

EX NAVODAYAN FOUNDATION

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12/04/2023 Morning

Answers & Solutions

Time : 3 hrs.

M.M. : 300

JEE (Main)-2023 (Online) Phase-2

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(Mathematics, Physics and Chemistry)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) The Test Booklet consists of 90 questions. The maximum marks are 300.
- (3) There are three parts in the question paper consisting of Mathematics, Physics and Chemistry having 30 questions in each part of equal weightage. Each part (subject) has two sections.
 - (i) **Section-A:** This section contains 20 multiple choice questions which have only one correct answer. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer.
 - (ii) Section-B: This section contains 10 questions. In Section-B, attempt any five questions out of 10. The answer to each of the questions is a numerical value. Each question carries 4 marks for correct answer and -1 mark for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

MATHEMATICS

3.

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

- The number of five-digit numbers, greater than 1. 40000 and divisible by 5, which can be formed using the digits 0, 1, 3, 5, 7 and 9 without repetition, is equal to
 - (1) 132 (2) 120
 - (3) 72 (4) 96

Answer (2)

Sol. Case I : Numbers start with 5

<u>0</u> = 4 × 3 × 2 = 24 $\overline{\downarrow}$ \downarrow 4 ways 3 ways 2 ways Case II: $\begin{array}{c} \underline{7} \\ \underline{1} \\ 4 \\ 4 \\ 3 \\ 2 \\ 2 \end{array} = 48$

Case III :

1

1

С

Total numbers = 120

Let a, b, c be three distinct real numbers, none 2. equal to one. If the vectors $a\hat{i} + \hat{j} + \hat{k}$, $\hat{i} + b\hat{j} + \hat{k}$ $\hat{i} + \hat{j} + c\hat{k}$ and are coplanar, then $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$ is equal to (1) 2 (2) -1 (3) -2 (4) 1 Answer (4) a 1 1 **Sol.** | 1 b 1 | = 0 1 1 C $a - 1 \ 1 - b \ 0$ $b-1 \ 1-c = 0$ 0

$$R_{1} \rightarrow R_{1} - R_{2}$$

$$R_{2} \rightarrow R_{2} - R_{3}$$

$$\Rightarrow (a-1)[c(b-1) - (1-c)] + 1[(1-b)(1-c)] = 0$$

$$\Rightarrow c(a-1)(b-1) - (a-1)(1-c) + (1-b)(1-c) = 0$$

$$\Rightarrow \frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1$$
3. Let be a sequence such that
 $a_{1} + a_{2} + ... + a_{n} = \frac{n^{2} + 3n}{(-1)(n+2)}$. If
 $28\sum_{k=1}^{10} \frac{1}{a_{k}} = p_{1} p_{2} p_{3} ... p_{m}$, where $p_{1}, p_{2} ..., p_{m}$ are
the first *m* prime numbers, then *m* is equal to
(1) 5
(2) 8
(3) 6
(4) 7
Answer (3)
Sol. $a_{n} = \frac{n^{2} + 3n}{(n+1)(n+2)} - \frac{(n-1)^{2} + 3(n-1)}{n(n+1)}$
 $= \frac{4}{n(n+1)(n+2)}$
 $\sum_{k=1}^{10} \frac{1}{a_{k}} = \frac{1}{4}\sum_{k=1}^{10} k(k+1)(k+2)$
 $= \frac{1}{16}\sum_{k=1}^{10} k(k+1)(k+2)(k+3) - (k-1)k(k+1)(k+2)$
 $\frac{1}{16}[(1\cdot2\cdot3\cdot4.-0) + (2\cdot3\cdot4\cdot5 - 1\cdot2\cdot3\cdot4)$
 $(10\cdot11\cdot12\cdot13 - 9\cdot10\cdot11\cdot12)]$
 $= \frac{1}{16}[10\cdot11\cdot12\cdot13] =$
 $\therefore 28\sum_{k=1}^{10} \frac{1}{a_{k}} = \frac{28 \times 5 \times 11 \times 3 \times 13}{2}$
 $= 2\cdot3\cdot5\cdot7\cdot11\cdot13$
 $\therefore m = 6]$

4. Let
$$A = \begin{bmatrix} 1 & \frac{1}{51} \\ 0 & 1 \end{bmatrix}$$
. If $B = \begin{bmatrix} 1 & 2 \\ - & -1 \end{bmatrix} A = \begin{bmatrix} 1 & -2 \\ 1 & 1 \end{bmatrix}$, then
the sum of all the elements of the matrix $\sum_{n=1}^{50} B^n$ is
equal to
(1) 75
(2) 125
(3) 50 (4) 100
Answer (4)
Sol. $\because \begin{bmatrix} 1M \\ -2 \\ - & -1 \end{bmatrix} \begin{bmatrix} - & -2 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
 $\therefore MN = I = NM$
 $B = MAN$
 $B = MAN$
 $B = MAN$
 $B = (MAN)^n = (MAN)^n (MAN) (MAN) ...$
 $= (MAR)^n MAN$
 $= MARN$
 $B = MAN$
 $B = (MAR)^n = (I + E)^n = I + E + \frac{n}{C_2}E^2$
 $= I + nE$
 $= \begin{bmatrix} 1 & \frac{n}{51} \\ 0 & 1 \end{bmatrix}$
 $Sol. $B = MA^nN = \begin{bmatrix} 1 & \frac{n}{51} \\ -\frac{5}{5251} \end{bmatrix} = \begin{bmatrix} 75 & 25 \\ -5 & 25 \end{bmatrix}$
 $\therefore Sum = 100$
 $A = Sum = 10$
 $B = MAR$
 $A = 0 = 0$
 $A = 0$$

Equation of tangent at (-1, -1) (y + 1) = 3(x + 1) y = 3x + 2 ...(ii) Solving (i) and (ii) $x^3 = 3x + 2$ $x^3 - 3x - 2 = 0$ a = 2 Q(2, 8)Required area $= \int_{-}^{2} (3x + 2 - x^3) dx$ $= \frac{3}{2}(4 - 1) + 2(2 + 1) - \frac{1}{4}(16 - 1)$ $= \frac{27}{4}$ If the total maximum value of the function

7.

 $f(x) = \left(\frac{\sqrt{3e}}{2\sin x}\right)^{\sin^2 x}, x \in \left(0, \frac{\pi}{2}\right), \text{ is } \frac{k}{e}, \text{ then}$ $\left(\frac{k}{e}\right)^8 + \frac{k^8}{e^5} + k^8 \text{ is equal to}$ $(1) \ e^3 + e^6 + e^{11}$ $(2) \ e^5 + e^6 + e^{11}$ $(3) \ e^3 + e^6 + e^{10}$ $(4) \ e^3 + e^5 + e^{11}$ Answer (1)

Sol.
$$f(x) = \left(\frac{\sqrt{3}e}{2\sin x}\right)^{\sin^2 x}$$
$$\begin{vmatrix} 2\sin x \cos x \ln\left(\frac{\sqrt{3}e}{2\sin x}\right) + f'(x) = f(x) \\ \sin^2 x \frac{1 \times 2\sin x}{\sqrt{3}e} \times \frac{\sqrt{3}e}{2} - \frac{1}{\sin^2 x} \times \cos x \end{vmatrix}$$
$$= f(x) \sin 2x \ln\left(\frac{\sqrt{3}e}{2\sin x}\right) - \sin x \cos x \end{vmatrix} = 0$$

Sin
$$2x = 0$$
 (not possible)

$$\ln\left(\frac{\sqrt{3}e}{2\sin x}\right) = +\frac{1}{2}$$
$$\frac{\sqrt{3}e}{2\sin x} = e + \frac{1}{2}$$
$$\sin x = \frac{\sqrt{3}}{2}$$
$$f_{\text{max}} = (e)^{\frac{3}{8}} = \frac{c^{\frac{11}{8}}}{e} \Rightarrow k = e^{\frac{17}{8}}$$
$$\left(\frac{k}{e}\right)^{8} + \frac{8}{e^{5}} + k^{8} = e^{3} + e^{6} + e^{11}$$

- 8. Let α , β be the roots of the quadratic equation $x^2 + \sqrt{6}x + 3 = 0$. Then $\frac{\alpha^{23} + \beta^{23} + \alpha^{14} + \beta^{14}}{\alpha^{15} + \beta^{15} + \alpha^{10} + \beta^{10}}$ is equal to (1) 81
 - (1) 81
 (2) 9
 (3) 72
 (4) 729

Answer (2)

Sol.
$$\frac{\alpha^{23} + \beta^{23} + \alpha^{14} + \beta^{14}}{\alpha^{15} + \beta^{15} + \alpha^{10} + \beta^{10}}$$

