one-fourth of its initial value is _____ min.

Answer (75)

Sol.

$$a \to x = \frac{a}{4} \Rightarrow x = \frac{3a}{4}$$

 $t_{\frac{1}{2}} = \frac{a}{2K} = 50 \text{ min.} \Rightarrow \frac{a}{K} = 100 \text{ min.}$
 $t = \frac{x}{K} = \frac{3a}{4K} = 75$

54. 0.3 g of ethane undergoes combustion at 27°C in a bomb calorimeter. The temperature of calorimeter system (including the water) is found to rise by 0.5°C. The heat evolved during combustion of ethane at constant pressure is _____ kJ mol⁻¹.

(Nearest integer)

[Given: The heat capacity of the calorimeter system is 20 kJ K⁻¹, R = 8.3 JK⁻¹ mol⁻¹.

Assume ideal gas behaviour.

Atomic mass of C and H are 12 and 1 g mol⁻¹ respectively]

Answer (1006)

Sol.
$$C_2H_6(g) + \frac{7}{2}O_2(g) \rightarrow 2CO_2(g) + 3H_2O(\ell)$$

No. of moles of ethane = $\frac{0.3}{30} = 0.01$ Heat evolved in Bomb calorimeter = 20×0.5 = 10 kJ $\Delta U = -\frac{10}{0.01} = -1000 \text{ kJ mol}^{-1}$ $\Delta H = \Delta U + \Delta n_g RT$ = $-1000 + (-2.5) \times \frac{8.3 \times 300}{1000}$ = -1000 - 6.225= -1006.225

 $|\Delta H|\simeq 1006 \; kJ \; mol^{-1}$

55. The spin only magnetic moment of [Mn(H₂O)₆]²⁺ complexes is _____ B.M. (Nearest integer)
 (Given: Atomic no. of Mn is 25)

Answer (6)

min.

Sol.
$$\left[Mn(H_2O)_6\right]^{2+}$$

 Mn^{2+} : $3a^5$
No. of unpaired electrons = 5
 $\mu = \sqrt{35}$ BM $\simeq 6$ BM

56. 20% of acetic acid is dissociated when its 5 g is added to 500 mL of water. The depression in freezing point of such water is ______ × 10^{-3°}C. Atomic mass of C, H and O are 12, 1 and 16 a.m.u. respectively.

[Given : Molal depression constant and density of water are 1.86 K kg mol^-1 and 1 g cm^{-3} respectively.

Answer (372)

Sol.
$$CH_{3}COOH \longrightarrow H^{+} + CH_{3}COO^{-}$$

 $i = 1.2$
 $[CH_{3}COOH] = \frac{5}{60 \times 0.5} = \frac{5}{30}M$
 $\Delta T_{f} = i K_{f} m$
 $1.2 \times 1.86 \times \frac{5}{30} = 0.372 \,^{\circ}C$
 $= 372 \times 10^{-3} \,^{\circ}C$

57.	1×10^{-5} M AgNO ₃ is added to 1 L of saturated	Answer (3)	
	solution of AgBr. The conductivity of this solution at	Sol. Chloroliazepoxide	
	298 K is × 10 ⁻⁸ S m ⁻¹ .	Veronal	
	[Given : K _{SP} (AgBr) = 4.9 × 10 ⁻³ at 298 K	Valium	
	$\lambda_{Ag^+}^0 = 6 \times 10^{-3} \text{ S m}^2 \text{ mol}^{-1}$	Salvarsan is an antibiotic	
	$\lambda_{Br^{-}}^{0} = 8 \times 10^{-3} \text{ S m}^{2} \text{ mol}^{-1}$	59. The molarity of a 10% (v/v) solution of di-bromine solution in CCl₄ (carbon tetrachloride) is 'x'.	
	$\lambda_{NO_3^-}^0 = 7 \times 10^- \text{ S m}^2 \text{ mol}^-$]	x = × 10^{-2} M. (Nearest integer)	
Ans	wer (13039.2)	[Given : molar mass of $Br_2 = 160 \text{ g mol}^{-1}$	
Sol	$A_0Br(S) \longrightarrow A_0^+ (a_0) + Br^-(a_0)$	atomic mass of $C = 12 \text{ g mol}^{-1}$	
001.	$\operatorname{AgBr}(S) \underset{(10^{-} + x)}{\longrightarrow} \operatorname{Ag^{+}}(aq) + \operatorname{Br}_{x}^{-}(aq)$	atomic mass of CI = 35.5 g mol ⁻¹	
	$x(x + 10^{-5}) = 4.9 \times 10^{-13}$	density of dibromine = 3.2 g cm ^{-3}	
	$x \simeq 4.9 \times 10^{-} M$	density of CCl ₄ = 1.6 g cm ^{-3}]	
	$\lambda^{0}_{Ag^{+}} = 6 \times 10^{-3} \text{ S cm}^{2} \text{ mol}^{-1}$	Answer (139)	
	$10 \qquad 9 + 10^{-3} \text{ S cm}^2 \text{ mol}^{-1}$	Sol. Mass of 10 mL of $Br_2 = 10 \times 3.2 = 32$ gm	
	$\lambda^{0}_{Br^{-}} = 8 \times 10^{-3} \text{ S cm}^{2} \text{ mol}^{-1}$	Mass of 90 mL of CCl ₄ = 90 × 1.6 = 144 gm	
	$\lambda_{NO_3^-}^0 = 7 \times 10^- \text{ S cm}^2 \text{ mol}^{-1}$	Molality of Br ₂ solution in CCl ₄ = $\frac{32 \times 1000}{160 \times 144}$	
	$\mathbf{K}_{\text{solution}} = \mathbf{K}_{Ag^+} + \mathbf{K}_{Br^-} + \mathbf{K}_{NO_3^-}$	= 1.39 M	
	$= 6 \times 10^{-3} \times 10^{-5} \times 10^{3} + 8 \times 10^{-3} \times 4.9 \times 10^{-8} \times 10^{3}$	= 139 × 10⁻	
	+ 7 × 10 ⁻³ ×10 ⁻⁵ × 10 ³	60. Among following compounds, the number of those	
	= (6000 + 39.2 + 7000) × 10 ⁻⁸	present in copper matte is	
	= 13039.2 × 10 ⁻⁸ Sm ⁻¹	A. CuCO ₃	
58.	Among the following, the number of tranquilizer/s	B. Cu ₂ S	
	is /are	C. Cu ₂ O	
	A. Chloroliazepoxide	D. FeO	
	B. Veronal	Answer (3)	
	C. Valium	Sol. Copper matte contains	
	D. Salvarsan	Cu ₂ S, Cu ₂ O, FeO	