Let $a_n = \alpha^n + \beta^n$
$$= \frac{a_{23} + a_{14}}{a_{15} + a_{10}}$$
$$x^2 + \sqrt{6}x + 3 = 0$$
$$\beta$$
$$x = \frac{-\sqrt{6} \pm \sqrt{-6}}{2}$$
$$= \sqrt{6} \left(\frac{-1 \pm i}{2}\right)$$
$$= \sqrt{3} \left(\frac{-1 \pm i}{\sqrt{2}}\right)$$
$$\alpha = \sqrt{3} e^{\frac{i3\pi}{4}}$$

$$\beta = \sqrt{3} e^{\frac{i5\pi}{4}}$$

$$\beta = \sqrt{3} e^{\frac{i5\pi}{4}}$$

$$\frac{\alpha^{23} + \beta^{23} + \alpha^{14} + \beta^{14}}{\alpha^{15} + \beta^{15} + \alpha^{10} + \beta^{10}}$$

$$= 9 \left(\frac{(\sqrt{3})^9}{(\sqrt{3})^5} \left(\frac{e^{i23x\frac{3\pi}{4}} + e^{i23x\frac{5\pi}{4}}}{(\sqrt{3})^5} \right) + \left(\frac{e^{i14x\frac{3\pi}{4}} + e^{i4x\frac{5\pi}{4}}}{(\sqrt{3})^5 + e^{i15x\frac{5\pi}{4}}} \right) \right)$$

$$= \left(\frac{(\sqrt{3})^9 \left(\frac{1 + i - 1 + i}{\sqrt{2}} \right) + 0}{(\sqrt{3})^5 \left(\frac{i - 1 + i}{\sqrt{2}} \right) + 0} \right) \times 9$$

$$= 81$$
9. Let the lines $l_1 : \frac{x + 5}{3} = \frac{y + 4}{1} = \frac{z - \alpha}{-2}$ and $l_2 : 3x + 2y + z - 2 = 0 = x - 3y + 2z - 13$ be coplanar. If the point $P(a, b, c)$ on l_1 is nearest to the point $Q(-4, -3, 2)$, then $|a| + |b| + |c|$ is equal to (1) 12 (2) 14
(3) 8 (4) 10
Answer (4)
Sol. for $P_2 : \overline{n_2} = \begin{vmatrix} \hat{i} & \hat{j} & k \\ 3 & 2 & 1 \\ 1 & -3 & 2 \end{vmatrix}$

$$= \hat{i}(7) - \hat{j}(5) + k(-11)$$
Let R lies on k
Let $z = 0$
 $\therefore 3x + 2y = 2$

x - 3y = 13

$$\therefore 11y = -39 + 2 = -37$$

$$\therefore y = \frac{-37}{11}$$

$$\therefore x = 13 + 3y$$

$$= 13 - \frac{37 \times 3}{11}$$

$$= \frac{143 - 111}{11} = \frac{32}{11}$$

$$\therefore R\left(\frac{32}{11}, \frac{-37}{11}, 0\right)$$

$$h \& k \text{ are coplanar}$$

$$\left(\begin{array}{c} -\frac{32}{11} & -4 + \frac{37}{11} & \alpha\\ 3 & 1 & -2\\ 7 & -5 & -11\end{array}\right) = 0$$

$$= \left|\frac{-87}{11} & \frac{-7}{11} & \alpha\\ 3 & 1 & -2\\ 7 & -5 & -11\end{array}\right| = 0$$

$$\Rightarrow \alpha = 7$$

$$\therefore P(3k - 5, k - 4, -2k + 7) \text{ is nearest to } (-4, -3, 2)$$

$$Q(-4, -3, 2)$$

10. Let
$$P\left(\frac{2\sqrt{3}}{\sqrt{7}}, \frac{6}{\sqrt{7}}\right)$$
, *Q*, *R* and *S* be four points on the ellipse $9x^2 + 4y^2 = 36$. Let *PQ* and *RS* be mutually perpendicular and pass through the origin. If $\frac{1}{(PQ)^2} + \frac{1}{(RS)} = \frac{p}{q}$, where *p* and *q* are coprime, then $p + q$ is equal to
(1) 147
(2) 143
(3) 137
(4) 157

Answer (4)

Sol.
$$OP = r_1 = \sqrt{\left(\frac{2\sqrt{3}}{\sqrt{7}}\right)^2 + \left(\frac{6}{\sqrt{7}}\right)^2} = \sqrt{\frac{48}{7}}$$

Let P be $(r_1 \cos\theta, r_1 \sin\theta)$

P lies on ellipse

$$\frac{r_1^2 \cos^2 \theta}{4} + \frac{r_1^2 \sin^2 \theta}{9} = 1$$
$$\Rightarrow \quad \frac{\cos^2 \theta}{4} + \frac{\sin^2 \theta}{9} = \frac{7}{48} \qquad \dots (i)$$

Let R be $(-r_2 \sin\theta, r_2 \cos\theta)$

$$\frac{r_2^2 \sin^2 \theta}{4} + \frac{r_2^2 \cos^2 \theta}{9} = 1$$
$$\Rightarrow \quad \frac{\sin^2 \theta}{4} + \frac{\cos^2 \theta}{9} = \frac{1}{r_2^2}$$

From (i)

$$\frac{1}{r_2^2} = \frac{1}{4} + \frac{1}{9} - \frac{7}{48} = \frac{31}{144}$$
$$\frac{1}{PQ^2} + \frac{1}{RS^2} = \frac{1}{4} \left(\frac{1}{r_1^2} + \frac{1}{r_2^2} \right)$$
$$= \frac{1}{4} \left(\frac{7}{48} + \frac{31}{144} \right) = \frac{13}{144} = \frac{p}{m}$$
$$\therefore \quad p + m = 157$$
Option (4) is correct.

11. Two dice A and B are rolled. Let the numbers obtained on A and B be α and β respectively. If the variance of $\alpha - \beta$ is $\frac{p}{q}$, where *p* and *q* are co-prime, then the sum of the positive divisors of p is equal to (1) 72 (2) 36 (3) 48 (4) 31 Answer (3) **Sol.** $\alpha \in \{1, 2, 3, 4, 5, 6\}$ $\beta \in \{1, 2, 3, 4, 5, 6\}$ $(\alpha - \beta) = 0$ (6 case) $(\alpha - \beta) = -1$ (5 case) $(\alpha - \beta) = -2$ (4 case) $(\alpha - \beta) = -3$ (3 case) $(\alpha - \beta) = -4$ (2 case) $(\alpha - \beta) = -5$ (1 case) $(\alpha - \beta) = 1$ (5 case) $(\alpha - \beta) = 2$ (4 case) $(\alpha - \beta) = 3$ (3 case) $(\alpha - \beta) = 4$ (2 case) $(\alpha - \beta) = 5$ (1 case) Mean = 0 $0^2 \times 6 + 2 \times 1^2 \times 5 + 2 \times 2^2 \times 4 +$

Volume =
$$\sigma^2 = \frac{2 \times 3^2 \times 3 + 2 \times 4^2 \times 2 \times 5^2 \times 1}{36}$$

$$=\frac{2}{36}\times\left(5+16+27+32+25\right)=\frac{105}{18}=\frac{35}{6}$$

 $\therefore p = 35$ Sum of divisors of p = 1 + 5 + 7 + 35 = 48Option (3) is correct.

12. Let the plane P: 4x - y + z = 10 be rotated by an angle $\frac{\pi}{2}$ about its line of intersection with the plane x + y - z = 4. If α is the distance of the point (2, 3, -4) from the new position of the plane *P*, then 35α is equal to (1) 85 (2) 105

(3)	126	(4)	90
• • •		()	

Sol. Equation of plane after rotation : $(4x - y + z - 10) + \lambda(x + y - z - y) = 0$ $\Rightarrow (4+\lambda)x + y(\lambda-1) + z(1-\lambda) - 4\lambda - 10 = 0$ $\overrightarrow{n_1} \cdot \overrightarrow{n_2} = 0$ $\Rightarrow (4 + \lambda)4 + (\lambda - 1)(-1) + (1 - \lambda)1 = 0$ \Rightarrow 16 + 4 λ - λ + 1 + 1 - λ = 0 $\Rightarrow 2\lambda = -18$ $\Rightarrow \lambda = -9$ \therefore equation of plane : -5x - 10y + 10z + 26 = 0Distance of plane from (2, 3, -4) $=\left|\frac{-10-30-40+26}{\sqrt{100+100+26}}\right|=\frac{54}{15}=\alpha$ $35\alpha = 35 \cdot \frac{54}{15} = 7 \times \frac{54}{2} = 7 \times 18 = 126$ Option (3) is correct. 13. Let $\lambda \in \mathbb{Z}$, $\vec{a} = \lambda \hat{i} + \hat{j} - \hat{k}$ and $\vec{b} = 3\hat{i} - \hat{j} + 2\hat{k}$. Let \vec{c} be a vector such that $\left(\vec{a}+\vec{b}+\vec{c}\right)\times\vec{c}=\vec{0},\,\vec{a}\cdot\vec{c}=-17$ and $\vec{b}\cdot\vec{c}=-20$. Then $\left| \vec{c} \times (\lambda \hat{i} + \hat{j} + \hat{k}) \right|^2$ is equal to (1) 46 (2) 53 (3) 62 (4) 49 Answer (1) **Sol.** $\vec{a} = \lambda \hat{i} + \hat{j} - \hat{k}$ $\vec{b} = 3\hat{i} - \hat{i} + 2\hat{k}$ $k(\vec{a}+\vec{b})=\vec{c}$ $\vec{a} \cdot \vec{c} = -17$ $\vec{b} \cdot \vec{c} = -20$ $k(\lambda^2 + 3\lambda - 1) = -17$ $k(3\lambda + 11) = -20$ $\lambda = 3, \frac{-69}{20}$