MATHEMATICS

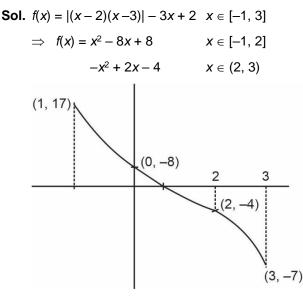
SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer :

- 61. The sum of absolute maximum and minimum values of the function $f(x) = |x^2 5x + 6| 3x + 2$ in the interval [-1, 3] is equal to :
 - (1) 24 (2) 13
 - (3) 12 (4) 10

Answer (1)



- ∴ Maximum value = 17
 Minimum value of -7
- ∴ Sum = 24

62. The value of the integral $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{x + \frac{\pi}{4}}{2 - \cos 2x} dx$ is: (1) $\frac{\pi^2}{6}$ (2) $\frac{\pi^2}{6\sqrt{3}}$ (3) $\frac{\pi^2}{12\sqrt{3}}$ (4) $\frac{\pi^2}{3\sqrt{3}}$ Answer (2)

Sol.
$$I = \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{x + \frac{\pi}{4}}{(2 - \cos 2x)} dx$$

Using $\int_{a}^{b} f(x) dx = \int_{a}^{b} f(a + b - x) dx$
 $I = \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \left(\frac{-x + \frac{\pi}{4}}{2 - \cos 2x} \right) dx$
 $\therefore 2I = \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{\pi dx}{2(2 - \cos 2x)}$
 $\Rightarrow I = \frac{2\pi}{4} \int_{0}^{\frac{\pi}{4}} \left(\frac{\frac{dx}{2 - 1 - \tan^{2} x}}{1 + \tan^{2} x} \right) dx$
 $\Rightarrow I = \frac{\pi}{2} \int_{0}^{\frac{\pi}{4}} \left(\frac{1 + \tan^{2} x}{1 + 3\tan^{2} x} \right) dx$
Put $\tan x = t$
 $\Rightarrow I = \frac{\pi}{2} \int_{0}^{1} \frac{dt}{1 + 3t^{2}} \Rightarrow I = \frac{\pi}{6\sqrt{3}}$
63. The sum $\sum_{n=1}^{\infty} \frac{2^{2} + 3n + 4}{(2n)!}$ is equal to :
(1) $\frac{13e}{4} + \frac{5}{4e}$ (2) $\frac{11e}{2} + \frac{7}{2e}$
(3) $\frac{13e}{4} + \frac{5}{4e} - (4) \frac{11e}{2} + \frac{7}{2e}$
Answer (1)
Sol. $\sum_{n=1}^{\infty} \frac{2^{2} + 3n + 4}{(2n)!}$
Put $2n = t \Rightarrow n = \frac{t}{2}$
 $\therefore \sum_{t \to even} \frac{\frac{t^{2}}{2} + \frac{3t}{2} + 4}{t!}$

$$\Rightarrow \sum_{t \to \text{even}} \frac{2}{2t!}$$

$$\Rightarrow \frac{1}{2} \sum_{t \to \text{even}} \left(\frac{t-1}{(t-1)!} + \frac{1}{(t-1)!} + \frac{3}{(t-1)!} + \frac{8}{t!} \right)$$

$$\Rightarrow \frac{1}{2} \sum_{t \to \text{even}} \left(\frac{1}{(t-2)!} + \frac{4}{(t-1)!} + \frac{8}{t!} \right)$$

$$\Rightarrow \frac{1}{2} \left(\frac{e+e^{-1}}{2} + \frac{4(e-e^{-1})}{2} + \frac{8(e+e^{-1})}{2} \right)$$

$$\Rightarrow \frac{1}{4} \left(13e+5e^{-1} \right)$$

64. Let *a*, *b* be two real numbers such that ab < 0. If the complex number $\frac{1+ai}{b+i}$ is of unit modulus and a + ib lies on the circle |z - 1| = |2z|, then a possible value of $\frac{1+[a]}{4b}$, where [*t*] is greatest integer function is :

(1)
$$-1$$
 (2) 1
(3) $-\frac{1}{2}$ (4) $\frac{1}{2}$

Answer (*)

Sol.
$$|1+ai| = |b+i|$$

$$\Rightarrow a^{2}+1 = b^{2}+1 \Rightarrow a^{2} = b^{2}$$

$$\& |a+ib-1| = |2a+2ib|$$

$$\Rightarrow a^{2}+1-2a+b^{2} = 4a^{2}+4b^{2}$$

$$\Rightarrow 3a^{2}+3b^{2}+2a-1=0$$

$$\Rightarrow ba^{2}+2a-1=0$$

$$\therefore a = \frac{-2\pm\sqrt{4+24}}{2(6)}$$

$$= \frac{-1\pm\sqrt{-2}}{6}$$

$$\therefore (a, b) = \left(\frac{-1+\sqrt{7}}{6}, \frac{-1-\sqrt{7}}{6}\right) \text{ or }$$

$$\left(\frac{-1-\sqrt{7}}{6}, \frac{-1+\sqrt{7}}{6}\right)$$

$$\therefore \frac{1+[a]}{4b} = 0 \text{ or } \frac{3}{2(-1-\sqrt{7})}$$

$$\therefore \text{ No option matches}$$

65. Let
$$f: \mathbb{R} - \{0, 1\} \rightarrow \mathbb{R}$$
 be a function such that
 $f(x) + f\left(\frac{1}{1-x}\right) = 1 + x$. then $f(2)$ is equal to
(1) $\frac{9}{2}$ (2) $\frac{9}{4}$
(3) $\frac{7}{3}$ (4) $\frac{7}{4}$
Answer (2)
Sol. $f(x) + f\left(\frac{1}{1-x}\right) = 1 + x$...(i)
If $x \rightarrow \frac{1}{1-x}$
 $f\left(\frac{1}{1-x}\right) + f\left(\frac{1}{1-\frac{1}{1-x}}\right) = 1 + \frac{1}{1-x}$
 $f\left(\frac{1}{1-x}\right) + f\left(\frac{1-x}{-x}\right) = \frac{2}{-x}$...(ii)
If $x \rightarrow \frac{x-1}{x}$
 $f\left(\frac{x-1}{x}\right) + f(x) = \frac{2x-1}{-x}$...(iii)
Putting $x = 2$
 $f(2) + f(-1) = 3$
 $(-1) + f\left(\frac{1}{2}\right) = 0$
 $f \mid \frac{1}{2} \mid + f(2) = \frac{3}{2}$
Solving these $f(2) = \frac{9}{4}$
66. Let the plane P pass through the intersection of the
planes $2x + 3y - z = 2$ and $x + 2y + 3z = 6$, and be
perpendicular to the plane $2x + y - z + 1 = 0$. If d is
the distance of P from the point (-7, 1, 1), then c^{β} is

(1)	25	(2)	15
(1)	83	(2)	53

(3)
$$\frac{250}{82}$$
 (4) $\frac{250}{83}$

equal to :

- **Sol.** Let the equation of plane *P* be
 - $(2x+3y-z-2)+\lambda(x+2y+3z-6) = 0$ Now since *P* is \perp^r to 2x+y-z+1=0 $\therefore \quad 2(2+\lambda)+1(3+2\lambda)-1(-1+3\lambda) = 0$ $\boxed{\lambda = -8}$ $\therefore \quad P: \quad 6x+13y+25z = 46$

Now distance from the point (-7, 1, 1)

$$d = \left| \frac{-42 + 13 + 25 - 46}{\sqrt{36 + 169 + 625}} \right|$$

$$\therefore \quad d^2 = \frac{2500}{830} = \frac{250}{83}$$

67. Let $s = \left| x \in \mathbb{R} : 0 < x < 1 \text{ and } 2 \tan \left(\frac{1-x}{1+x} \right) = \cos^{-1} \left(\frac{1-x^2}{1+x^2} \right) \right|$

If n(S) denotes the number of elements in S then :

- (1) n(S) = 0
- (2) n(S) = 2 and only one element in S is less than $\frac{1}{2}$
- (3) n(S) = 1 and the element in S is less than $\frac{1}{2}$

(4) n(S) = 1 and the elements is S is more than $\frac{1}{2}$

Answer (3)

Sol. 2tan $\left(\frac{x}{1+x}\right) = \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$ Put $\tan^{-1}x = \theta, \ \theta \in \left(0, \frac{\pi}{4}\right)$ 2tan $\left(\tan\left(\frac{\pi}{4}-\theta\right)\right) = \cos^{-1}(\cos 2\theta)$ $2\left(\frac{\pi}{4}-\theta\right) = 2\theta$ $\frac{\pi}{2} = 4\theta$ or $\left[\theta = \frac{\pi}{8}\right]$ $x = \tan\left(\frac{\pi}{8}\right) = \sqrt{2} - 1 < \frac{1}{2}$ 68. Let $\vec{a} = 2i - 7\hat{j} + 5\hat{k}$, $\vec{b} = \hat{i} + \hat{k}$, $\vec{c} = \hat{i} + 2\hat{j} - 3\hat{k}$ be three given vectors. If \vec{r} is a vector such that $\vec{r} \times \vec{a} = \vec{c} \times \vec{a}$ and $\vec{r} \cdot \vec{b} = 0$, then $|\vec{r}|$ is equal to