For $\lambda = 3$, k = -1 $\vec{c} = -1(\vec{a} + \vec{b})$ $= -((\lambda + 3)\hat{i} + \hat{i}) = -6\hat{i} - \hat{k}$ $\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -6 & 0 & -1 \\ & & \ddots & 2 \end{vmatrix} = \hat{i} - 3\hat{j} + 6\hat{k}$ $\left|\vec{c} \times (\lambda \hat{j} + \hat{j} + \hat{k})\right|^2 = 46$ 14. Let D be the domain of the function $f x = \sin^{-1} \left(\log_{3x} \left(\frac{6 + 2\log_3 x}{-5x} \right) \right)$. If the range of the function $g: D \to \mathbb{R}$ defined by g(x) = x - [x], ([x] is the greatest integer function), is (α, β) , then $\alpha^2 + \frac{5}{\beta}$ is equal to (1) 135 (2) 45 (3) 46 (4) 136 Answer (*) **Sol.** $f(x) = \sin^{-1} \left(\log_{3x} \left(\frac{6 + 2\log_3 x}{-5x} \right) \right)$ $\log_{3x}\left(\frac{6+2\log_{3} x}{-5x}\right) \in \begin{bmatrix}-1,1\\-(1)\end{bmatrix}, \ 3x > 0, \ 3x \neq 1, \ \frac{6+2\log_{3} x}{-5x} > 0$ \Rightarrow From (2), x > 0, from (3), $x \neq \frac{1}{3}$ From (4), $6 + 2 \log_3 x < 0$ (:: x > 0) $\log_3 x < -3$ $\Rightarrow x < 3^{-3}$ $\Rightarrow \left[x < \frac{1}{27}\right]$ ⇒ From (2), (3), (4), $0 < x < \frac{1}{27}$...(5) From (1), $-1 \le \log_{3x} \left(\frac{6 + 2\log_3 x}{-5x} \right) \le 1$ $\therefore 3x \in \left(0, \frac{1}{9}\right)$

$$\Rightarrow \frac{1}{3x} \ge \frac{6+2\log_3 x}{-5x} \ge 3x$$

$$\Rightarrow -\frac{5}{3} \le 6+2\log_3 x \le -15x^2$$

$$\Rightarrow -\frac{23}{6} \le \log_3 x \le \frac{-15x^2-6}{2}$$

$$\Rightarrow 3^{\frac{23}{6}} \le x \le 3^{\frac{-15x^2-6}{2}}$$

$$\Rightarrow \frac{1}{\frac{23}{36}} \le x \le 3^{\frac{-15x^2-6}{2}}$$

$$\Rightarrow \frac{1}{\frac{23}{36}} \le x \le \frac{1}{32}$$
 ...(6)
From (5) & (6), $0 < x < \frac{1}{27}$, $[x] = 0$

$$\Rightarrow g(x) = x$$

$$\Rightarrow \text{ Range } g(x) \text{ is domain of } f(x)$$
15. If the point $\left[\alpha, \frac{7\sqrt{3}}{3}\right]$ lies on the curve traced by the mid-points of the line segments of the lines $x\cos\theta + y\sin\theta = 7, \theta \in \left(0, \frac{\pi}{2}\right)$ between the co-ordinates axes, then α is equal to
(1) -7 (2) $-7\sqrt{3}$
(3) $7\sqrt{3}$ (4) 7
Answer (4)
Sol.
 $\int \left(0, \frac{7}{2\cos\theta}, \frac{7}{2\sin\theta}\right) = (h, k)$
 $\therefore \cos\theta = \frac{7}{2h}$ $\sin\theta = \frac{7}{2k}$
 $\therefore \theta \in \left(0, \frac{\pi}{2}\right)$

$$\therefore \text{ Locus } = \frac{1}{x^2} + \frac{1}{y^2} = \frac{4}{49}$$

$$\left(\alpha, \frac{7\sqrt{3}}{3}\right) \text{ lies on curve}$$

$$\frac{1}{\alpha^2} + \frac{9}{147} = \frac{4}{49}$$

$$\frac{1}{\alpha^2} = \frac{1}{49}$$

$$\therefore \alpha = \pm 7$$

$$\therefore \alpha = 7$$
16. Let $y = y(x), y > 0$, be a solution curve of the differential equation $(1 + x^2) dy = y(x - y) dx$. If $y(0) = 1$ and $y(2\sqrt{2}) = \beta$, then

(1)
$$e^{3\beta^{-1}} = e(3+2\sqrt{2})$$

(2) $e^{3\beta^{-1}} = e(5+\sqrt{2})$
(3) $e^{\beta^{-1}} = e^{-2}(3+2\sqrt{2})$
(4) $e^{\beta^{-1}} = e^{-2}(5+\sqrt{2})$

Sol.
$$(1+x^2)dy = y(x-y)dx$$

$$\frac{dy}{dx} = \frac{x}{1+x^2}y - \frac{y^2}{1+x^2}$$

$$\frac{-1}{y^2}\frac{dy}{dx} + \frac{x}{1+x^2} \cdot \frac{1}{y} = \frac{1}{1+x^2}$$
Let $\frac{1}{y} = t$

$$\frac{-1}{y^2}y' = \frac{dt}{dx}$$

$$\therefore \quad \frac{dt}{dx} + \frac{x}{1+x^2}t = \frac{1}{1+x^2}$$

$$\mathsf{IF} = e^{\int \frac{x}{1+x^2}dx} = \sqrt{1+x^2}$$

$$t\sqrt{1+x^2} = \int \frac{\sqrt{1+x^2}}{1+x^2}dx$$

$$\frac{1}{y}\sqrt{1+x^2} = \int \frac{1}{\sqrt{1+x^2}} dx$$

$$\frac{1}{y}\sqrt{1+x^2} = \ln(x+\sqrt{x}+1) + C$$

$$\therefore \quad y(0) = 1 \implies C = 1$$

$$\frac{1}{y}\sqrt{1+x^2} = \ln(x+\sqrt{x^2+1}) + 1$$

For $y = 2\sqrt{2}$
$$\frac{3}{y} = \ln|2\sqrt{2}+3| + 1$$

$$y = \beta = \frac{3}{1+\ln|2\sqrt{2}+3|}$$

$$\implies 3\beta^{-1} = 1 + \ln|2\sqrt{2}+3|$$

$$e^{3\beta^{-1}} = e^{|2\sqrt{2}+3|}$$

17. In a triangle *ABC*, if $\cos A + 2 \cos B + \cos C = 2$ and the lengths of the sides opposite to the angles *A* and *C* are 3 and 7 respectively, then $\cos A - \cos C$ is equal to

(1)
$$\frac{9}{7}$$
 (2) $\frac{10}{7}$
(3) $\frac{5}{7}$ (4) $\frac{3}{7}$

Answer (2)

Sol.
$$\cos A + 2\cos B + \cos C = 2$$

 $\cos A + \cos C = 2(1 - \cos B)$
 $2\cos \frac{A+C}{2}\cos\left(\frac{A-C}{2}\right) = 2 \times 2\sin^2 \frac{B}{2}$
 $\cos \frac{A-C}{2} = 2\sin \frac{B}{2}$
 $2\cos \frac{B}{2}\cos \frac{A-C}{2} = 4\sin \frac{B}{2}\cos \frac{B}{2}$
 $2\sin\left(\frac{A+C}{2}\right)\cos\left(\frac{A-C}{2}\right) = 2\sin B$
 $\sin A + \sin C = 2\sin B$
 $a + c = 2b$
 $\Rightarrow b = 5$ ($\because a = 3, c = 7$)
 $\cos A - \cos C = \frac{25 + 49 - 9}{70} - \frac{9 + 25 - 49}{30} = \frac{10}{7}$

18. Let *C* be the circle in the complex plane with centre $z_0 = \frac{1}{2}(1+3i)$ and radius r = 1. Let $z_1 = 1+i$ and the complex number z_2 be outside circle *C* such that $|z_1 - z_0||z_2 - z_0| = 1$. If z_0 , z_1 and z_2 are collinear, then the smaller value of $|z_2|^2$ is equal to $(1) \quad \frac{5}{2} \qquad (2) \quad \frac{7}{2}$

(1) 2 (2) 2
(3)
$$\frac{13}{2}$$
 (4) $\frac{3}{2}$

Answer (1)

Sol.
$$z_0 = \frac{1+3i}{2}, \ z_1 = (1+i)$$

 $|z_1 - z_0| |z_2 - z_0| = 1$
 $\frac{1}{\sqrt{2}} |z_2 - z_0| = 1$
 $\Rightarrow |z_2 - z_0| = \sqrt{2}$
 $\frac{z_2 - z_0}{z_1 - z_0} = \frac{|z_2 - z_0|}{|z_1 - z_0|} (\pm 1) = \pm$
 $z_2 = z_0 \pm 2(z_1 - z_0)$
 $z_2 = 2z_1 - z_0 = \frac{3}{2} + \frac{1}{2}i \Rightarrow |z_2|^2 = \frac{5}{2}$
OR

$$z_2 = 3z_0 - 2z_1 = \frac{-1}{2} + \frac{5}{2}i \Rightarrow |z_2|^2 = \frac{13}{2}$$

19. Among the two statements

$$(S_1): (p \Rightarrow q) \land (p \land (\sim q)) \text{ is a contradiction and}$$
$$(S_2): (p \land q) \lor ((\sim p) \land q) \lor (p \land (\sim q))$$
$$\lor ((\sim p) \land (\sim q)) \text{ is a tautology}$$
(1) only (S₂) is true

(2) only (S_1) is true

- (3) both are false
- (4) both are true

Sol.
$$S_1 : (p \Rightarrow q) \land (p \land \neg q)$$

$$\equiv (\neg p \lor q) \land (p \land \neg q)$$

$$\equiv (\neg p \land p \land \neg q) \lor (q \land p \land \neg q)$$

$$\equiv (f \land \neg q) \lor (f \land p)$$

$$\equiv f \lor f \equiv t$$

$$S_2 : (p \land q) \lor (\neg p \land q) \lor (p \land \neg q) \lor (\neg p \land \neg q)$$

$$\equiv ((p \lor \neg p) \land q) \lor ((p \lor \neg p) \land \neg q)$$

$$\equiv (t \land q) \lor (t \land \neg q) \equiv q \lor \neg q \equiv t$$

20. The sum, of the coefficients of the first 50 terms in the binomial expansion of $(1 - x)^{100}$, is equal to

(1)	$^{101}C_{50}$	(2)	⁹⁹ C ₄₉
(3)	$-^{101}C_{50}$	(4)	- ⁹⁹ C ₄₉

Answer (4)

Answer (64)

Sol.