(1)
$$\frac{11}{7}$$
 (2) $\frac{11}{5}\sqrt{2}$

(3)
$$\frac{\sqrt{914}}{7}$$
 (4) $\frac{11}{7}\sqrt{2}$

Answer (4)

Sol.
$$\vec{r} = \vec{c} + \lambda \vec{a}$$

 $\vec{r} \cdot \vec{b} = \vec{c} \cdot \vec{b} + \lambda \vec{a} \cdot \vec{b} = 0$
 $-2 + \lambda(7) = 0 \implies \lambda = \frac{2}{7}$
 $\vec{r} = (\hat{i} + 2\hat{j} - 3\hat{k}) + \frac{2}{7}(2\hat{i} - 7\hat{j} + 5\hat{k})$
 $= \frac{11}{7}\hat{i} + 0\hat{j} + \frac{11}{7}\hat{k}$
 $|\vec{r}| = \frac{11}{7}\sqrt{2}$

69. Let $P(x_0, y_0)$ be the point on the hyperbola $3x^2 - 4y^2$ = 36, which is nearest to the line 3x + 2y = 1. Then $\sqrt{2}(y_0 - x_0)$ is equal to

Answer (3)

Sol. If (x_0, y_0) is point on hyperbola then

tangent at (x_0, y_0) is parallel to 3x + 2y = 1

Equation of tangent
$$\rightarrow \frac{xx_0}{12} - \frac{yy}{9} = 2$$

Slope of tangent = $\frac{-3}{2}$

Equation of tangent in slope form

$$y = \frac{-3}{2}x \pm \sqrt{12 \cdot \frac{9}{4} - 9}$$
$$= \frac{-3}{2}x \pm 3\sqrt{2}$$

Or $3x+2y=6\sqrt{2}$

Comparing

$$\frac{\frac{x_0}{12}}{3} = \frac{\frac{-y_0}{9}}{2} = \frac{1}{6\sqrt{2}}$$
$$x_0 = 3\sqrt{2}, \ y_0 = \frac{-3}{\sqrt{2}}$$
$$\sqrt{2}(y_0 - x_0) = -3 - 6 = -9$$

- 70. The number of integral values of *k*, for which one root of the equation $2x^2 8x + k = 0$ lies in the interval (1, 2) and its other root lies in the interval (2, 3) is
 - (1) 1
 (2) 2

 (3) 3
 (4) 0

Answer (1)

- **Sol.** $f(1) > 0 \Longrightarrow k > 6$
 - $f(2) < 0 \Longrightarrow k < 8$
 - $f(3) > 0 \Longrightarrow k > 6$
 - $k \in (6, 8)$

Only 1 integral value of k is 7

- 71. Which of the following statements is a tautology?
 - (1) $(p \land (p \rightarrow q)) \rightarrow \sim q$
 - (2) $p \lor (p \land q)$

$$(3) \quad (p \land q) \rightarrow (\sim (p) \rightarrow q)$$

(4)
$$p \rightarrow (p \land (p \rightarrow q))$$

Answer (3)

Sol.
$$\sim p \rightarrow q \equiv \sim (\sim p) \lor q \equiv p \lor q$$

 $p \land q \rightarrow (\sim p \rightarrow q)$
 $\equiv p \land q \rightarrow (p \lor q)$
 $\equiv \sim (p \land q) \lor (p \lor q)$
 $\equiv (\sim p \lor \sim q) \lor (p \lor q)$
 $\equiv (\sim p \lor (p \lor q)) \lor (\sim q \lor (p \lor q))$
 $\equiv T \lor T$
 $\equiv T$

72. Let P(S) denote the power set of $S = \{1, 2, 3, ..., 10\}$. Define the relations R_1 and R_2 on P(S) as AR_1B if $(A \cap B^c) \cup (B \cap A^c) = \phi$ and AR₂B if $A \cup B^{c} = B \cup A^{c}$, $\forall A, B \in P(S)$. Then (1) Only R_2 is an equivalence relation (2) Both R_1 and R_2 are not equivalence relations (3) Only R_1 is an equivalence relation (4) Both R_1 and R_2 are equivalence relations Answer (4) **Sol.** R_1 : $(A \cap B^C) \cup (B \cap A^C) = \phi$ \Rightarrow A = B $R_2: (A \cup B^C) = (B \cup A^C)$ \Rightarrow A = BBoth R_1 and R_2 are equivalence. 73. Let $\alpha x = \exp(x^{\beta}y^{\gamma})$ be the solution of differential equation $2x^2ydy - (1 - xy^2)dx = 0, x > 0,$ $y(2) = \sqrt{\log_e 2}$. Then $\alpha + \beta - \gamma$ equals (1) -1 (2) 1 (3) 3 (4) 0 Answer (2) Sol. Given differential equation

$$2x^{2}ydy - (1 - xy^{2})dx = 0, x > 0$$

$$2xy dy + y^{2}dx \quad \frac{1}{x}dx$$

$$\int d(xy^{2}) = \int \frac{1}{x}dx$$

$$xy^{2} = \ln x + C \qquad \dots(i)$$

$$y(2) = \sqrt{\log_{e} 2}$$

$$2\ln 2 = \ln 2 + C$$

$$\therefore \quad \boxed{C = \ln 2}$$

$$\therefore \quad by (i)$$

$$xy^{2} = \ln 2x$$

$$2x = e^{xy^{2}}$$

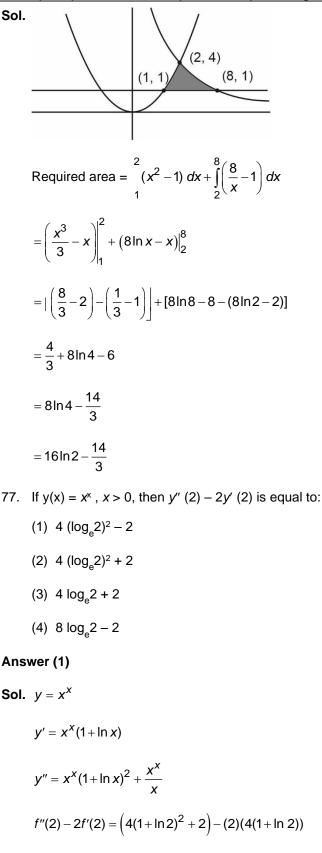
$$\therefore \quad \alpha = 2, \beta = 1, \gamma = 2$$

$$\therefore \quad \alpha + \beta - \gamma = 1$$

74. For the system of linear equations ax + y + z = 1, x + ay + z = 1, $x + y + az = \beta$, which one of the following is **NOT** correct? (1) It has infinitely many solutions if $\alpha = 1$ and $\beta = 1$ (2) $x + y + z = \frac{3}{4}$ if $\alpha = 2$ and $\beta = 1$ (3) It has no solution if $\alpha = -2$ and $\beta = 1$ (4) It has infinitely many solutions if $\alpha = 2$ and $\beta = -1$ Answer (4) Answer (3) **Sol.** For infinite solution $\Delta = \Delta_x = \Delta_y = \Delta_z = 0$ $\Delta = \begin{vmatrix} \alpha & 1 & 1 \\ 1 & \alpha & 1 \\ 1 & \alpha & 1 \end{vmatrix} = 0 \implies (\alpha^3 - 3\alpha + 2) = 0 \implies \alpha = 1, -2$ (5, 6) If $\beta = 1$, then all planes are overlapping n(A) = 15... Option (1) is correct. Option (2) $\alpha = 2, \beta = 1$ n(B) = 92x + y + z = 1x + 2y + z = 1x + y + 2z = 1Adding all three equations = 3 + 3 - 0 $x+y+z=\frac{3}{4}$ = 6 .: option (2) is correct. Option (3) If $\alpha = -2$ and $\beta = 1$, then $\Delta = 0$, $\Delta_x \neq 0$.: No solution .: Option (3) is correct. Option (4) If $\alpha = 2 \implies \Delta \neq 0$... Unique solution exist Option (4) is incorrect. *.*.. Answer (3) *.*.. Option (4) is answer.

75. Two dice are thrown independently. Let A be the event that the number appeared on the 1st die is less than the number appeared on the 2nd die, B be the event that the number appeared on the 1st die is even and that one the second die is odd, and C be the event that the number appeared on the 1st die is odd and that on the 2nd is even. Then (1) A and B are mutually exclusive (2) The number of favourable cases of the events A, B and C are 15, 6 and 6 respectively (3) The number of favourable cases of the event $(A \cup B) \cap C$ is 6 (4) B and C are independent |(1, 2), (1, 3), (1, 4), (1, 5), (1, 6) (2, 3), (2, 4), (2, 5), (2, 6)**Sol.** $A = \{(3, 4), (3, 5), (3, 6)\}$ (4, 5), (4, 6) (2, 1), (2, 3), (2, 5) $B = \{(4, 1), (4, 3), (4, 5)\}$ (6, 1), (6, 3), (6, 5)Similarly, n(C) = 9 $(4, 5) \in A \text{ and } (4, 5) \in B$:. A and B are not exclusive events $n((A \cup B) \cap C) = n(A \cap C) + n(B \cap C) - n(A \cap B \cap C)$ Option (3) is correct. $n(B) = \frac{9}{36}, n(C) = \frac{9}{36}, n(B \cap C) = 0$ \Rightarrow $n(B) \cdot n(C) \neq n(B \cap C)$: B and C are not independent 76. The area of the region given by $\{(x,y): xy \le 8, 1 \le y \le x^2\}$ is : (1) $8\log_e 2 - \frac{13}{3}$ (2) $16\log_e 2 + \frac{7}{3}$ (3) $16 \log_e 2 - \frac{14}{2}$ (4) $8 \log_e 2 + \frac{7}{6}$

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 $= 4(1 + (\ln 2)^2) + 2 - 8$