$$\begin{cases}
\begin{pmatrix}
^{100}C_0 & -^{100}C_1 & +^{100}C_2 & - \dots & -^{100}C_{49} \\
& + (-^{100}C_{51} & +^{100}C_{52} & - \dots & +^{100}C_{100} \\
& \lambda_1 & +^{100}C_{50} & +\lambda_2 &= 0 \\
& \lambda_1 &= -\frac{1}{2} & ^{100}C_{50} & (\because \lambda_1 &= \lambda_2) \\
& = -^{99}C_{49}
\end{cases}$$

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. Let
$$I(x) = \int \sqrt{\frac{x+7}{x}} dx$$
 and $I(9) = 12 + 7\log_{e}7$. If
 $I(1) = \alpha + 7\log_{e}(1 + 2\sqrt{2})$, then α^{4} is equal to

Sol.
$$l(x) = \int \sqrt{\frac{x+7}{x}} dx$$

 $\frac{x+7}{x} = t^2 \Rightarrow -\frac{7}{x^2} dx = 2t dt$
 $dx = \frac{-14t}{(t^2-1)^2} dt$
 $l(x) = -1 \int \frac{t^2}{(t^2-1)^2} dt$
 $= -14 \int \frac{dt}{(t^2+\frac{1}{t^2}-2)} = \frac{-14}{2} \int \frac{1}{(t+\frac{1}{t})^2-4} + \frac{(1+\frac{1}{t^2})}{(t+\frac{1}{t})^2} dt$
 $l(x) = -7 \left| \frac{1}{4} \ln \left| \frac{t+\frac{1}{t}-2}{t+\frac{1}{t}+2} \right| - \frac{1}{t-\frac{1}{t}} \right| + c$
when $x = 9, t = \frac{4}{3}$
 $\Rightarrow 12+7 \ln 7 = \frac{-7}{4} \ln \left(\frac{1}{7} \right)^2 + 7 \times \frac{12}{7} + c$
 $\Rightarrow c = \frac{7}{2} \ln 7$
when $x = 1, t = 2\sqrt{2}$
 $\Rightarrow l(1) = +\frac{7}{4} \ln \left(\frac{2\sqrt{2}+1}{2\sqrt{2}-1} \right)^2 + 7 \times \frac{2\sqrt{2}}{7} + \frac{7}{2} \ln 7$
 $= \frac{7}{2} \ln \left(\frac{(2\sqrt{2}+1)^2}{7} \right) + 2\sqrt{2} + \frac{7}{2} \ln 7$
 $a = 2\sqrt{2} \Rightarrow \frac{a^4 = 64}{3}$
22. If $\int_{-0.15}^{0.15} |100x^2 - 1| dx = \frac{k}{3000}$, then k is equal to

Answer (575)

JEE (Main)-2023 : Phase-2 (12-04-2023)-Morning

Sol.
$$\int_{-0.15}^{0.15} |100x^2 - 1| dx = 2 \int_{0}^{0.15} |100x^2 - 1| dx$$
$$= 2 \int_{0}^{0.1} (-100x^2 + 1) dx + 2 \int_{0.1}^{0.15} (100x^2 - 1) dx$$
$$= 2 \cdot \left(\frac{-100x^3}{3} + x \right)_{0}^{0.1} + 2 \left(\frac{100x^3}{3} - x \right)_{0.1}^{0.15}$$
$$= 4 \left(-\frac{1}{30} + \frac{1}{10} \right) + 2 \left(\frac{9}{80} - \frac{3}{20} \right)$$
$$= \frac{8}{30} - \frac{3}{40} = \frac{575}{3000} \Rightarrow k = 575$$

23. Let [x] be the greatest integer $\leq x$. Then the number of points in the interval (-2, 1) where the function $f(x) = |[x]| + \sqrt{x - [x]}$ is discontinuous, is _____.

Answer (2)

Sol. $f(x) = |[x]| + \sqrt{x - [x]}$ $x - [x] \ge 0 \Rightarrow x \in R$ $f(x) = \begin{cases} 2 + \sqrt{+2}, -2 < x < -1 \\ 1 + \sqrt{x + 1}, -1 \le x < 0 \\ \sqrt{x}, & 0 \le x < 1 \end{cases}$ (-2, 2)

f(x) is discontinuous at two points $x = \{-1, 0\}$

24. Two circles in the first quadrant of radii r_1 and r_2 touch the coordinate axes. Each of them cuts off an intercept of 2 units with the line x + y = 2. Then $r_1^2 + r_2^2 - r_1r_2$ is equal to _____.

Answer (07.00)



25. Let the positive numbers a_1 , a_2 , a_3 , a_4 and a_5 be in a G.P. Let their mean and variance be $\frac{31}{10}$ and $\frac{m}{n}$ respectively, where *m* and *n* are co-prime. If the mean of their reciprocals is $\frac{31}{10}$ and $a_3 + a_4 + a_5 = 14$, then m + n is equal to _____.

Answer (211.00)

Sol.
$$a + ar + ar^2 + ar^3 + ar^4 = \frac{31}{10} \cdot 5 = \frac{31}{2}$$

$$\frac{a(r^5 - 1)}{r - 1} = \frac{31}{2} \qquad \dots (i)$$

$$\frac{1}{a} \left(1 + \frac{1}{r} + \frac{1}{r^2} + \frac{1}{r^3} + \frac{1}{r^4} \right) = \frac{31}{40} \cdot 5 = \frac{31}{8}$$

$$\frac{1}{a} \left(\frac{1 - \left(\frac{1}{r}\right)^5}{1 - \frac{1}{r}} \right) = \frac{31}{8}$$
or $\frac{1}{a} \left(\frac{r^5 - 1}{r - 1} \right) \frac{1}{r^4} = \frac{31}{2} \qquad \dots (ii)$

JEE (Main)-2023 : Phase-2 (12-04-2023)-Morning

$$\frac{1}{a} \cdot \frac{31}{2a} \cdot \frac{1}{r^4} = \frac{31}{8}$$

$$\boxed{ar^2 = 2}$$
From (i)
$$\frac{2}{r^2} \left(\frac{r^5 - 1}{r - 1}\right) = \frac{31}{2}$$

$$\frac{1 + r + r^2 + r^3 + r^4}{r^2} = \frac{31}{4}$$

$$\left(r^2 + \frac{1}{r^2}\right) + \left(r + \frac{1}{r}\right) = \frac{27}{4}$$

$$t^2 - 2 + t = \frac{27}{4}$$

$$4t^2 + 4t - 35 = 0$$

$$4t^2 + 14t - 10t - 35 = 0$$

$$(2t - 5)(2t + 7) = 0$$

$$t = \frac{5}{2}, \frac{-7}{2} \Rightarrow \boxed{r = 2}$$

$$r = 2, a = \frac{1}{2}$$
Variance of data set $\left\{\frac{1}{2}, 1, 2, 4, \frac{1}{2}, \frac{341}{5} - \left(\frac{31}{10}\right)^2$

$$= \frac{341}{20} - \frac{961}{100} = \frac{1705 - 961}{100}$$

8

From (i) and (ii)

 $=\frac{744}{100}=\frac{186}{25}$

26. Let
$$D_k = \begin{vmatrix} 1 & 2 & 2k-1 \\ n & n^2 + n + 2 & n^2 \\ n & n^2 + n & n^2 + n + 2 \end{vmatrix}$$
. If $\sum_{k=1}^n D_k = 96$
then *n* is equal to ______.
Answer (06.00)
Sol. $\sum_{k=1}^n D_k = \begin{vmatrix} \sum 1 & 2\sum k & 2\sum k - \sum 1 \\ n & n^2 + n + 2 & n^2 \\ n & n^2 + n & n^2 + n + 2 \end{vmatrix}$
$$= \begin{vmatrix} n & n(n+1) & n^2 \\ n & n^2 + n & n^2 + n + 2 \\ n & n^2 + n & n^2 + n + 2 \end{vmatrix}$$
$$= \begin{vmatrix} 0 & -2 & 0 \\ 0 & 2 & -n - 2 \\ n & n^2 + n & n^2 + n + 2 \end{vmatrix}$$
$$= 2((-n) (-n-2)) = 96$$
 $n^2 + 2n = 48$ $n = 6, -8$ $\boxed{n=6}$

27. A fair n (n > 1) faces die is rolled repeatedly until a number less than n appears. If the mean of the number of tosses required is $\frac{n}{9}$, then n is equal to

Answer (10)

Sol.
$$x_i$$
 1 2 3 4 ...
 $p_i \frac{n-1}{n} \frac{1}{n} \cdot \left(\frac{n-1}{n}\right) \frac{1}{n^2} \cdot \frac{n-1}{n} \frac{1}{n^3} \cdot \left(\frac{n-1}{n}\right) \dots$
Mean $= \sum_{i=1}^{\infty} p_i x_i = 1 \cdot \frac{n-1}{n} + \frac{2}{n} \cdot \left(\frac{n-1}{n}\right) + \frac{3}{n^2} \left(\frac{n-1}{n}\right) + \dots$
 $\frac{n}{9} = \left(1 - \frac{1}{n}\right) S \dots (i)$
where $S = 1 + \frac{2}{n} + \frac{3}{n^2} + \frac{4}{n^3} + \dots$
 $\frac{1}{n} S = \frac{1}{n} + \frac{2}{n^2} + \frac{3}{n^3} + \dots$
 $\left(1 - \frac{1}{n}\right) S = 1 + \frac{1}{n} + \frac{1}{n^2} + \frac{1}{n^3} + \dots$

$$\left(1-\frac{1}{n}\right)S = \frac{1}{1-\frac{1}{n}}$$
$$\Rightarrow \quad \frac{n}{9} = \left(1-\frac{1}{n}\right) \times \frac{1}{\left(1-\frac{1}{n}\right)^2} = \frac{n}{n-1}$$

 $\Rightarrow n = 10$

28. The number of relations, on the set {1, 2, 3} containing (1, 2) and (2, 3), which are reflexive and transitive but not symmetric, is _____.