 $= 4(\ln 2)^2 - 2$

- 78. Let $\vec{a} = 5\hat{t} \hat{j} \hat{k}$ and $\vec{b} = i + 3j + 5\hat{k}$ be two vectors. Then which one of the following statements is True?
 - (1) Projection of \vec{a} on \vec{b} is $\frac{-17}{\sqrt{35}}$ and the direction of the projection vector is same as of \vec{b} .
 - (2) Projection of \vec{a} on \vec{b} is $\frac{17}{\sqrt{35}}$ and the direction of the projection vector is opposite to the direction of \vec{b} .
 - (3) Projection of \vec{a} on \vec{b} is $\frac{17}{\sqrt{35}}$ and the direction of the projection vector is same as of \vec{b} .
 - (4) Projection of \vec{a} on \vec{b} is $\frac{-17}{\sqrt{35}}$ and the direction of the projection vector is opposite to the direction of \vec{b}

Answer (2)

Sol.
$$\vec{a} = 5\hat{i} - \hat{j} - 3\hat{k}, \vec{b} = \hat{i} + 3\hat{j} + 5\hat{k}$$

projection of $\vec{a} \cdot \vec{b} = \left| \frac{5 - 3 - 15}{\sqrt{35}} \right| = \frac{17}{\sqrt{35}}$

 $\vec{a} \cdot \vec{b} < 0$

- ... Option (2) is correct.
- 79. Let $9 = x_1 < x_2 < ... < x_7$ be in an A.P. with common difference *d*. If the standard deviation of $x_1, x_2, ..., x_7$ is 4 and the mean is \overline{x} , then $\overline{x} + x_6$ is equal to:

(1)
$$18\left(1+\frac{1}{\sqrt{3}}\right)$$
 (2) 34
(3) 25 (4) $2\left(9+\frac{8}{\sqrt{7}}\right)$

Answer (2)

Sol. Let the series be a - 3d, a - 2d, a - d, a, a + d, a + 2d, a + 3dGiven $x_1 = 9 \Rightarrow a - 3d = 9$...(i) Variance does not change of shifting origin ∴ Variance and mean of -3d, -2d, -d, 0, d, 2d, 3d is 16 and $\overline{x} - a$ $\Rightarrow 16 = \frac{2}{7}(9d^2 + 4d^2 + d^2) - (0)^2$

 $\Rightarrow 16 = \frac{2}{7} \times 14d^2$ \Rightarrow d = 2 (A.P. is increasing) Using (i) a = 15 $x_{e} = a + 2d$ = 15 + 4 = 19 $\bar{x} + x_6 = a + 19$ = 15 + 19= 34.: option (2) is correct. 80. If $A = \frac{1}{2} \begin{vmatrix} 1 & \sqrt{3} \\ -\sqrt{3} & 1 \end{vmatrix}$, then: (1) $A^{30} - A^{25} = 2I$ (2) $A^{30} + A^{25} - A = I$ (3) $A^{30} + A^{25} + A = I$ (4) $A^{30} = A^{25}$ Answer (2) **Sol.** $A = \frac{1}{2} \begin{vmatrix} 1 & \sqrt{3} \\ -\sqrt{3} & 1 \end{vmatrix}$ Let $\theta = \frac{\pi}{3}$ $A^{2} = \begin{vmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{vmatrix} \begin{vmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{vmatrix}$ $= \begin{vmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{vmatrix}$ $A^{3} = \begin{vmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{vmatrix} \begin{vmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{vmatrix}$ $= \begin{vmatrix} \cos 3\theta & \sin 3\theta \\ -\sin 3\theta & \cos 3\theta \end{vmatrix}$ $\therefore \quad A^{30} \quad \begin{vmatrix} \cos 30\theta & \sin 30\theta \\ -\sin 30\theta & \cos 30\theta \end{vmatrix} = \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix}$ $A^{25} = \begin{bmatrix} \cos 25\theta & \sin 25\theta \\ -\sin 25\theta & \cos 25\theta \end{bmatrix} = \frac{1}{2} \begin{vmatrix} 1 & \sqrt{3} \\ -\sqrt{3} & 1 \end{vmatrix} = A$ $\therefore A^{30} + A^{25} - A = I$.: option (2) is correct.

JEE (Main)-2023 : Phase-1 (01-02-2023)-Evening

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

81. If the term without x in the expansion of $\left(x^{\frac{2}{3}} + \frac{\alpha}{x^{3}}\right)^{22}$ is 7315, then $|\alpha|$ is equal to _____.

Answer (01)

Sol. Given expansion
$$\left(x^{\frac{2}{3}} + \frac{\alpha}{x^3}\right)^{22}$$

$$T_{r+1} = {}^{22}C_r \left(x^{\frac{2}{3}}\right)^{22-r} \left(\frac{\alpha}{x^3}\right)^r$$

For constant term

$$\frac{44-2r}{3}-3r=0$$

Now ${}^{22}C_4 \alpha^4 = 7315$

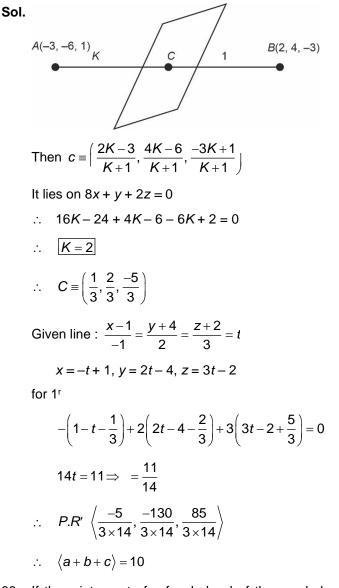
$$\frac{22 \times 21 \times 20 \times 19}{4 \times 3 \times 2 \times 1} \alpha^{4} = 7315$$

$$\therefore \quad \alpha^{4} = 1$$

 $\therefore |\alpha| = 1$

82. The point of intersection *C* of the plane 8x + y + 2z = 0 and the line joining the points A(-3, -6, 1) and B(2, 4, -3) divides the line segment *AB* internally in the ratio k : 1. If *a*, *b*, *c* (|*a*|, |*b*|, |*c*| are coprime) are the direction ratios of the perpendicular from the point *C* on the line $\frac{1-x}{1} = \frac{y+4}{2} = \frac{z+2}{3}$, then |a + b + c| is equal to