Answer (4)

Sol. $(1, 1), (2, 2), (3, 3) \in R$

Since $(1, 2), (2, 3) \in R, (1, 3)$ must $\in R$

Possible cases :

Case-1: All of (2, 1), (3, 2), (3, 1) $\notin R \rightarrow 1$ relation. **Case-2**: Only one of (2, 1), (3, 2), (3, 1) $\in R \rightarrow 3$ relations.

Note that exactly two of (2, 1), (3, 2), (3, 1) $\in R$ is not possible because if two of these $\in R$, third must $\in R$ to make relation transitive.

Total number of relations = 4

29. Let the plane x + 3y - 2z + 6 = 0 meet the co-ordinate axes at the points *A*, *B*, *C*. If the orthocenter of the triangle *ABC* is $\left(\alpha, \beta, \frac{6}{7}\right)$, then

 $98(\alpha + \beta)^2$ is equal to _____.

Answer (288)



$$(x-0) \times 0 + (+1) \times 2 + \left(z - \frac{3}{2}\right) \times 3 = 0$$

$$\Rightarrow 4y + 6z - 5 = 0 \qquad \dots(i)$$

$$(x+3) \times (-6) + (y-0) \times 0 + \left(z - \frac{3}{2}\right) (-3) = 0$$

$$\Rightarrow 4x + 2z + 9 = 0 \qquad \dots(ii)$$

$$\Rightarrow (x+3) \times (-6) + (y+1) \times 2 + (z-0) \times 0 = 0$$

$$\Rightarrow 3x - y + 8 = 0 \qquad \dots(iii)$$

From (i), (ii), (iii),

$$x = \frac{-9}{4} - \frac{z}{2}, y = \frac{5}{4} - \frac{3}{2}z, z = z$$

$$\begin{pmatrix} 1 & 2 \\ 0' & G \\ -\frac{9}{4} - \frac{z}{2}, \frac{5}{4} - \frac{3}{2}z, z \end{pmatrix} \qquad (-2, \frac{-2}{3}, 1) \qquad (\alpha, \beta, \frac{6}{7})$$

$$\Rightarrow G = \left(\frac{\alpha - \frac{9}{2} - z}{3}, \frac{\beta + \frac{5}{2} - 3z}{3}, \frac{6}{7} + 2z}{3}\right)$$

$$\Rightarrow z = \frac{15}{14}, \alpha = -\frac{3}{7}, \beta = -\frac{9}{7}$$

$$\Rightarrow 98(\alpha + \beta)^2 = 98 \times \frac{144}{49} = 288$$

30. Let the digits *a*, *b*, *c* be in A.P. Nine-digit numbers are to be formed using each of these three digits thrice such that three consecutive digits are in A.P. at least once. How many such numbers can be formed?

Answer (1260)

Sol. Digits are in A.P. at least once



Total ways of selecting 3 consecutive places out of 9 places is 7.

Total ways =
$$\frac{{}^7C_1 \times 2 \times 6!}{2! \times 2! \times 2!} = 1260$$

PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

31. A proton and an α -particle are accelerated from rest by 2 V and 4 V potentials, respectively. The ratio of their de-Broglie wavelength is :

(1) 8:1	(2) 2:1
---------	---------

Answer (3)

Sol.
$$\frac{\lambda_p}{\lambda_a} = \frac{\sqrt{m_a}}{\sqrt{m_p}} \times \sqrt{\frac{q_a 4}{q_p 2}}$$

= 2 × 2

32. Given below are two statements: one is labelled as **Assertion A** and the other is labelled as **Reason R**

Assertion A : EM waves used for optical communication have longer wavelengths than that of microwave, employed in Radar technology.

Reason R : Infrared EM waves are more energetic than microwaves, (used in Radar)

In the light of given statements, choose the *correct* answer from the options given below.

- (1) Both A and R are true but R is NOT the correct explanation of A
- (2) A is false but R is true
- (3) A is true but R is false
- (4) Both A and R are true and R is the correct explanation of A

Answer (2)

Sol. Assertion is false

as $\lambda_{optical} < \lambda_{microwave}$

33. If the r.m.s speed of chlorine molecule is 490 m/s at 27°C, the r.m.s speed of argon molecules at the same temperature will be (Atomic mass of argon = 39.9 u, molecular mass of chlorine = 70.9 u)

(1) 55	51.7 m/s	(2)	651.7 m/s
(3) 45	51.7 m/s	(4)	751.7 m/s

Answer (2)

Sol.
$$\frac{v_{Ar}}{v_{Cl}} = \sqrt{\frac{M_{Cl}}{M_{Ar}}}$$

 $\Rightarrow v_{Ar} = \sqrt{\frac{71}{40}} \times 490$

- ≅ 651.7
 34. Two satellites A and B move round the earth in the same orbit. The mass of A is twice the mass of B.
 - The quantity which is same for the two satellites will be
 - (1) Speed
- (2) Kinetic energy
- (3) Total energy
- (4) Potential energy

Answer (1)

- Sol. Speed will be independent of mass of satellite.
- 35. A particle is executing simple harmonic motion (SHM). The ratio of potential energy and kinetic energy of the particle when its displacement is half of its amplitude will be

(3) 2 : 1 Answer (2)

Sol.
$$\frac{P.E.}{K.E.} = \frac{x^2}{A^2 - x^2} = \frac{\frac{1}{4}}{\frac{3}{4}} = \frac{1}{3}$$

 Given below are two statements:
 Statement I : The diamagnetic property depends on temperature.

Statement II : The induced magnetic dipole moment in a diamagnetic sample is always opposite to the magnetizing field.

In the light of given statements, choose the **correct** answer from the options given below

- (1) Both Statement I and Statement II are False
- (2) Statement I is incorrect but Statement II is true
- (3) Statement I is correct but Statement II is flase
- (4) Both Statement I and Statement II are true

Answer (2)

- Sol. Diamagnetic materials oppose external field.
- 37. A wire of resistance 160Ω is melted and drawn in a wire of one-fourth of its length. The new resistance of the wire will be

(1) 16 Ω	(2) 10 Ω
(3) 640 Ω	(4) 40 Ω

Answer (2)

Sol. *R*′ = *R*/16

R′ = 10Ω

- A body cools from 80°C to 60° in 5 minutes. The temperature for the surrounding is 20°C. The time it takes to cool from 60°C to 40°C is
 - (1) 450 s (2) 420 s
 - (3) 500 s (4) $\frac{25}{3}$ s

Answer (3)

Sol.
$$\frac{20}{5} = c(50)$$

 $\frac{20}{x} = c(30)$
 $\Rightarrow x = \frac{25}{3}$ minutes

= 500 s

39. Match List I with List II

	List-I		List-II
Α.	Spring constant	I.	[T ⁻¹]
В.	Angular speed	II.	[MT ⁻²]
C.	Angular momentum	III.	[ML ²]
D.	Moment of Inertia	IV.	[ML ² T ⁻¹]

Choose the correct answer from the options given below:

- (1) A-I, B-III, C-II, D-IV
- (2) A-IV, B-I, C-III, D-II
- (3) A-II, B-I, C-IV, D-III
- (4) A-II, B-III, C-I, D-IV

Answer (3)

Sol. $[k] = [M^1L^0T^{-2}]$

 $ω = [T^{-1}]$

40. In an n-p-n common emitter (CE) transistor the collector current changes from 5 mA to 16 mA for the change in base current from 10 μ A and 200 μ A, respectively. The current gain of transistor is _____

(4) 9

(1) 110 (2) 210

(3) 0.9

Answer (1)

Sol. ∆*I*_c = 11 mA

$$\Delta I_b = 100 \ \mu A$$

$$\beta = \frac{\Delta I_c}{\Delta I_b} = 110$$

41. An ice cube has a bubble inside. When viewed from one side the apparent distance of the bubble is 12 cm. When viewed from the opposite side, the apparent distance of the bubble is observed as 4 cm. If the side of the ice cube is 24 cm, the refractive index of the ice cube is

(1)
$$\frac{3}{2}$$
 (2) $\frac{2}{3}$
(3) $\frac{6}{5}$ (4) $\frac{4}{3}$

Answer (1)

Sol.
$$\frac{x}{\mu} = 12$$

 $\frac{a-x}{\mu} = 4$
 $24 - 12 \ \mu = 4 \ \mu$
 $\mu = \frac{24}{16} = 1.5$

- 42. The amplitude of 15 sin(1000 πt) is modulated by 10 sin(4 πt) signal. The amplitude modulated signal contains frequencies of
 - A. 500 Hz B. 2 Hz
 - C. 250 Hz D. 498 Hz
 - E. 502 Hz

Choose the correct answer from the options given below

(1) A and B only(2) A and C only(3) A and D only(4) A, D and E only

Answer (4)

Sol. Frequencies in the system

$$=\frac{1000\,\pi}{2},\frac{996\,\pi}{2},\frac{1004\,\pi}{2}$$

2π '2π '2π

= 500 Hz, 498 Hz, 502 Hz

- 43. An engine operating between the boiling and freezing points of water will have
 - A. Efficiency more than 27%
 - B. Efficiency less than the efficiency of a Carnot engine operating between the same two temperatures.
 - C. Efficiency equal to 27%.
 - D. Efficiency less than 27%.

(3) B and D only

Choose the correct answer from the options given below

- (1) B, C and D only (2) A and B only
 - (4) B and C only
- Answer (3)

Sol.
$$\eta_C = 1 - \frac{273}{373} = 26.8\%$$

$$\Rightarrow \eta_{\text{engine}} < \eta_{\text{carnot}} = \eta_{C}$$

- 44. Three forces $F_1 = 10$ N, $F_2 = 8$ N, $F_3 = 6$ N are acting on a particle of mass 5 kg. The forces F_2 and F_3 are applied perpendicularly so that particle remains at rest. If the force F_1 is removed, then the acceleration of the particle is
 - (1) 7 ms^{-2} (2) 0.5 ms^{-2} (3) 4.8 ms^{-2} (4) 2 ms^{-2}

Answer (4)

- Sol. $\sqrt{F_2^2 + F_3^2} = 10 \text{ N}$ $\Rightarrow a = \frac{10}{5} = 2 \text{ m/s}^2$
- Given below are two statements: one is labelled as
 Assertion A and the other is labelled as Reason
 R.

Assertion A : If an electric dipole of dipole moment 30×10^{-5} Cm is enclosed by a closed surface, the net flux coming out of the surface will be zero.

Reason R : Electric dipole consists of two equal and opposite charges.

In the light of above, statements, choose the **correct** answer from the options given below.

- (1) Both A and R are true and R is the correct explanation of A
- (2) A is false but R is true
- (3) A is true but R is false
- (4) Both A and R are true and R is NOT the correct explanation of A

Answer (1)

- **Sol.** $\phi = \frac{q_{in}}{\epsilon_0} = 0$
- 46. Given below are two statements:

Statement I: When the frequency of an a.c source in a series LCR circuit increases, the current the circuit first increases, attains a maximum value and then decreases.

Statement II : In a series LCR circuit, the value of power factor at resonance is one.

In the light of given statements, choose the most appropriate answer from the options given below.

- (1) Statement I is incorrect but Statement II is true.
- (2) Both Statement I and Statement II are false.

(3) Both Statement I and Statement II are true.(4) Statement I is correct but Statement II is false.

Answer (3)

Sol. Z first decreases and then increases

 $\phi_{\text{resonance}} = 1 \text{ as } Z = R$

47. A 12.5 eV electron beam is used to bombard gaseous hydrogen at room temperature. The number of spectral lines emitted will be:

Answer (4)

Sol. *h*v_{max} = 12.5 eV

 \Rightarrow maximum excitation level = 3

$$\Rightarrow$$
 spectral lines possible = $3C_2$

48. A ball is thrown vertically upward with an initial velocity of 150 m/s. The ratio of velocity after 3 s

	and 5 s is $\frac{x+1}{x}$. The value	ue of x is
	{take, g = 10 m/s²}	
	(1) 10	(2) -5
	(3) 6	(4) 5
Ansv	wer (4)	
Sol.	$\frac{v_3}{v_5} = \frac{150 - 30}{150 - 50} = \frac{120}{100}$	

49. Given below are two statements:

 $=\frac{6}{5}$

Statement I : A truck and a car moving with same kinetic energy are brought to rest by applying breaks which provide equal retarding forces. Both come to rest in equal distance.

Statement II : A car moving towards east takes a turn and moves towards north, the speed remains unchanged. The acceleration of the car is zero.

In the light of given statements, choose the most appropriate answer from the options given below

- (1) Statement I is correct but statement II is incorrect.
- (2) Statement I is incorrect but statement II is correct.
- (3) Both statement I and Statement II are correct.
- (4) Both statement I and statement II are incorrect.

Answer (1)

Sol. $WD = Fx = \Delta KE$

 $x_1 = x_2$

50. The ratio of escape velocity of a planet to the escape velocity of earth will be:-

Given: Mass of the planet is 16 times mass of earth and radius of the planet is 4 times the radius of earth.

(1) 4:1 (2) 1:4

(3)
$$1:\sqrt{2}$$
 (4) $2:1$

Answer (4)

Sol.
$$v = \sqrt{\frac{2GM}{R}}$$

 $\Rightarrow \frac{v_p}{v_e} = \sqrt{\frac{M_p}{M_e}} \times \sqrt{\frac{R_e}{R_p}} = 4 \times \frac{1}{2}$
 $= 2:1$

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

 64 identical drops each charged upto potential of 10 mV are combined to form a bigger drop. The potential of the bigger drop will be _____ mV.

Answer (160)

Sol.
$$V' = \frac{kQ'}{R'}$$

 $V' = \frac{k \times 64 \times Q}{4R} = 16 \times V = 160 \text{ mV}$

52. A common example of alpha decay is

$${}^{238}_{92}\text{U} \longrightarrow {}^{234}_{90}\text{Th} + {}_{2}\text{He}^4 + \text{G}$$

Given :

 ${}^{4}_{2}$ He = 4.00260 u and 1u = 931.5 $\frac{\text{MeV}}{c^{2}}$

The energy released (Q) during the alpha decay of $^{238}_{92}$ U is _____ MeV.

Answer (4)

Sol. Q = 931.5 × 00.0044 = 4.0986

53. Glycerin of density 1.25×10^3 kg m⁻³ is flowing through the conical section of pipe. The area of cross-section of the pipe at its ends are 10 cm^2 and 5 cm² and pressure drop across its length is 3 Nm^{-2} . The rate of flow of glycerin through the pipe is $x \times 10^{-5} \text{ m}^3 \text{s}^{-1}$. The value of *x* is _____.

Answer (4)

Sol.
$$A_1 = 10 \text{ cm}^2; A_2 = 5 \text{ cm}^2$$

 $\Delta P = -3 \text{ N/m}^2$
 $-\frac{1}{2}\rho v_1^2 + \frac{1}{2}\rho v_2^2 = \Delta P$
 $= v_1^2(3) = \frac{3 \times 2}{1.25 \times 10^3}$
 $\Rightarrow v_1 = \frac{\sqrt{2}}{\sqrt{1250}}$
 $Q = A_2 v_2 = \frac{10 \times \sqrt{2}}{\sqrt{1250}} = 4 \times 10^{-5}$

54. A conducting circular loop is placed in a uniform magnetic field of 0.4 T with its plane perpendicular to the field. Somehow, the radius of the loop starts expanding at a constant rate of 1 mm/s. The magnitude of induced emf in the loop at an instant when the radius of the loop is 2 cm will be _____ μ V.

Answer (50)

Sol.
$$\phi = 2\pi R \frac{dR}{dt} \times B$$

= $2 \times \frac{22}{7} \times 2 \times 10^{-2} \times 10^{-3} \times 0.4$
= 5×10^{-5} V = 50.28 μ V

55. A compass needle oscillates 20 times per minute at a place where the dip is 30° and 30 times per minute where the dip is 60°. The ratio of total magnetic field due to the earth at two places

respectively is
$$\frac{4}{\sqrt{x}}$$
. The value of x is

Answer (243)

Sol.
$$T = 2\pi \sqrt{\frac{l}{MB_H}}$$

 $T = 2\pi \sqrt{\frac{l}{MB\cos\theta}}$

$$\frac{20}{30} = \sqrt{\frac{B_1}{B_2} \frac{\sqrt{3}/2}{1/2}}$$
$$\frac{4}{9} = \frac{B_1}{B_2} \sqrt{3}$$
$$\frac{B_1}{B_2} = \frac{4}{\sqrt{243}}$$

56. Two convex lenses of focal length 20 cm each are placed coaxially with a separation of 60 cm between them. The image of the distant object formed by the combination is at _____ cm from the first lens.

Answer (100)

Sol. $u_1 = \infty$, $f_1 = 20$ cm, $v_1 = 20$ cm

 $u_2 = 40 \text{ cm}, f_2 = 20 \text{ cm}, v_2 = 40 \text{ cm}$

 \Rightarrow x = 40 cm + 60 cm

= 100 cm

and road is 0.04]

Answer (784)

Sol. *v* = 80 kph

$$P_{\text{friction}} = (0.04) (500\text{g}) \times 80 \times \frac{5}{18} \text{ watts}$$
$$P = \frac{20 \times 80 \times 5 \times 9.8}{18}$$

$$W = \frac{20 \times 80 \times 5}{18} \times \frac{4 \times 10^3}{80 \times \frac{5}{18}} \times 9.8$$

= 784 kJ

58. For a certain organ pipe, the first three resonance frequencies are in the ratio of 1:3:5 respectively. If the frequency of fifth harmonic is 405 Hz and the speed of sound in air is 324 ms⁻¹ the length of the organ pipe is _____ m.

Answer (1)

Sol.
$$f_5 = 405$$

$$\Rightarrow \frac{5v}{4l} = 405$$

$$\Rightarrow l = \frac{405 \times 4}{5 \times 324}$$

$$= 1 \text{ m}$$

59. For rolling spherical shell, the ratio of rotational kinetic energy and total kinetic energy is $\frac{x}{5}$. The value of x is _____.

Answer (2)

Sol.
$$\frac{K \cdot E_R}{K \cdot E_T} = \frac{\frac{2}{3}MR^2\omega^2}{\frac{5}{3}MR^2\omega^2} = \frac{2}{5}$$

60. The current flowing through a conductor connected across a source is 2 A and 1.2 A at 0°C and 100°C respectively. The current flowing through the conductor at 50°C will be _____ × 10² mA.