Answer (10)



83. If the *x*-intercept of a focal chord of the parabola $y^2 = 8x + 4y + 4$ is 3, then the length of the chord is equal to _____.

Answer (16)

- **Sol.** $y^2 = 8x + 4y + 4$
 - $(y-2)^2 = 8(x+1)$

Focus \equiv (1, 2)

Equation of focal chord : $\frac{x}{3} + \frac{y}{b} = 1$ and $\frac{1}{3} + \frac{2}{b} = 1$

 $\therefore x + y = 3$

Intersection with parabola

 $y^2 + 4 - 4y = 8(4 - y)$

 $y^2 + 4y - 28 = 0$

- $\therefore (y_1 y_2)^2 = 16 + 4 \times 28$ $(x_1 x_2)^2 = 16 + 4 \times 28$ $\therefore \text{ length} = \sqrt{2 \times 16 \times 8} = 16$
- 84. Let $\alpha x + \beta y + \gamma z = 1$ be the equation of a plane passing through the point (3, -2, 5) and perpendicular to the line joining the points (1, 2, 3) and (-2, 3, 5). Then the value of $\alpha\beta\gamma$ is equal to

Answer (06)

$$a(x-3) + b(y+2) + c(z-5) = 0$$

Dr's of plane : $3\hat{i} - \hat{j} - 2\hat{k}$
 $< 3, -1, -2 >$
 $P: 3(x-3) - 1(y+2) - 2(z-5) = 0$
 $3x - 9 - y - 2 - 2z + 10 = 0$
 $3x - y - 2z = 1$
 $\therefore \quad \alpha = 3, \ \beta = -1, \ \gamma = -2$
 $\alpha\beta\gamma = 6$

85. The line x = 8 is the directrix of the ellipse $E \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ with the corresponding focus (2, 0). If the tangent to *E* at point *P* in the first quadrant passes through the point $(0, 4\sqrt{3})$ and intersects the x-axis at *Q*, then $(3PQ)^2$ is equal to

Answer (39)

Sol.
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

 $F(2, 0) = (ae, 0) \begin{vmatrix} a = 4 \\ e = \frac{1}{2} \end{vmatrix} \Rightarrow b^2 = 12$
 $E : \frac{x^2}{16} + \frac{y^2}{12} = 1$
 $T : y = mx \pm \sqrt{16m^2 + 12}$
Passes through $(0, 4\sqrt{3})$
 $4\sqrt{3} = \pm \sqrt{16m^2 + 12}$

Sol. ${}^{m}C_{1}, {}^{m}C_{2}, {}^{m}C_{3}$ are first, third and fifth term of AP

$$\therefore \quad m = \pm \frac{3}{2}$$

$$T : y = \frac{-}{2}x + \sqrt{48}$$

$$T : \frac{3}{2}x + y = \sqrt{48} \qquad \dots(i)$$

$$T \quad \frac{xx}{16} + \frac{yy_1}{12} = 1 \qquad \dots(ii)$$
Comparing (i) and (ii)
$$P\left(\frac{\sqrt{48}}{2}, \frac{\sqrt{48}}{4}\right)$$

$$Q\left(\frac{2\sqrt{48}}{3}, 0\right)$$

$$3(PQ)^2 = 9(PQ)^2$$

$$\left(\left(\frac{\sqrt{48}}{2} - \frac{2\sqrt{48}}{3}\right)^2 + \left(\frac{\sqrt{48}}{4}\right)^2\right)$$

$$= 39$$
Number of integral solutions
$$x + y + z = 21$$
 where $x \ge 1, y \ge 2$

86. Number of integral solutions to the equation x + y + z = 21, where $x \ge 1$, $y \ge 3$, $z \ge 4$, is equal to

Answer (105)

- **Sol.** *x* + *y* + *z* = 21
 - $\therefore \quad x \ge 1, \ y \ge 3, \ y \ge 4$

$$\therefore x_1 + y_1 + z_1 = 13$$

Number of solutions = $13 + 3 - {}^{1}C_{3-1}$

$$= {}^{15}C_2 = \frac{151}{21,131} = 7 \times 15$$

- = 105
- 87. Let the sixth term in the binomial expansion of

$$\left(\sqrt{2^{\log_2(10-3^x)}} + \sqrt[5]{2^{(x-2)\log_2^3}}\right)^m$$
, in the increasing

powers of $2^{(x-2)\log_2^3}$, be 21. If the binomial coefficients of the second, third and fourth terms in the expansion are respectively the first, third and fifth terms of an A.P., then the sum of the squares of all possible values of *x* is _____.

Answer (04)

$$\therefore a = {}^{m} C_{1}$$

$$a + 2d = {}^{m} C_{2}$$

$$a + 4d = {}^{m} C_{3}$$

$$\therefore 2 {}^{m} C_{2} - {}^{m} C_{3} = m$$

$$\Rightarrow m = 7 \text{ or } m = 2$$

$$\therefore m = 7$$

$$\left(\sqrt{2^{\log_{2}(10-3^{x})} + \sqrt[5]{2(x-2)\log_{2}^{3}}}\right)^{m}$$

$$T_{6} = 21$$

$${}^{7}C_{5}\left(\left(10 - 3^{x}\right)^{\frac{1}{2}}\right)^{7-5}(3)^{x-2} 21$$

$$\frac{27}{9}3^{x}(10 - 3^{x}) = 27$$

$$3^{x}(10 - 3^{x}) = 9$$
Let $3^{x} = t$

$$t(10 - t) = 9$$

$$t^{2} - 10t + 9 = 0$$

$$(t - 9)(t - 1) = 0$$

$$t = 9 \text{ or } t = 1$$

$$3^{x} = 9 \text{ or } 3^{x} = 1$$

$$\therefore x_{1} = 2 \text{ or } x_{1} = 0$$

$$x_{1}^{2} + x_{2}^{2} = 4$$
The avere of the constraint form of the

- 88. The sum of the common terms of the following three arithmetic progressions.
- 3, 7, 11, 15, ..., 399, 2, 5, 8, 11, ..., 359 and 2, 7, 12, 17, ..., 197, Is equal to _____. Answer (321)

Sol. $S_1 \rightarrow 3, 7, 11, ..., 399$ $S_2 \rightarrow 2, 5, 8, ..., 359$ $S_3 \rightarrow 2, 7, 12, ..., 197$ Common terms of S_2 and S_3 are given by $S_4 \rightarrow 2, 17, 32, ..., a_n$ $a_n \le 197$ $2+15(n-1) \le 197$ $n \le 14$ $S_4 \rightarrow 2, 17, 32, ..., 197$ Common terms of S_4 and S_1 are given by 47, 107, 167Sum = 47 + 107 + 167 = 32189. The total number of six digit numbers, formed using the digits 4, 5, 9 only and divisible by 6, is _____.

Answer (81)

Sol. Units, place must be occupied by 4 and hence, at least one 4 must be there.

Possible combination of 4, 5, 9 are as follows

4	5	9		No. of Number
1	1	4	\rightarrow	$\frac{5!}{4!} = 5$
1	4	1	\rightarrow	$\frac{5!}{4!} = 5$
2	2	2	\rightarrow	$\frac{5!}{2!2!} = 30$
3	0	3		$\frac{5!}{2!3!} = 10$
3	3	0		$\frac{5!}{2!3!} = 10$
4	1	1		$\frac{5!}{3!} = 20$
6	0	0		$\frac{5!}{5!} = 1$ Total = 81

90. If
$$\int_{0}^{\pi} \frac{5^{\cos x} \left(1 + \cos x \cos 3x + \cos^2 x + \cos^3 x \cos 3x\right) dx}{1 + 5^{\cos x}} = \frac{k\pi}{16},$$

then k is equal to _____.

Answer (13)

Sol. Let $g(x) = 1 + \cos x \cos 3x + \cos^2 x + \cos^3 x \cos 3x$

Clearly,
$$g(\pi + x) = g(x)$$

$$I = \int_{0}^{\pi} \frac{5^{\cos x} (g(x))}{1 + 5^{\cos x}} dx \qquad \dots(i)$$

$$I = \int_{0}^{\pi} \frac{5^{\cos x} (g(x))}{1 + 5^{\cos x}} dx \left(\because \int_{0}^{\pi} f(x) dx = \int_{0}^{\pi} f(\pi - x) dx \right)$$

$$I = \int_{0}^{\pi} \frac{1}{1 + 5^{\cos x}} g(x \qquad \dots(ii)$$

$$(i) + (ii) \Rightarrow 2I = \int_{0}^{\pi} g(x) dx$$

$$2I = \int_{0}^{\pi} 1 + \cos x \cos 3x + \cos^{2} x + \cos^{3} x \cos 3x dx$$

$$= \int_{0}^{\pi} 1 + \frac{1}{2} (\cos 4x + \cos 2x) + \frac{1}{2} (1 + \cos 2x)$$

$$+ \frac{1}{4} (\cos 3x + 3 \cos x) \cos 3x dx$$

$$= \pi + \frac{1}{2} (0 + 0) + \frac{\pi}{2} + \frac{1}{2} (0)$$

$$\frac{1}{4} \int \cos^{2} 3x + 3 \cos x \cos 3x dx$$

$$= \frac{3\pi}{2} + \frac{1}{4} \int \frac{1}{2} (1 + \cos 6x) + \frac{3}{2} (\cos 4x + \cos 2x) dx$$

$$= \frac{3\pi}{2} + \frac{1}{4} \left(\frac{\pi}{2} + \frac{1}{2} \times 0 + \frac{3}{2} (0 + 0) \right) = \frac{3\pi}{2} + \frac{\pi}{8}$$

$$= \frac{13\pi}{8} \Big| \Rightarrow I = \frac{13\pi}{16} \Rightarrow k = 13 \Big|$$