Answer (15)

Sol.
$$\frac{R_1}{R_2} = \frac{1 \cdot 2}{2} = \frac{1}{1 + \alpha 100}$$

 $1 + \alpha 100 = \frac{2}{1.2}$
 $\alpha 100 = \frac{0.8}{1.2} = \frac{2}{3}$
 $\alpha 50 = \frac{1}{3}$
 $1 + \alpha 50 = \frac{4}{3}$
 $\Rightarrow \frac{l_3}{l_1} = \frac{3}{4} \times 2 \text{ A} = 1.5 \text{ A}$
 $= 15 \times 10^2 \text{ mA}$

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

61. The incorrect statement regarding the reaction given below is

$$Me - N - Me$$

$$O + NaNO_2 + HX \longrightarrow B'$$

$$A'$$

- (1) The product 'B' formed in the above reaction is p-nitroso compound at low temperature
- (2) 'B' is N-nitroso ammonium compound
- (3) The reaction occurs at low temperature
- (4) The electrophile involved in the reaction is NO⁺

Answer (2)

Sol. $NaNO_2 + HX \longrightarrow HNO_2 + NaX$



- ... Statement (2) is incorrect
- 62. The bond order and magnetic property of acetylide ion are same as that of

(1)	O_2^+		(2)	N_2^+	

(3) NO ⁺	(4)	O_2^-
---------------------	-----	---------

Answer (3)

Species	Bond Order	Magnetic moment
$HC \equiv C^-$	3	0
O_2^+	2.5	√3 B.M
N_2^+	2.5	√3 В.М
NO ⁺	3	0
O_2^-	1.5	√3 B.M
	Species $HC \equiv C^-$ O_2^+ N_2^+ NO^+ O_2^-	Species Bond Order $HC \equiv C^-$ 3 O_2^+ 2.5 N_2^+ 2.5 NO^+ 3 O_2^- 1.5

63. Match List I with List II

	List I Complex		List II CFSE (∆₀)
Α.	[Cu(NH ₃) ₆] ²⁺	١.	-0.6
В.	[Ti(H ₂ O) ₆] ³⁺	II.	-2.0
C.	[Fe(CN) ₆] ^{3–}	III.	-1.2
D.	[NiF ₆] ^{4–}	IV.	-0.4

Choose the correct answer from the options given below:

- (1) A(III), B(IV), C(I), D(II)
- (2) A(I), B(IV), C(II), D(III)
- (3) A(I), B(II), C(IV), D(III)
- (4) A(II), B(III), C(I), D(IV)

Answer (2)

Sol.

(A) [Cu(NH ₃) ₆] ²⁺	CFSE
Cu ²⁺ : 3 d^6 , $t^6_{2q} e^3_q$	$= (-6 \times 0.4 + 3 \times 0.6) \Delta_0$
	= − 0.6 Δ ₀
(B) [Ti(H ₂ O) ₆] ³⁺	$CFSE = -1 \times 0.4\Delta_0$
Ti^{3_+} : $3d^1$, $t^1_{2g} e^0_g$	$= -0.4 \Delta_0$
(C) [Fe(CN) ₆] ³⁻	$CFSE = -5 \times 0.4\Delta_0$
Fe^{3+} : $3d^{5}$, t_{2g}^{5} e_{g}^{0}	= $-2.0 \Delta_0$
(D) [NiF ₆] ^{4–}	CFSE
Ni^{2+} : $3d^8$, $t^6_{2g} e^2_g$	$= (-6 \times 0.4 + 2 \times 0.6) \Delta_0$
	$= -1.2 \Delta_0$

A - I; B - IV; C - II; D - III

64. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R
 Assertion A: In the Ellingham diagram, a sharp change in slope of the line is observed from Mg → MgO at ~ 1120°C

Reason R: There is a large change of entropy associated with the change of state

In the light of the above statements, choose the *correct* answer from the options given below

- (1) Both A and R are true but R is NOT the correct explanation of A
- (2) A is false but R is true
- (3) Both A and R are true and R is the correct explanation of A
- (4) A is true but R is false

Answer (3)

CH. – Č = CH – CH.

Synthetic rubber

>PbO,

(cathode)

Sol. In the Ellingham diagram, a sharp change in slope Sol. of the line is observed for Mg - MgO at ~1120°C CI $CH_2 = C - CH = CH_2$ because that is the boiling point of magnesium. A 2-chloro-1, 3-butadiene There is a large increase in entropy associated with the change of state of magnesium. So, both В Nylon-2-nylon-6 Biodegradable polymer Assertion (A) and Reason (R) are true and (R) is С Polyacrylonitrile Addition polymer the correct explanation of (A). D Dacron Polyester 65. In the given reaction cycle A-II; B-I; C-IV; D-III $CaCl_2 + Na_2CO_3 \longrightarrow X + Y$ 67. For lead storage battery pick the correct statements A. During charging of battery, PbSO₄ on anode is Ζ converted into PbO₂ X, Y and Z respectively are B. During charging of battery, PbSO₄ on cathode is Х Υ Ζ converted into PbO₂ C. Lead storage battery consists of grid of lead (1) $CaCO_3$ NaCl KCI packed with PbO₂ as anode (2) $CaCO_3$ NaCl HCI D. Lead storage battery has ~ 38% solution of (3) CaO NaCI + CO₂ NaCl sulphuric acid as an electrolyte NaCI + CO₂ (4) CaO KCI Choose the correct answer from the options given Answer (2) below: **Sol.** $CaCl_2 + Na_2CO_3 \longrightarrow CaCO_3 + 2NaCl$ (1) A, B, D only (2) B, C, D only $CaCO_3 + 2HCI \longrightarrow CaCl_2 + CO_2(g) + H_2O(l)$ (3) B, C only (X) (Z) (4) B, D only ∴ (X) CaCO₃ Answer (4) (Y) NaCl Sol. (Z) HCI Pb ← 66. Match List I with List II (Anode)

~ 38% H,SO,

The lead storage battery is as shown in diagram. During charging of battery PbSO₄ deposited on cathode is converted in PbO2 and PbSO4 deposited on anode is converted into Pb. The electrolyte used in battery is H₂SO₄ which is about 38% by mass.

68. Given below are two statements:

Statement I: SbCl₅ is more covalent than SbCl₃

Statement II: The higher oxides of halogens also tend to be more stable than the lower ones.

In the light of the above statements, choose the most appropriate answer from the options given below.

	List I (Example)		List II (Type)
А.	2-chloro-1, 3-butadiene	I.	Biodegradable polymer
В.	Nylon 2-nylon 6	II.	Synthetic Rubber
C.	Polyacrylonitrile	III.	Polyester
D.	Dacron	IV.	Addition Polymer

Choose the correct answer from the options given below:

- (1) A(II), B(IV), C(I), D(III)
- (2) A(II), B(I), C(IV), D(III)
- (3) A(IV), B(I), C(III), D(II)

(4) A(IV), B(III), C(I), D(II)

Answer (2)

JEE (Main)-2023 : Phase-2 (12-04-2023)-Morning

- (1) Statement I is incorrect but statement II is correct
- (2) Both Statement I and Statement II are incorrect
- (3) Both Statement I and Statement II are correct
- (4) Statement I is correct but statement II is incorrect

Answer (3)

- Sol. SbCl₅ is more covalent than SbCl₃ due to higher polarisation power of Sb[∨] than that of Sb^{III}. Higher oxides of halogens are more stable than lower ones due to the formation of more number of bonds, which results in higher release of energy. So, both the statements I and II are correct.
- 69. Four gases, A, B, C and D have critical temperatures 5.3, 33.2, 126.0 and 154.3K respectively

For their adsorption on a fixed amount of charcoal, the correct order is :

- (1) C > D > B > A
- (2) C > B > D > A
- $(3) \quad \mathsf{D} > \mathsf{C} > \mathsf{B} > \mathsf{A}$
- (4) D > C > A > B

Answer (3)

Sol. The extent of adsorption of different gases on the surface of a fixed amount of charcoal is directly proportional to their critical temperatures.

Order of T_c D > C > B > A

Order of adsorption D > C > B > A

70. Match List I with List II

	List I	List II				
А.	Nitrogen oxides in air	I.	Eutrophication			
В.	Methane in air	II.	pH of rain water becomes 5.6			
C.	Carbon dioxide	III.	Global warming			
D.	Phosphate fertilisers in water	IV.	Acid rain			

Choose the correct answer from the options given below :

- (1) A-II, B-III, C-I, D-IV
- (2) A-I, B-II, C-III, D-IV
- (3) A-IV, B-III, C-II, D-I
- (4) A-IV, B-II, C-III, D-I

Answer (3)

Sol.

A.	Nitrogen oxides in air	IV	Acid rain
В.	Methane in air	III	Global warming
C.	Carbon dioxide	II	pH of rain water becomes 5.6
D.	Phosphate fertilisers in water	I	Eutrophication

- ∴ A-IV; B-III; C-II; D-I
- 71. In the following reaction



Answer (2)

Sol.







Answer (3)

Sol.



73. Given below are two statement : one is labelled as Assertion A and the other is labelled as Reason R Assertion A : 5f electron can participate in bonding to a far greater extent than 4f electrons

Reason R : 5f orbitals are not as buried as 4f orbitals

In the light of the above statements, choose the correct answer from the options given below

- (1) A is false but R is true
- (2) Both A and R are true and R is the correct explanation of A
- (3) A is true but R is false
- (4) Both A and R are true but R is **NOT** the correct explanation of A

Answer (2)

Sol. 5f electron can participate in bonding to a far greater extent than 4f electron because 5f orbitals are more exposed than 4f orbitals.

So, Assertions (A) is true

5f orbitals are not as buried as 4f orbitals.

So, reason (R) is also true and (R) is the correct explanation of (A) $% \left(A\right) =0$

74. 2-hexene
$$\xrightarrow{(i) O_3}$$
 Products

The two products formed in above reaction are-

- (1) Butanal and acetaldehyde
- (2) Butanoic acid and acetaldehyde
- (3) Butanal and acetic acid
- (4) Butanoic acid and acetic acid

1. O₃

Answer (4)

Sol.

$$\Rightarrow \begin{array}{c} CH_{3}COOH + CH_{3}-CH_{2}-CH_{2}-COOH \\ (Acetic acid) (Butanoic acid) \end{array}$$

75. Match List I with List II

List I Type of Hydride			List II Example		
Α.	Electron deficient hydride	I.	MgH ₂		
В.	Electron rich hydride	II.	HF		
C.	Electron precise hydride	111.	B2H6		
D.	Saline hydride	IV.	CH4		

Choose the correct answer from the options given below :

- (1) A-III, B-II, C-IV, D-I
- (2) A-II, B-III, C-I, D-IV
- (3) A-II, B-III, C-IV, D-I
- (4) A-III, B-II, C-I, D-IV

Answer (1)

Sol.

- A Electron deficient hydride III B₂H₆
- B Electron rich hydride II HF
- C Electron precise hydride IV CH₄
- D Saline hydride I MgH₂
- 76. The density of alkali metals is in the order
 - (1) K < Cs < Na < Rb
 - (2) Na < Rb < K < Cs
 - (3) Na < K < Cs < Rb
 - (4) K < Na < Rb < Cs
- Answer (4)

Sol. Density of alkali metals increases down the group with the exception of potassium. Therefore, correct order of density of given alkali metals is

77. Given below are two statements:

Statement I: Boron is extremely hard indicating its high lattice energy

Statement II: Boron has highest melting and boiling point compared to its other group members.

In the light of the above statements, choose the **most appropriate** answer from the options given below

- (1) Both Statement I and Statement II are incorrect
- (2) Statement I is correct but Statement II is incorrect
- (3) Both statement I and Statement II are correct
- (4) Statement I is incorrect but Statement II is correct

Answer (3)

Sol. Boron is extremely hard as it exists as B₁₂ icosahedral molecular units which accounts for its high lattice energy. So, statement-I is correct.

Boron has the highest melting point and boiling point than other members of its group due to its network structure. So, statement-II is also correct.

 The major product 'P' formed in the following sequence of reactions is





Answer (4)



79. A metal chloride contains 55.0% of chlorine by weight. 100 mL vapours of the metal chloride at STP weigh 0.57 g. The molecular formula of the metal chloride is

(Given: Atomic mass of chlorine is 35.5 u)

- (1) MCl₄
- (2) MCI₃
- (3) MCl₂
- (4) MCI

Answer (3)

Sol. Let the formula of metal chloride be MCI_x

Mass of 100 mL of vapours of MCI_x at

STP = 0.57 g

$$\therefore \quad \frac{100 \times M}{22400} = 0.57$$

 \therefore Molar mass of MCl_x = 127.68 g mol⁻¹

% of CI =
$$\frac{35.5 \times 100}{127.68} = 55$$

 \Rightarrow x = 2

... Formula of metal chloride is MCl₂

80. Correct statements for the given reaction are:

$$OH \rightarrow OH$$

 $OH \rightarrow OH$
 $OH \rightarrow B$

- A. Compound 'B' is aromatic
- B. The completion of above reaction is very slow
- C. 'A' shows tautomerism
- D. The bond lengths of C-C in compound B are found to be same

Choose the correct answer from the options given below.

- (1) B, C and D only (2) A, B and C only
- (3) A, C and D only (4) A, B and D only

Answer (3)



Compound (A), also called squaric acid is a strong acid. So, above reaction proceeds very fast. All C - C bond lengths in (B) are same due to resonance. (A) shows tautomerism.

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

81. At 600 K, the root mean square (rms) speed of gas X (molar mass = 40) is equal to the most probable speed of gas Y at 90 K. The molar mass of the gas Y is _____ g mol⁻¹. (Nearest integer)

Answer (4)

Sol.
$$\frac{V_{rms} \text{ of } X}{V_{rmp} \text{ of } Y} = \sqrt{\frac{3 T_X M_Y}{2 T_Y M_X}}$$

$$1 = \sqrt{\frac{3 \times 600 \times M_Y}{2 \times 90 \times 40}} = \sqrt{\frac{M_Y}{4}}$$

 $M_{\rm Y} = 4 \text{ gm mol}^{-1}$

82. The reaction 2NO + $Br_2 \rightarrow 2NOBr$ takes place through the mechanism given below

 $NO + Br_2 \implies NOBr_2$ (fast)

 $\text{NOBr}_2 + \text{NO} \rightarrow 2\text{NOBr} \text{ (slow)}$

The overall order of the reaction is _____.

Answer (3)

Sol. On applying LOMA over slowest step (r.d.s.)

 $R = k[NOBr_2][NO]$

On applying LOMA on equilibrium of Step I

$$k = \frac{[NOBr_2]}{[NO] [Br_2]}$$

 $[NOBr_2] = k [NO][Br_2]$

Hence overall rate equation will be

$$\mathsf{R} = \mathsf{k} \left[\mathsf{NO}\right]^2 \left[\mathsf{Br}_2\right]$$

$$= k' [NO]^2 [Br_2]$$

Hence, overall order will be 3.

80 mole percent of MgCl₂ is dissociated in aqueous solution. The vapour pressure of 1.0 molal aqueous solution of MgCl₂ at 38°C is _____ mm Hg. (Nearest integer)

Given: Vapour pressure of water at 38°C is 50 mm Hg

Answer (48)

$$MgCl_{2} \longrightarrow Mg^{2+} + 2 Cl^{-}$$
Sol. 1 0 0
1-0.8 0.8 1.6

Hence overall molality will be equal to = 2.6

$$\frac{p^{\circ} - p}{p^{\circ}} = \frac{2.6}{\frac{1000}{18} + 2.6}$$

JEE (Main)-2023 : Phase-2 (12-04-2023)-Morning

For dil solution

$$\frac{p^{\circ} - p}{p^{\circ}} = \frac{2.6}{\frac{1000}{18}}$$

 $p=47.66\simeq 48~mm~Hg$

 In an oligopeptide named Alanylglycylphenyl alanyl isoleucine, the number of sp² hybridised carbons is

Answer (10)

Sol. The given Oligopeptide has the following structure

$$\begin{array}{c} O & O & O \\ II \\ H_2 N - CH - {}^{*}C - NH - CH_2 - {}^{*}C - NH - CH - {}^{*}C - NH - CH - {}^{*}C - OH \\ I \\ CH_3 & {}^{*}CH_3 - {}^{*}CH - CH_2 - CH_3 \end{array}$$

It has 10 sp² hybridised C atoms given with star in the above structure.

85. One mole of an ideal gas at 350 K is in a 2.0 L vessel of thermally conducting walls, which are in contact with the surroundings. It undergoes isothermal reversible expansion from 2.0 L to 3.0 L against a constant pressure of 4 atm. The change in entropy of the surroundings (Δ S) is _____ J K⁻¹ (Nearest integer)

Given: $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$.

Answer (03)

Sol. For isothermal process Q = -W

The W for isothermal reversible process is

$$W = -nRT \ln \frac{V_2}{V_1}$$
$$\Delta S_{surrounding} = -nR \ln \frac{V_2}{V_1}$$
$$= -1 \times 8.314 \times 2.303 \times \log \frac{3}{2}$$
$$= -3.37 \text{ JK}^{-1}$$
$$\approx -3 \text{ JK}^{-1}$$

Note : The given process is mentioned as isothermal reversible process hence the $\Delta S_{surrounding}$ is calculated accordingly.



The value of x in compound 'D' is ____

Answer (15)



87. Three organic compounds A, B and C were allowed to run in thin layer chromatography using hexane and gave the following result (see figure). The R_f value of the most polar compound is _____ × 10⁻²



Answer (25)

- **Sol.** In thin layer chromatography using hexane, the least polar compound will rise to maximum height and most polar compound will rise to minimum height.
 - ... Rf value for most polar compound

$$=\frac{2}{8}=0.25$$

- $= 25 \times 10^{-1}$
- Values of work function (W₀) for a few metals are given below

Metal	Li	Na	К	Mg	Cu	Ag
W₀/eV	2.42	2.3	2.25	3.7	4.8	4.3

The number of metals which will show photoelectric effect when light of wavelength 400 nm falls on it is

Given: $h = 6.6 \times 10^{-34} \text{ J s}$

 $c = 3 \times 10^8 \text{ m s}^{-1}$

 $e = 1.6 \times 10^{-19} C$

Answer (3)

Sol. Energy of incident photon = $\frac{hc}{\lambda}$

$$= \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{400 \times 10^-} J$$
$$= \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{400 \times 10^{-9} \times 1.6 \times 10^{-19}} eV$$
$$= 3.1 eV$$

... Li, Na and K will show photoelectric effect.

- 89. The mass of NH₃ produced when 131.8 kg of cyclohexane carbaldehyde undergoes Tollen's test is ______ kg. (Nearest Integer)
 Molar mass of C = 12 g/mol
 N = 14 g/mol
 - O = 16 g/mol

Answer (60)

Sol.
$$RCHO + 2[Ag(NH_3)_2]OH \rightarrow RCOONH_4 + 2Ag$$

 $3NH_3 + H_2O$

RCHO =
$$\frac{131.8 \times 10^3}{112} = 1.176 \times 10^3$$

1 mole of aldehyde produces 3 moles of NH₃

 1.176×10^3 mol aldehyde will produce

= 3 x 1.176 x 10³ moles of NH₃

Mass of NH₃ produced = $3 \times 1.176 \times 10^3 \times 17$

$$= 59.97 \times 10^3 \text{ g}$$

 An analyst wants to convert 1 L HCl of pH = 1 to a solution of HCl of pH 2. The volume of water needed to do this dilution is _____ mL. (Nearest integer)

Answer (9000)

Sol. The concentration of H⁺ or say HCl in both the given solution is 10^{-1} and 10^{-2} mole L⁻¹ respectively.

For the given amount of HCI the concentration depends over dilution hence

$$\frac{C_1}{C_2} = \frac{V_2}{V_1}$$

$$\frac{10^{-1}}{10^{-2}} = \frac{V_2}{1L}$$

$$V_2 = 10 L = 10000 \text{ mL}$$

$$\Delta V = 10000 - 1000 \text{ mL} = 9000 \text{ mL}$$